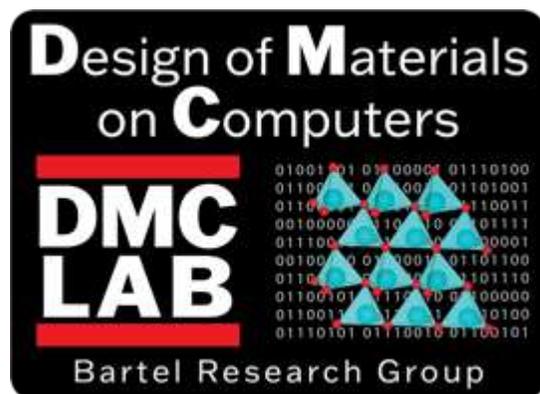




The role of computation in materials synthesis and characterization

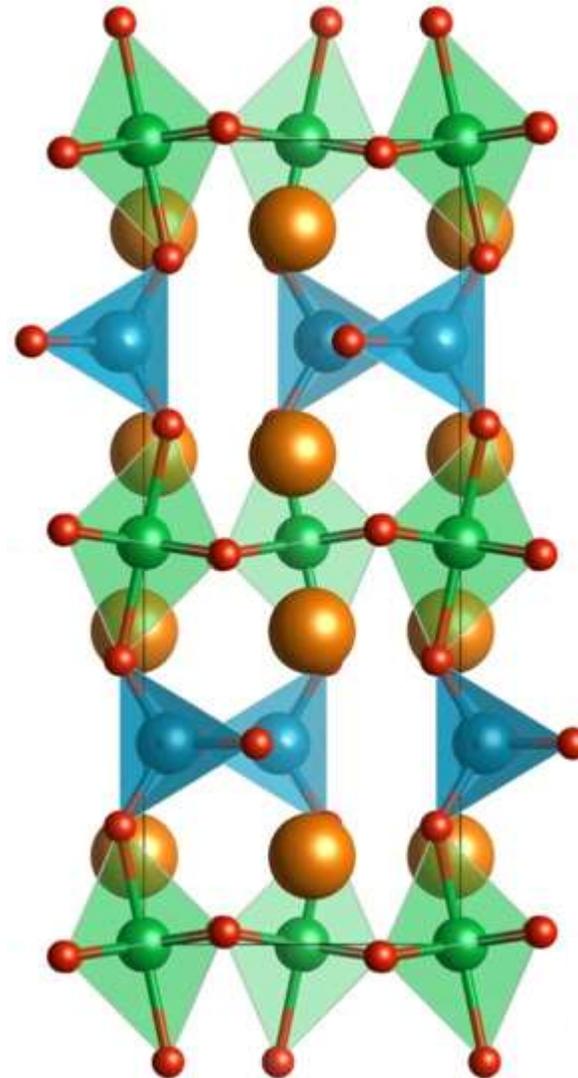
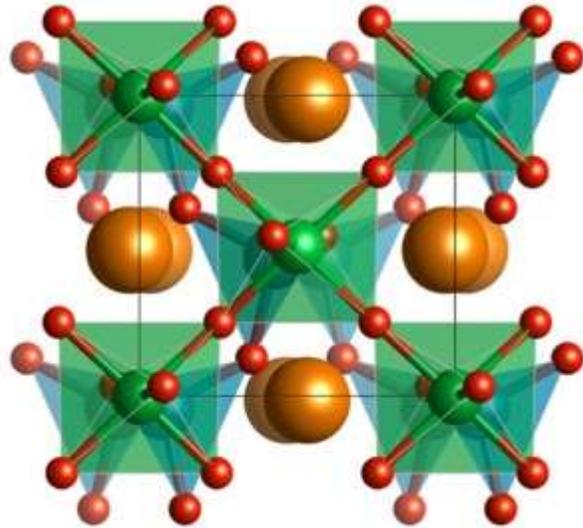
Nathan Szymanski

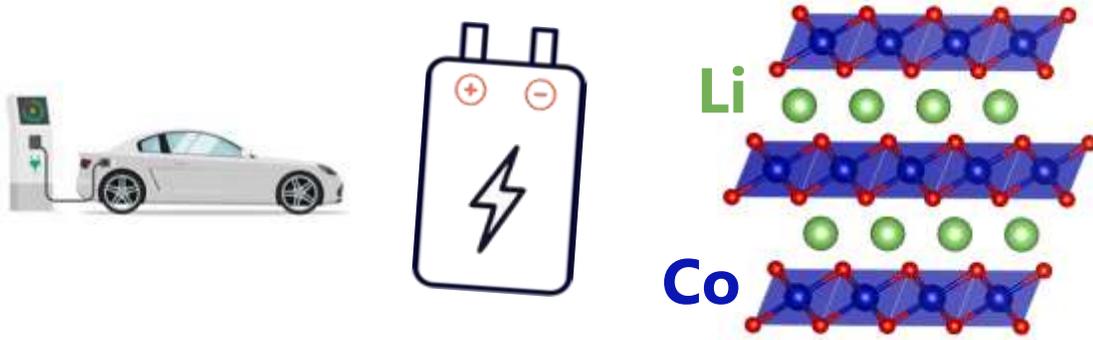


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Chemical Engineering
& Materials Science
UNIVERSITY OF MINNESOTA

Research Seminar for Faculty Search 2025

Inorganic crystalline materials





LiCoO₂ as a Li-ion cathode:

- Li can be reversibly (de)intercalated
- Co^{3+/4+} redox occurs at high voltage

Innovation is driven by materials with “just the right” properties

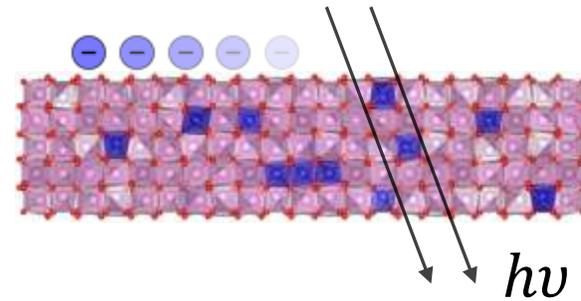


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In_{2-x}Sn_xO₃ as a transparent conductor:

- High transparency to visible light
- Good electrical conductivity



Innovation is driven by materials with “just the right” properties

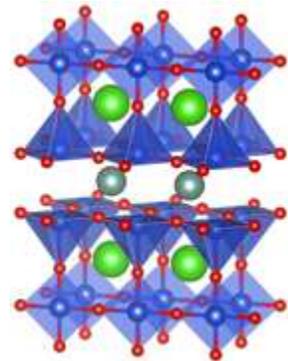
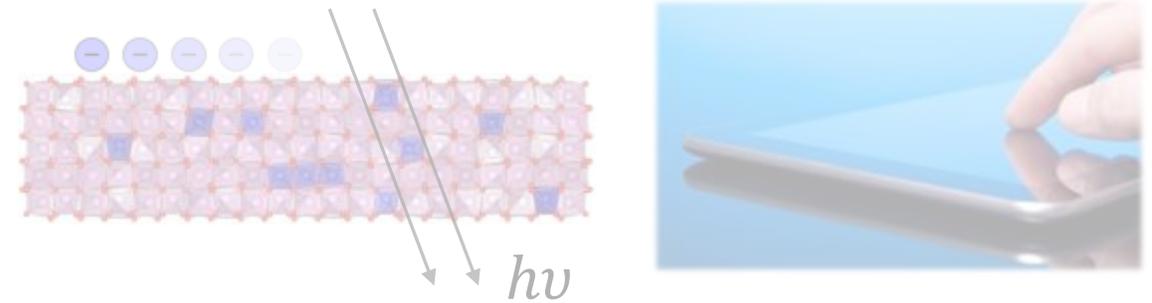


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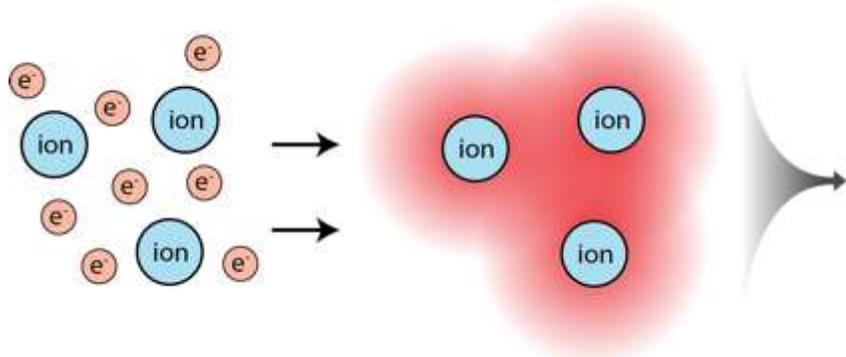


YBa₂Cu₃O_{7-x} as a high-*T_c* superconductor:

- Superconductivity across CuO₂ planes
- Good tolerance to oxygen vacancies (*x*)

Computations can assist in designing new materials

Density functional theory (DFT)



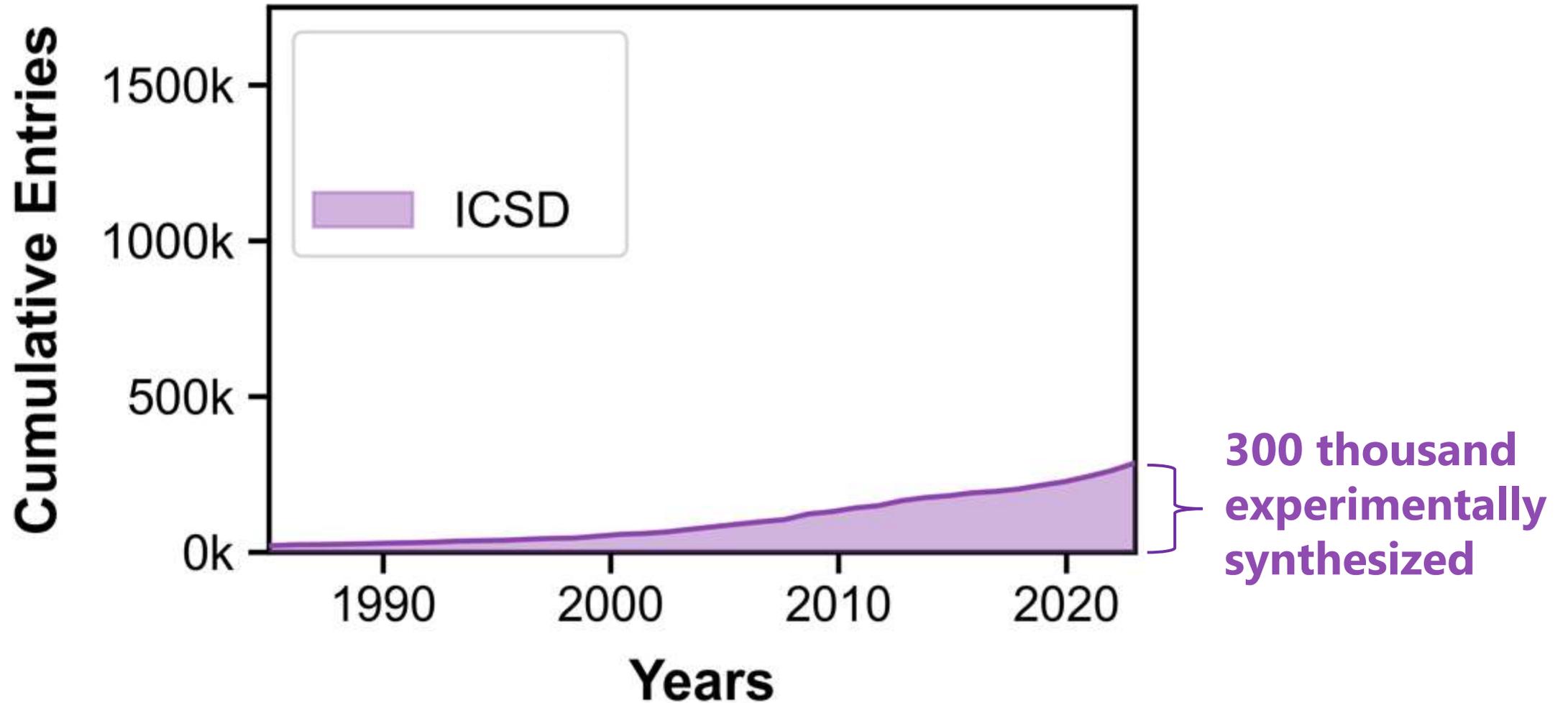
Internal **energy**
Electronic properties
Response functions

Provides an answer to the questions:

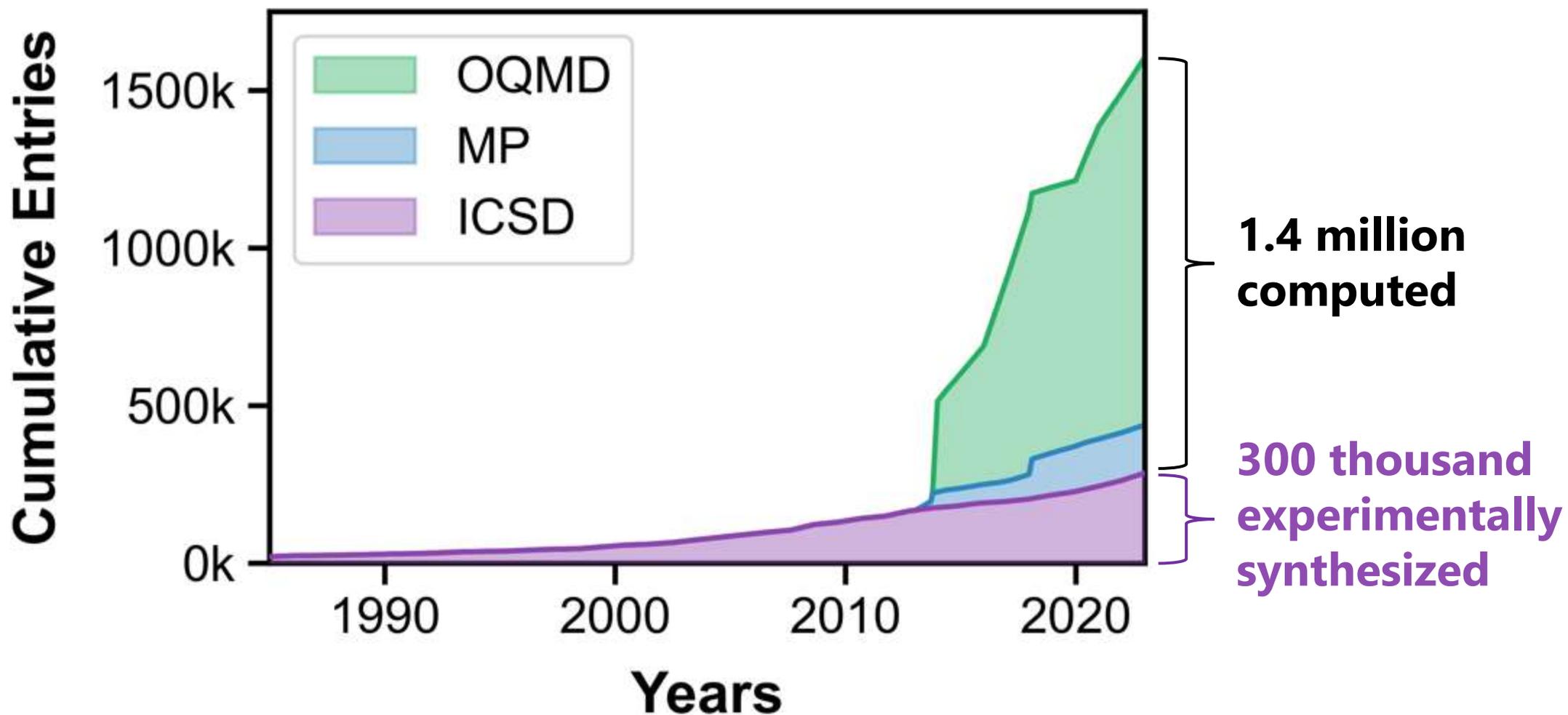
Is the material **stable**?
Does it have the properties we want?



There has been explosive growth in predicted materials

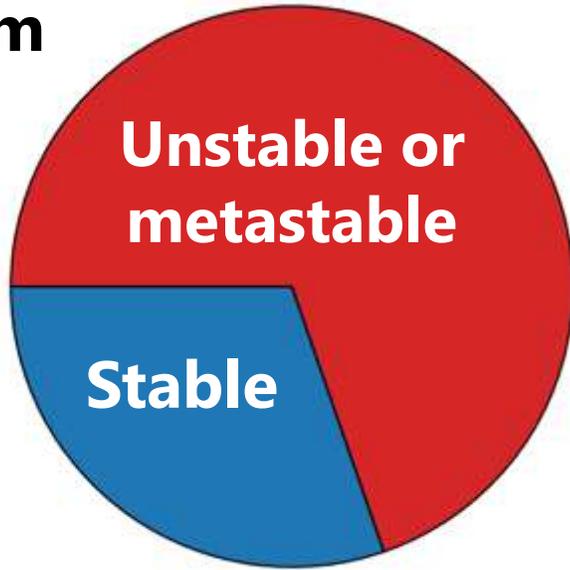


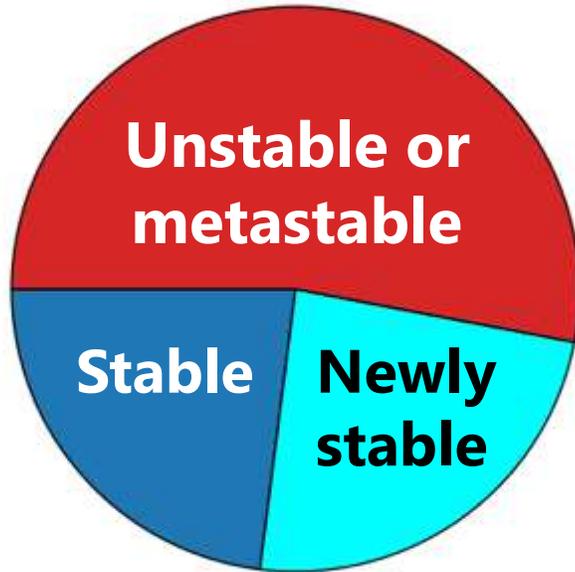
There has been explosive growth in predicted materials



Only some of these materials are thermodynamically stable

From
MP





SCIENCE ADVANCES | RESEARCH ARTICLE

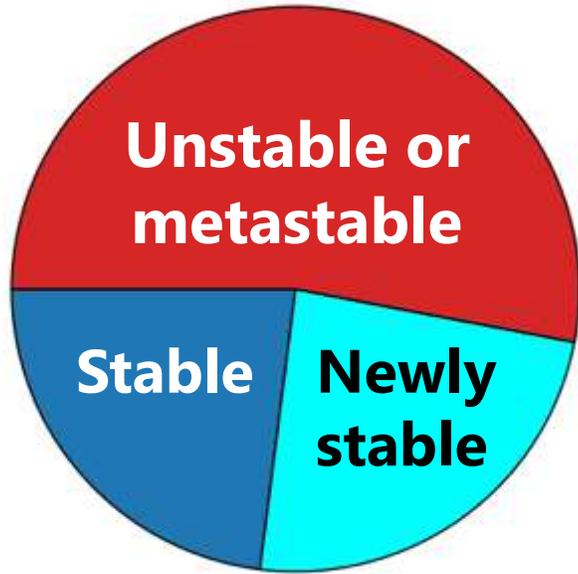
MATERIALS SCIENCE

Wide-ranging predictions of new stable compounds powered by recommendation engines

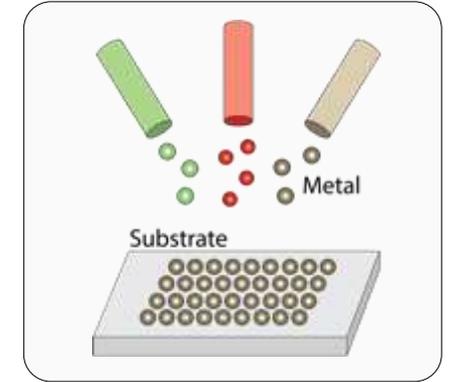
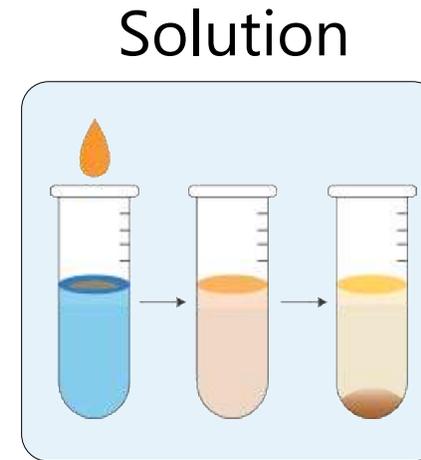
Sean D. Griesemer^{1,2}, Bianca Baldassarri¹, Ruijie Zhu¹, Jiahong Shen¹, Koushik Pal^{1,3}, Cheol Woo Park^{1,4}, Chris Wolverton^{1*}

+60k predictions of stable materials!

Synthesizing predicted materials remains challenging



Solid-state

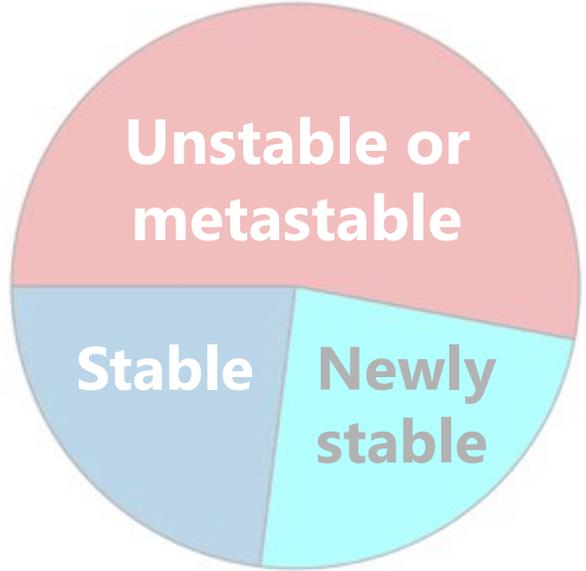


Thin film

So how do we synthesize these compounds?



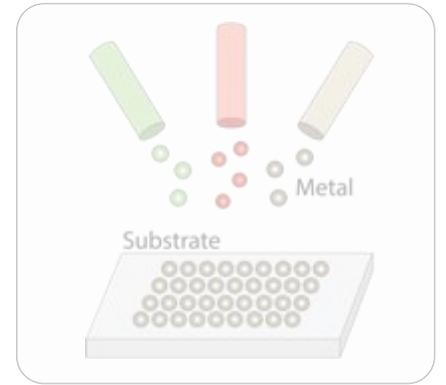
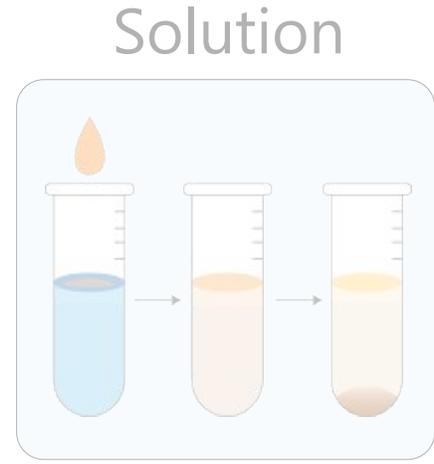
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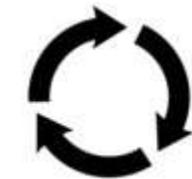
?



Solid-state



Thin film



Trial and error

What **precursors** and **conditions** to use? —————>



The wrong answer may lead to:

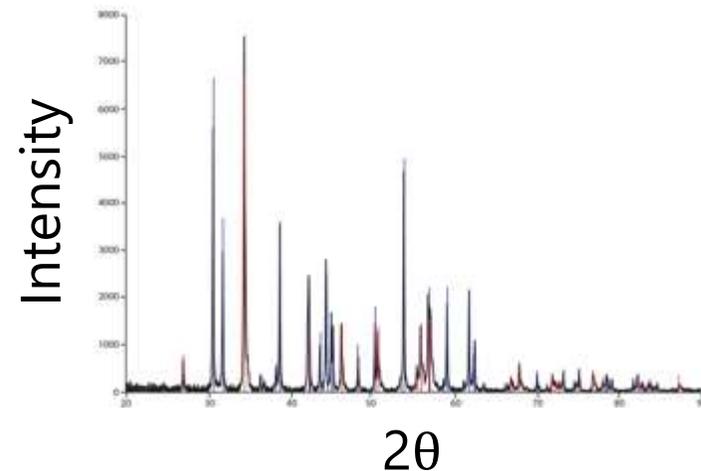
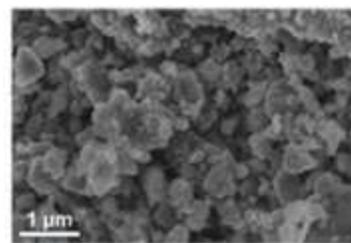
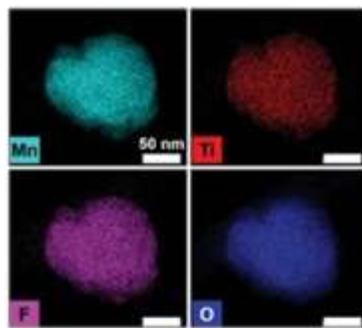
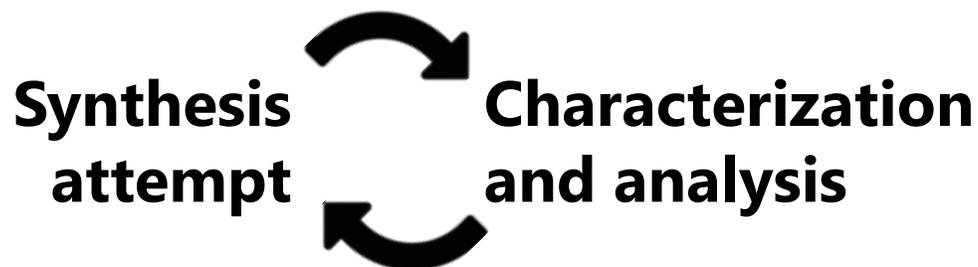
No target formed Impurities

Loss of necessary elements



Characterization is a long and expertise-driven process

The “**cook-and-look**” process



Trial and error

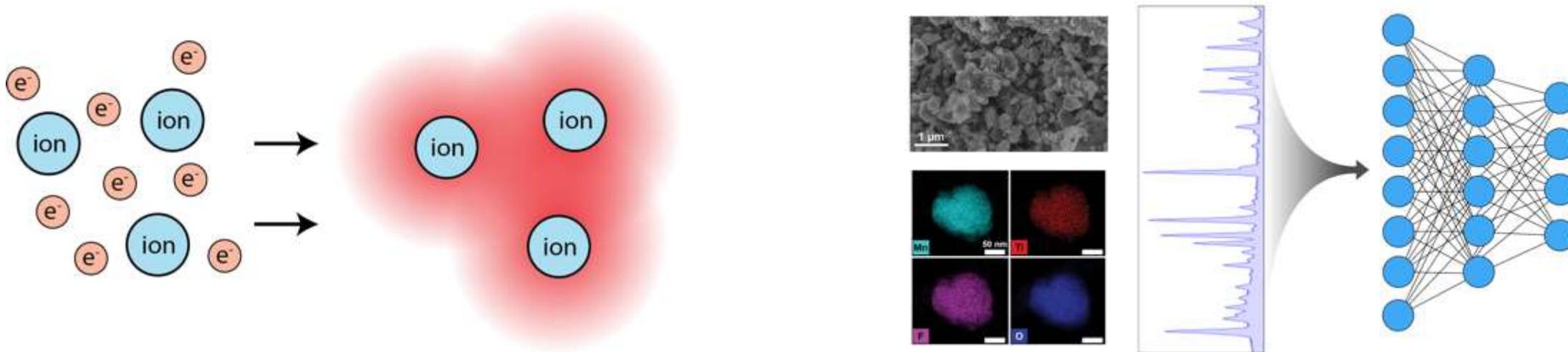
What **precursors** and **conditions** to use? →



The wrong answer may lead to:

- No target formed**
- Impurities**
- Loss of necessary elements**

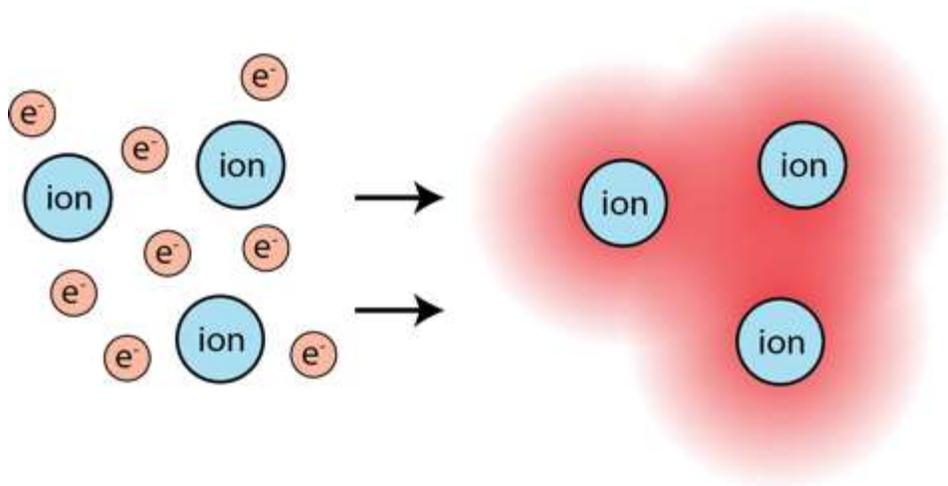




DFT for synthesis planning

AI for characterization

Integrate these two approaches
for **closed-loop** experimental optimization



DFT for synthesis planning

- 1) What can we learn from computed thermodynamics?**
- 2) Using what we've learned: how can we design synthesis procedures?

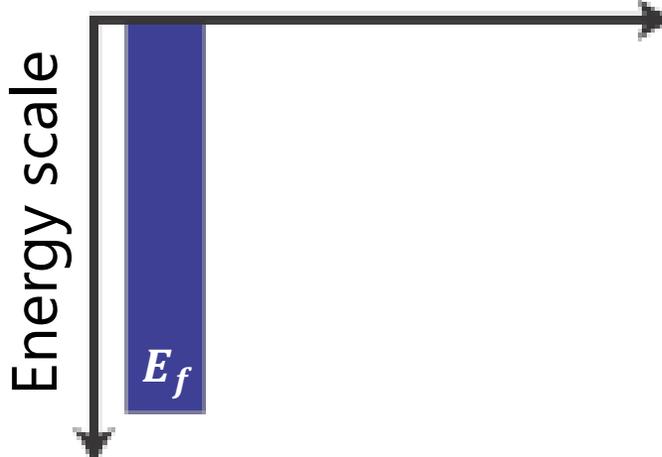
Ab-initio calculation of the Gibbs free energy (G)

$$G(T, P) = E + PV - TS$$



Ab-initio calculation of the Gibbs free energy (G)

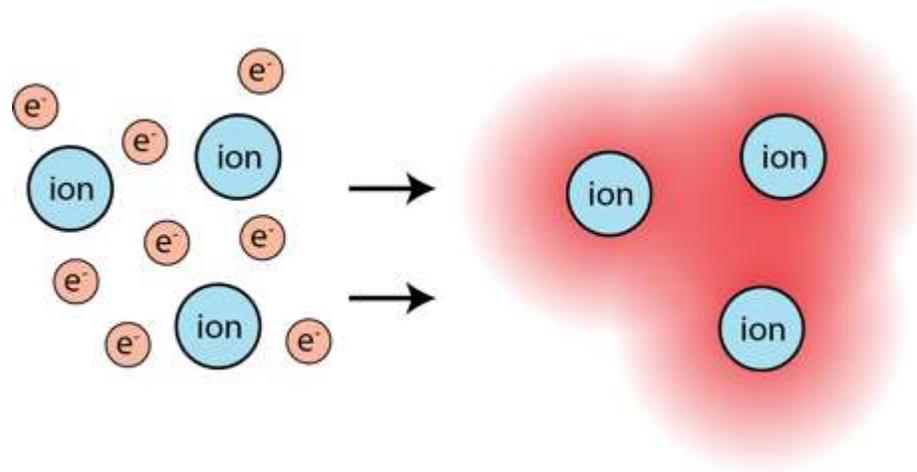
Energy scale



$$G(T, P) = E + PV - TS$$

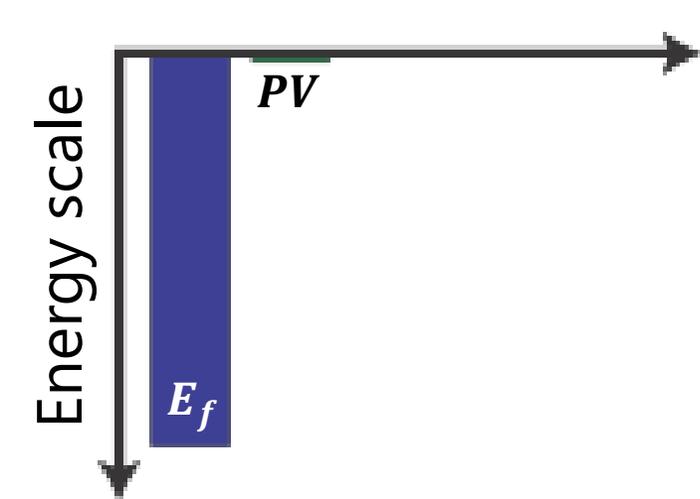
↓

Internal energy (E) from DFT



Scale of E_f is usually a few eV/atom

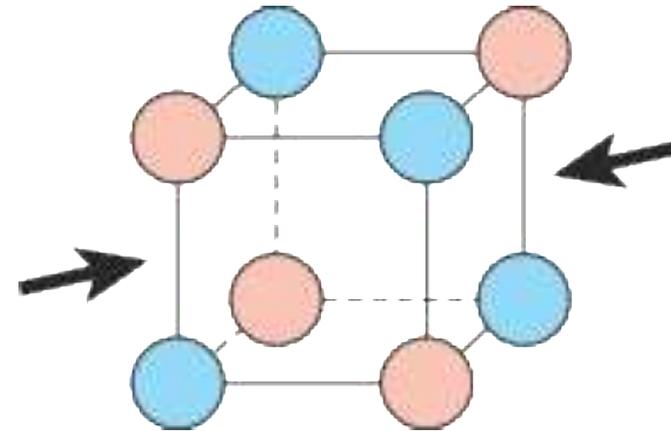
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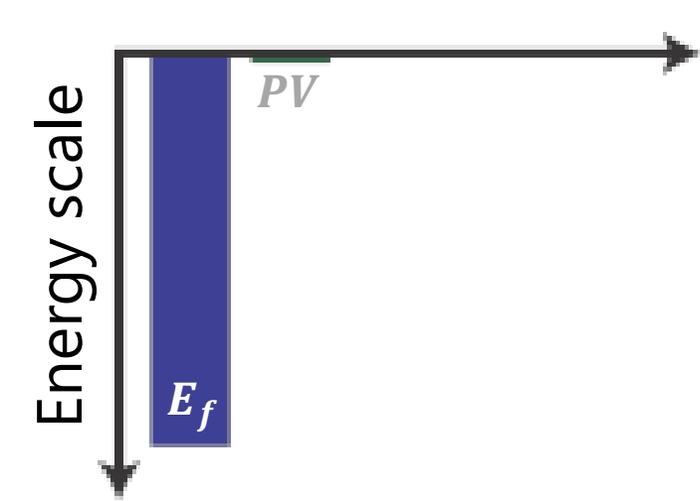
Work term associated with volume change

For most solids:
 $P\Delta V \leq 0.01 \text{ eV/atom}$



We can safely neglect this term under ambient pressure

Ab-initio calculation of the Gibbs free energy (G)

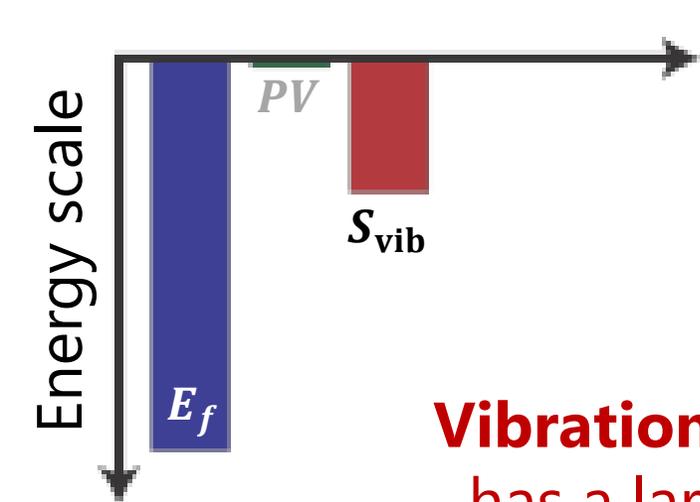


$$G(T, P) = E + PV - TS$$

↓

$$S_{\text{vib}} + S_{\text{elec}} + S_{\text{config}}$$

Ab-initio calculation of the Gibbs free energy (G)

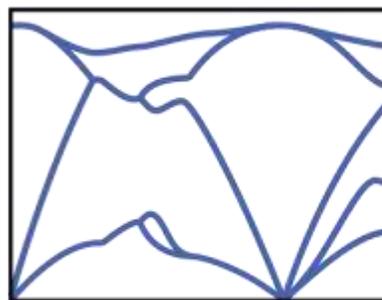


$$G(T, P) = E + PV - TS$$

↓

$$S_{\text{vib}} + S_{\text{elec}} + S_{\text{config}}$$

Vibrational entropy
has a large effect at
high temperature
(> 0.1 eV/atom)



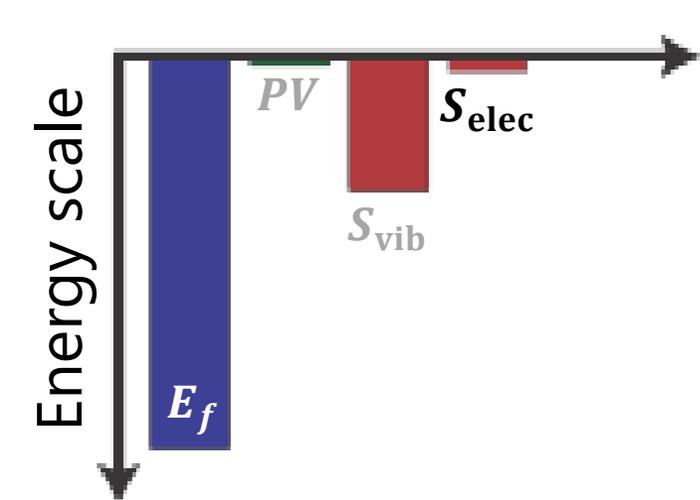
Phonons
or ML*

*Schwalbe-Koda *et al.*, arXiv (2024).

*Bartel *et al.*, Nature Communications (2018).



Ab-initio calculation of the Gibbs free energy (G)

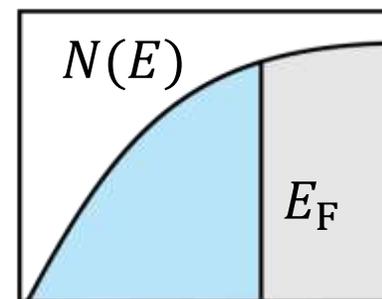


$$G(T, P) = E + PV - TS$$

↓

$$S_{vib} + S_{elec} + S_{config}$$

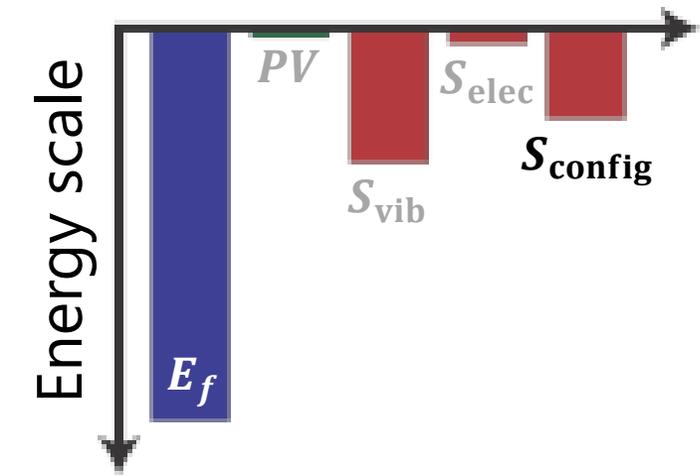
Electronic entropy
has a small effect on
most solids
(~ 0.01 eV/atom)



**Density
of states**



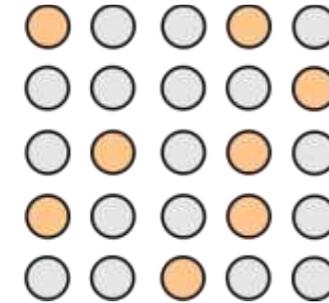
Ab-initio calculation of the Gibbs free energy (G)



$$G(T, P) = E + PV - TS$$

$$S_{\text{vib}} + S_{\text{elec}} + S_{\text{config}}$$

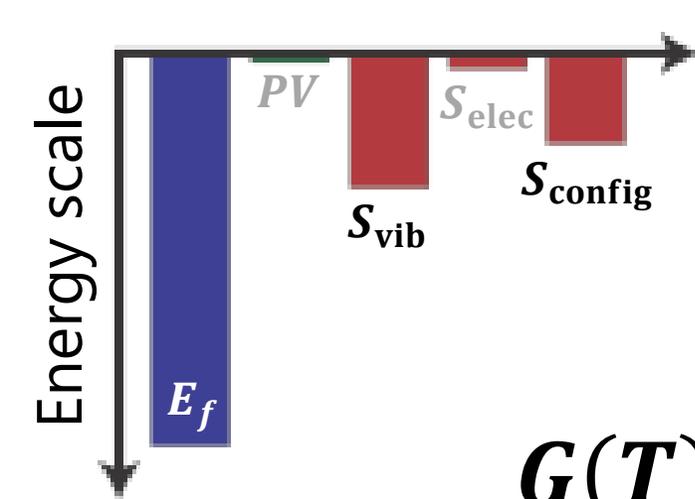
Configurational entropy
has a large effect on
disordered materials
(~0.1 eV/atom)



$$S = -Nk_B \sum_i x_i \ln x_i$$

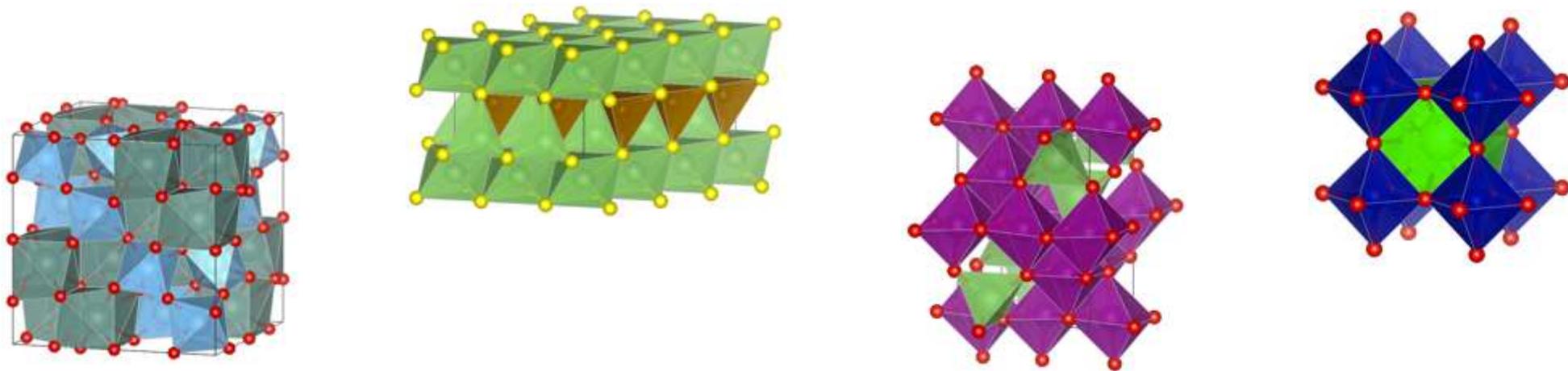
Statistical thermo.

Ab-initio calculation of the Gibbs free energy (G)

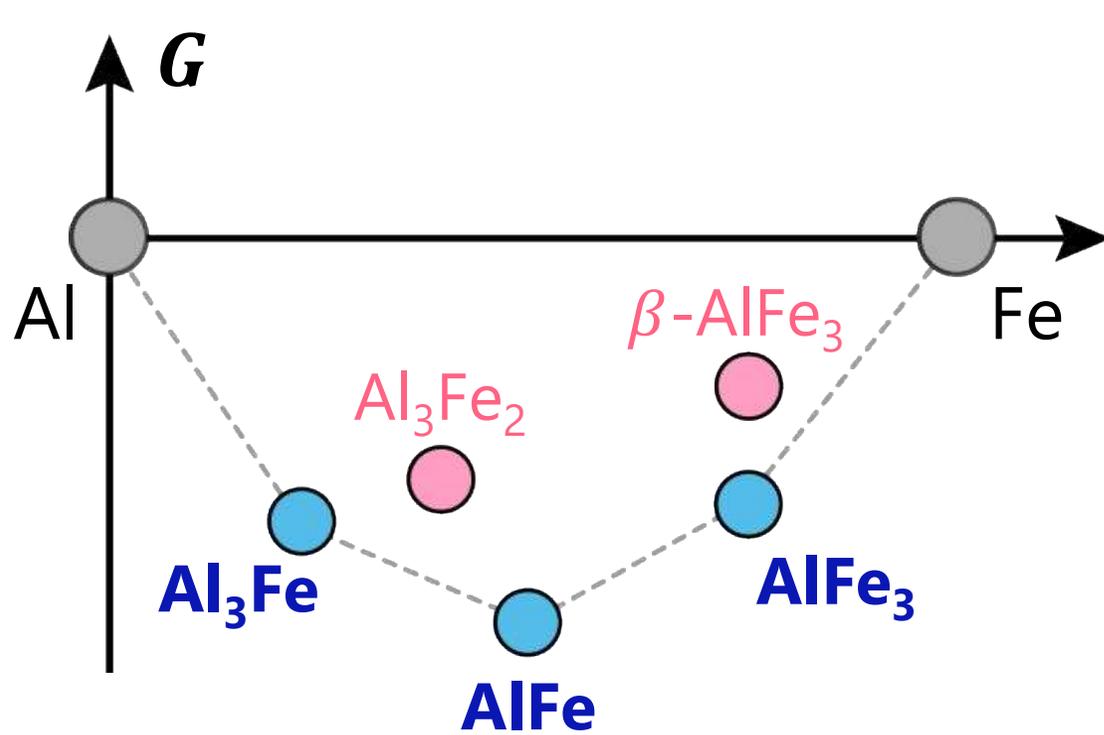


$$G(T, P) = E + PV - TS$$

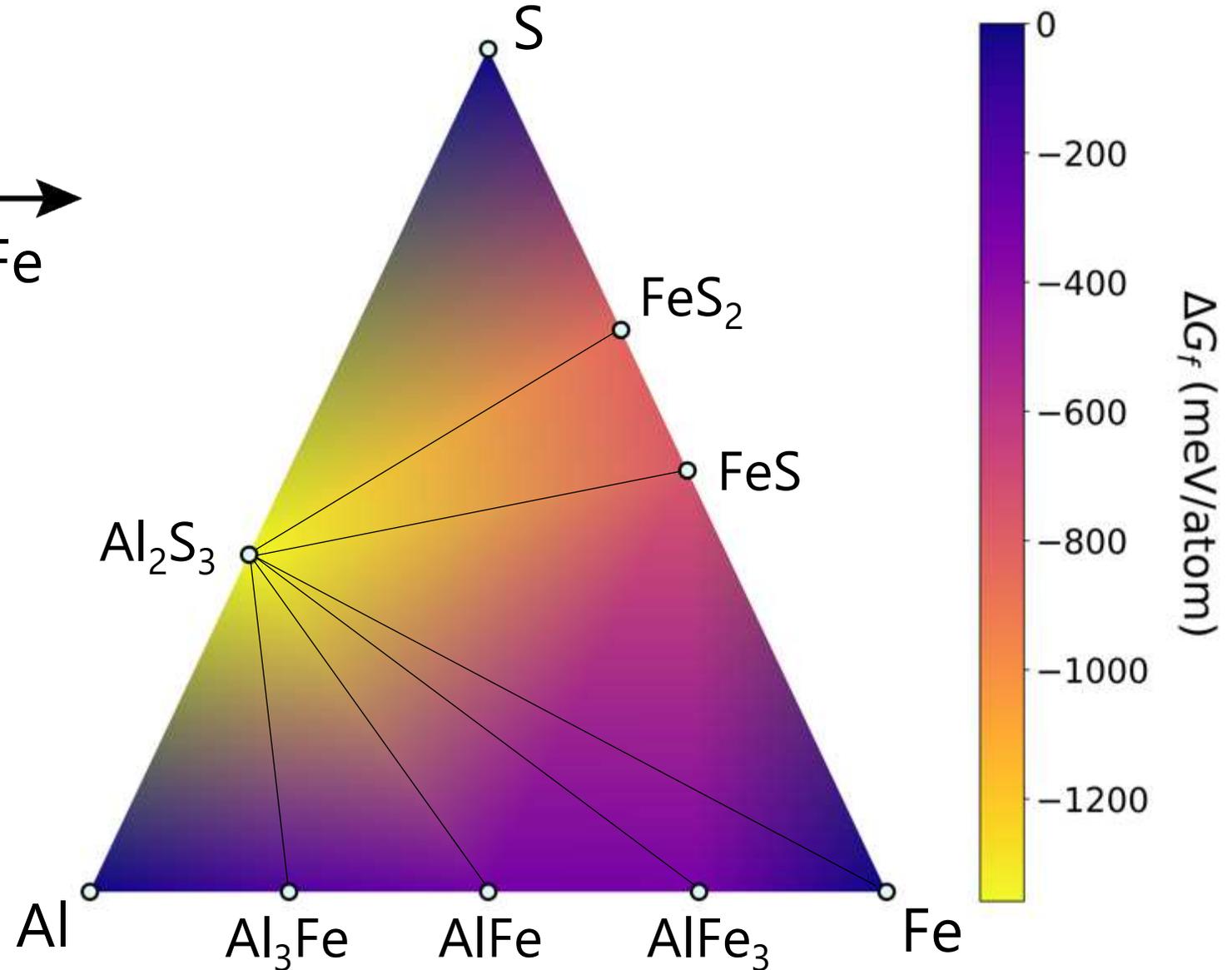
$$G(T) = E - TS_{vib} + Nk_B T \sum_i x_i \ln x_i$$



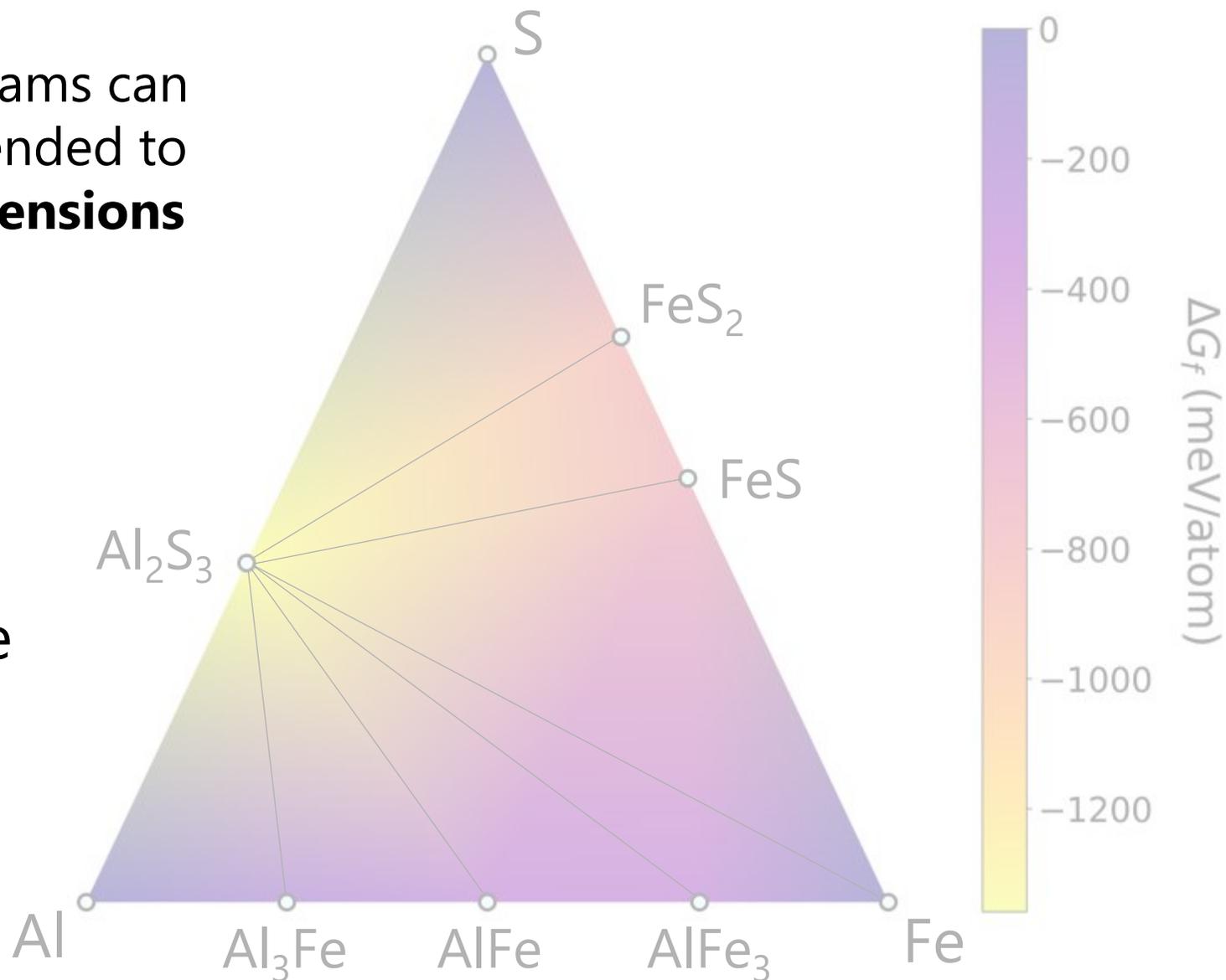
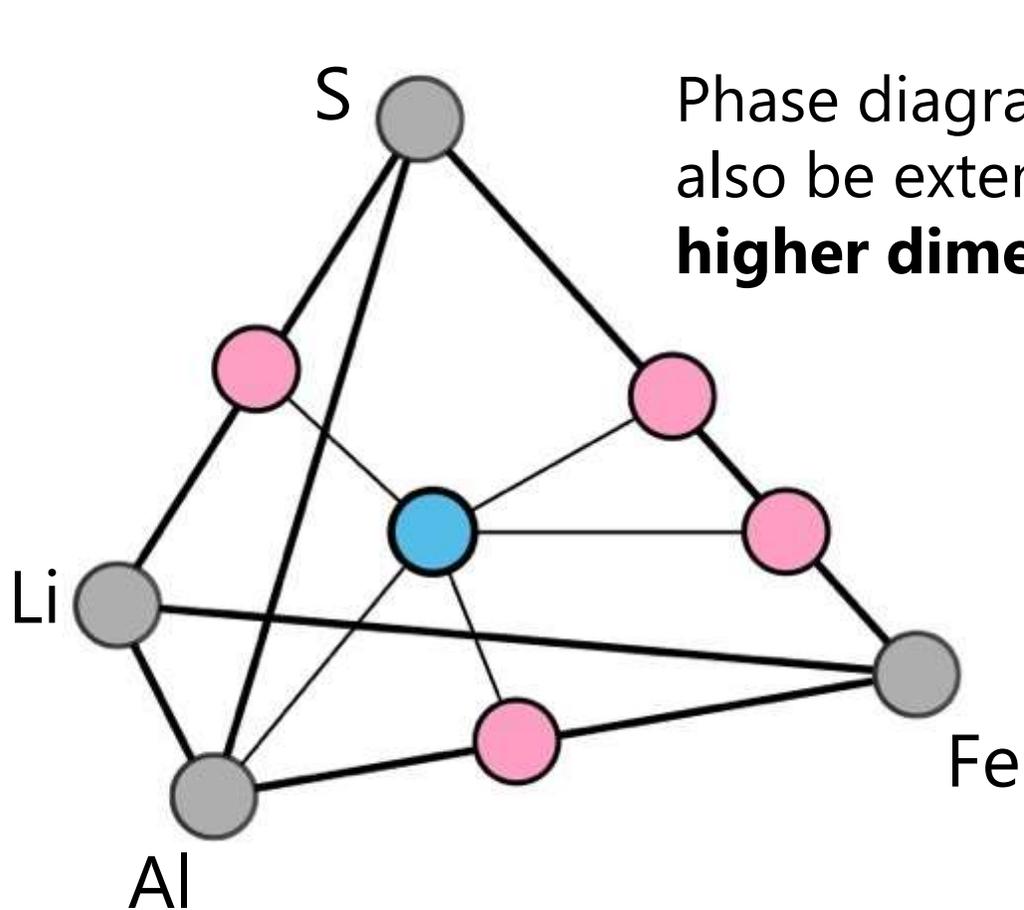
Using $G(T)$ to make computational phase diagrams



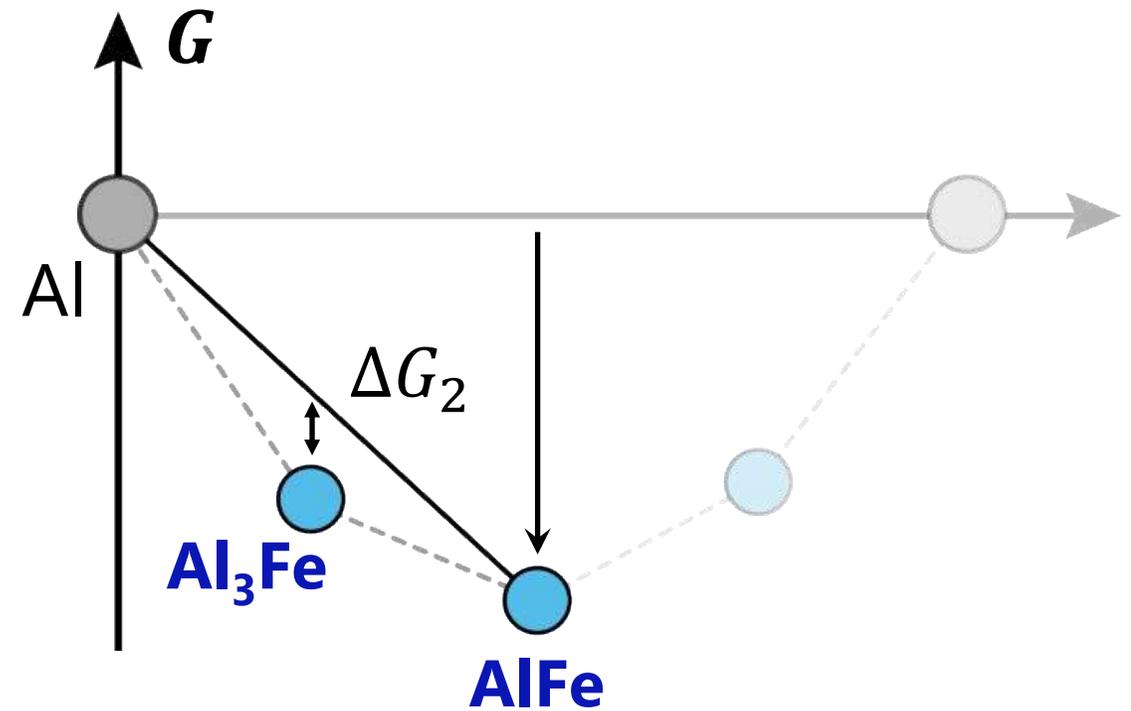
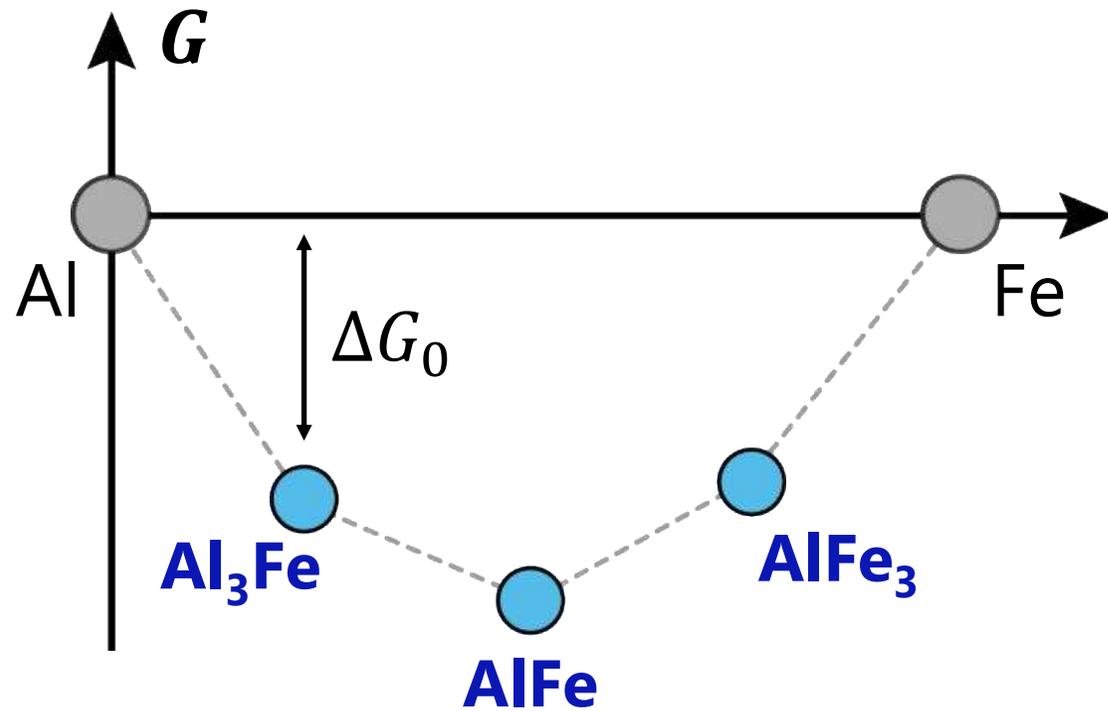
Ground states = lowest G
at a given composition



Using $G(T)$ to make computational phase diagrams



Computed phase diagrams don't always tell the whole story

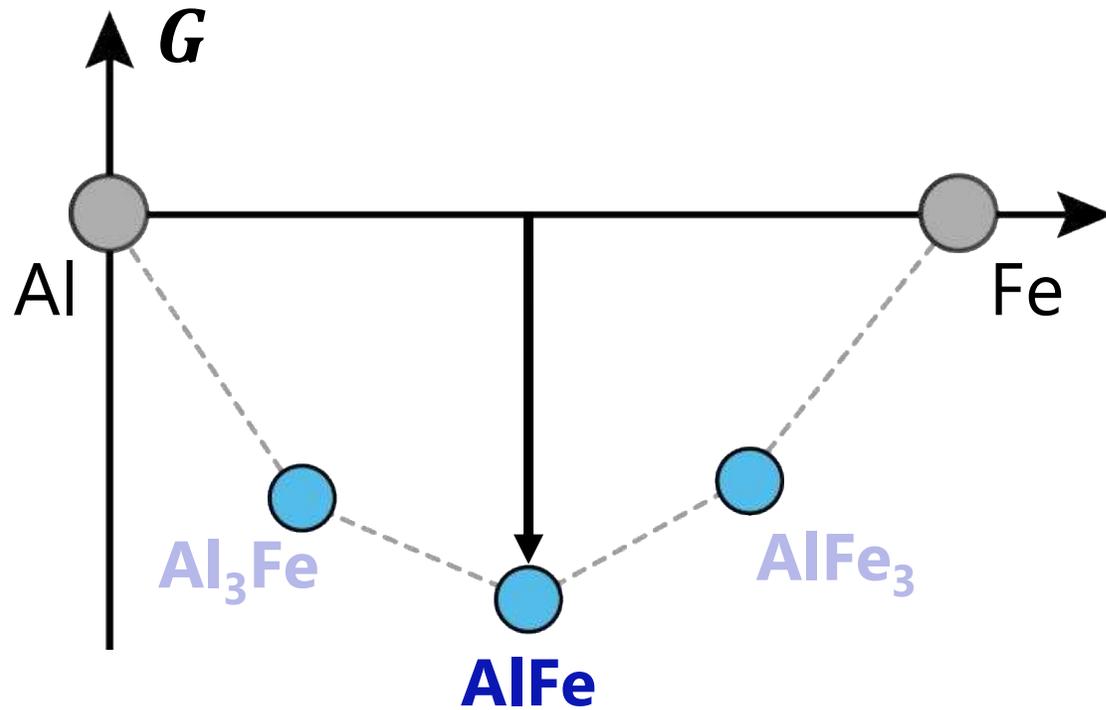


Desired reaction: $3 \text{Al} + \text{Fe} \rightarrow \text{Al}_3\text{Fe}$ ($\Delta G_0 = -199 \text{ meV/atom}$)

Actual reactions: $\text{Al} + \text{Fe} \rightarrow \text{AlFe}$ ($\Delta G_1 = -327 \text{ meV/atom}$)

$\text{AlFe} + 2 \text{Al} \rightarrow \text{Al}_3\text{Fe}$ ($\Delta G_2 = -83 \text{ meV/atom}$)

Computed phase diagrams don't always tell the whole story



**Can we predict
this initial reaction
from the phase
diagram alone?**

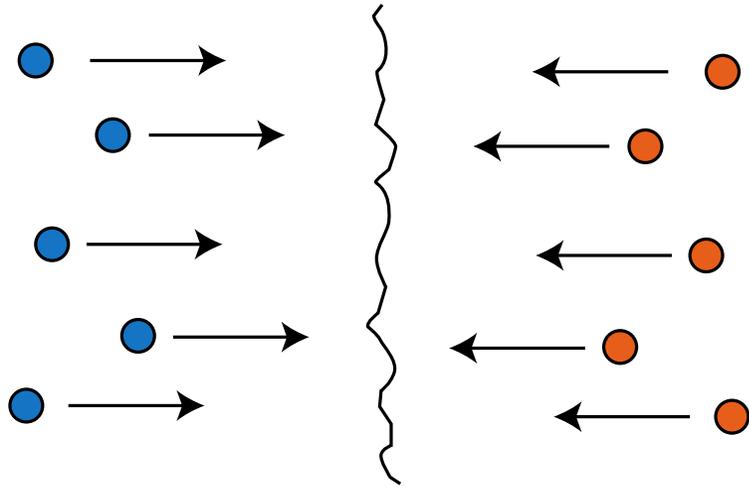
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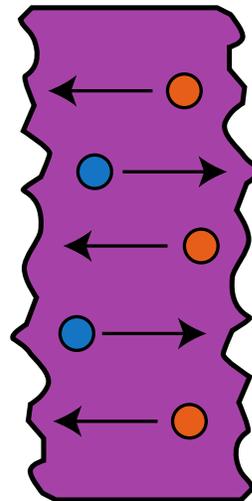
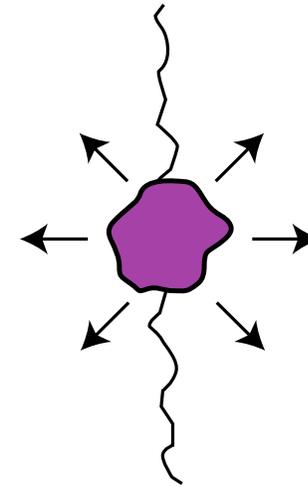
$\text{ AlFe} + 2 \text{ Al} \rightarrow \text{ Al}_3\text{ Fe}$ ($\Delta G_2 = -83 \text{ meV/atom}$)

Reactions are inherently dictated by kinetics

Ions need to **diffuse** to the interface



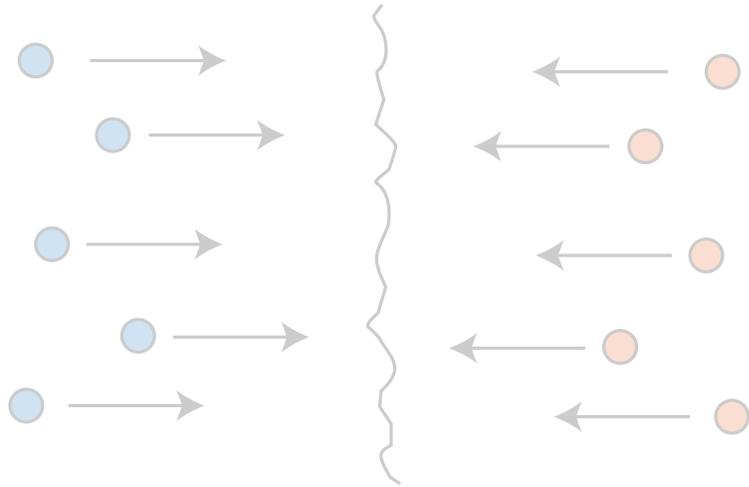
A product needs to **nucleate**



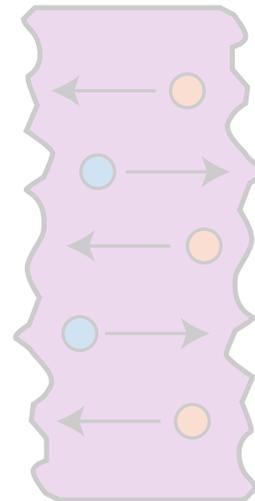
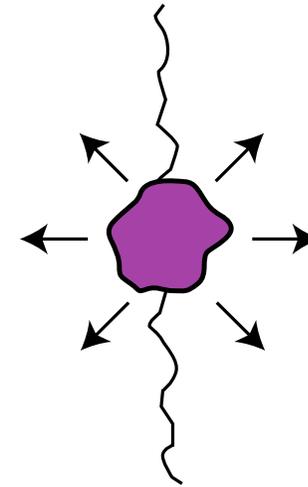
That product
 needs to grow
via interdiffusion

Reactions are inherently dictated by kinetics

Ions need to **diffuse** to the interface



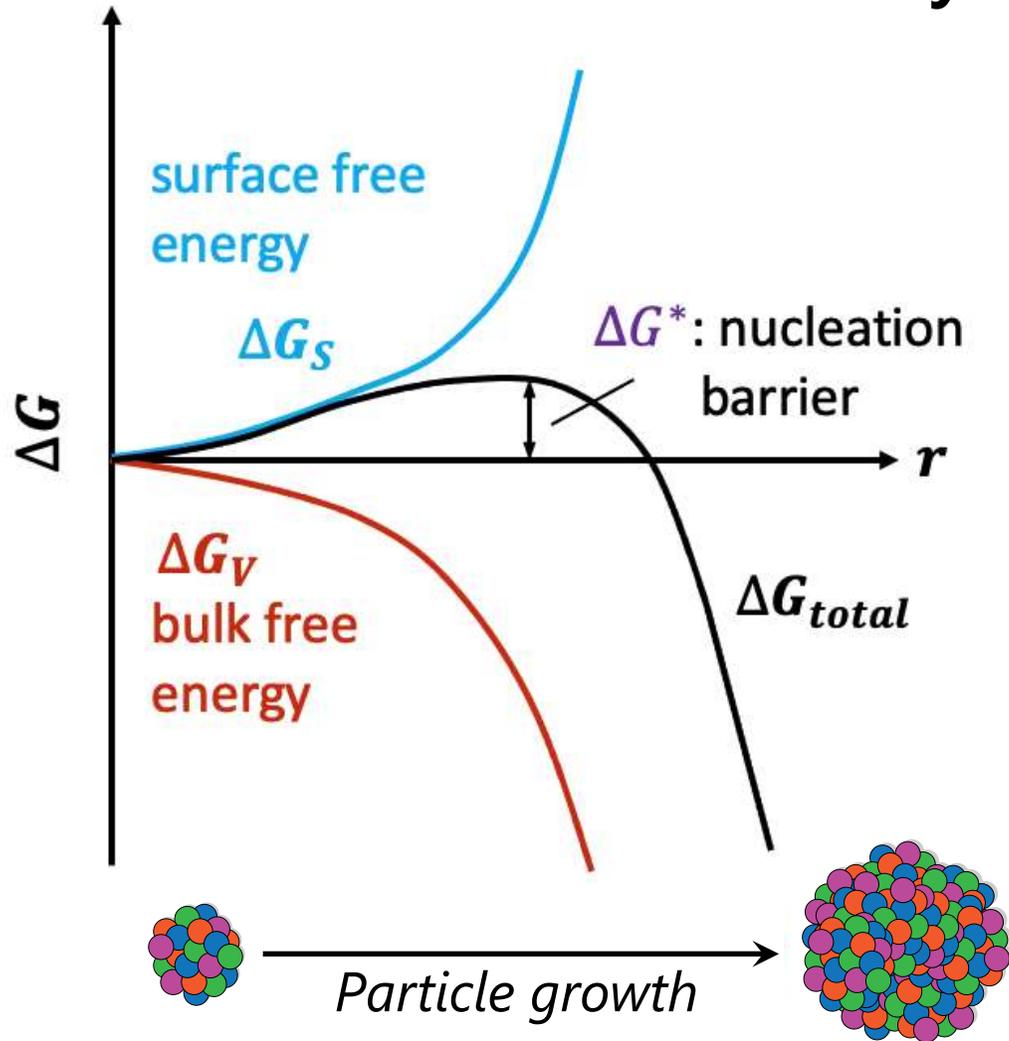
A product needs to **nucleate**



That product
 needs to grow
via interdiffusion

Nucleation primarily depends on ΔG and σ

Classical nucleation theory



Nucleation rate:

$$Q = A \exp\left(-\frac{\Delta G^*}{k_B T}\right)$$

Nucleation barrier:

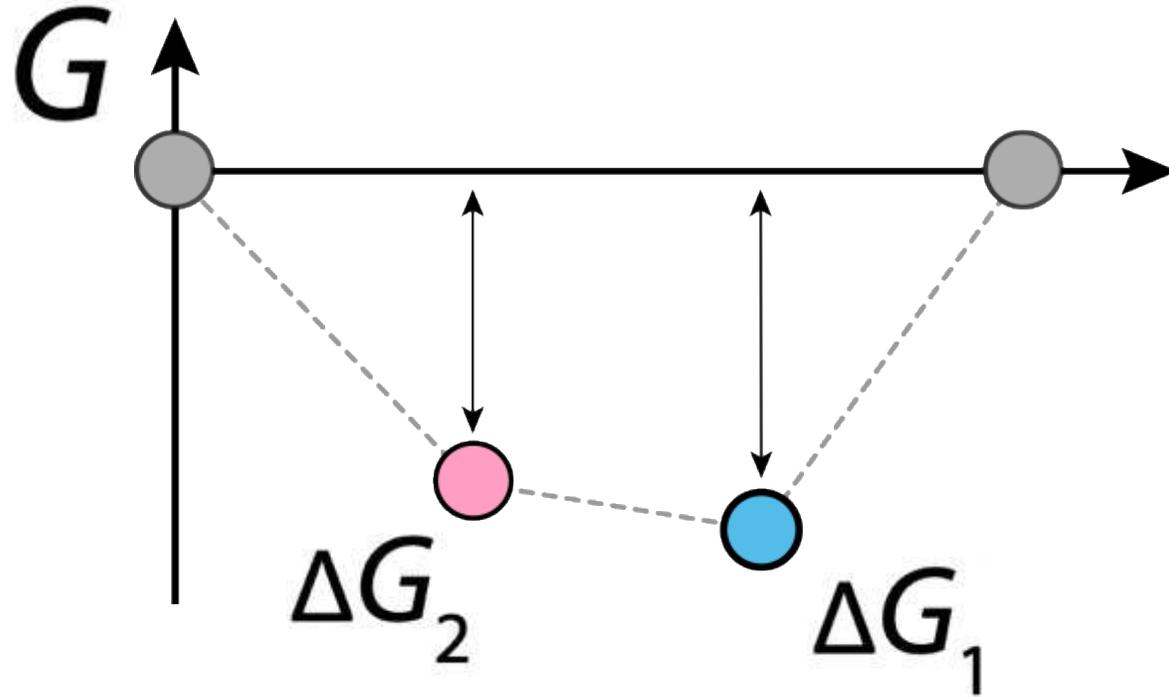
$$\Delta G^* = \frac{16\pi\sigma^3}{3(n\Delta G)^2}$$

Labels for the equation components:

- σ : Surface energy
- n : Atomic density
- ΔG : Bulk reaction energy



Can we use ΔG to predict which phase will nucleate first?

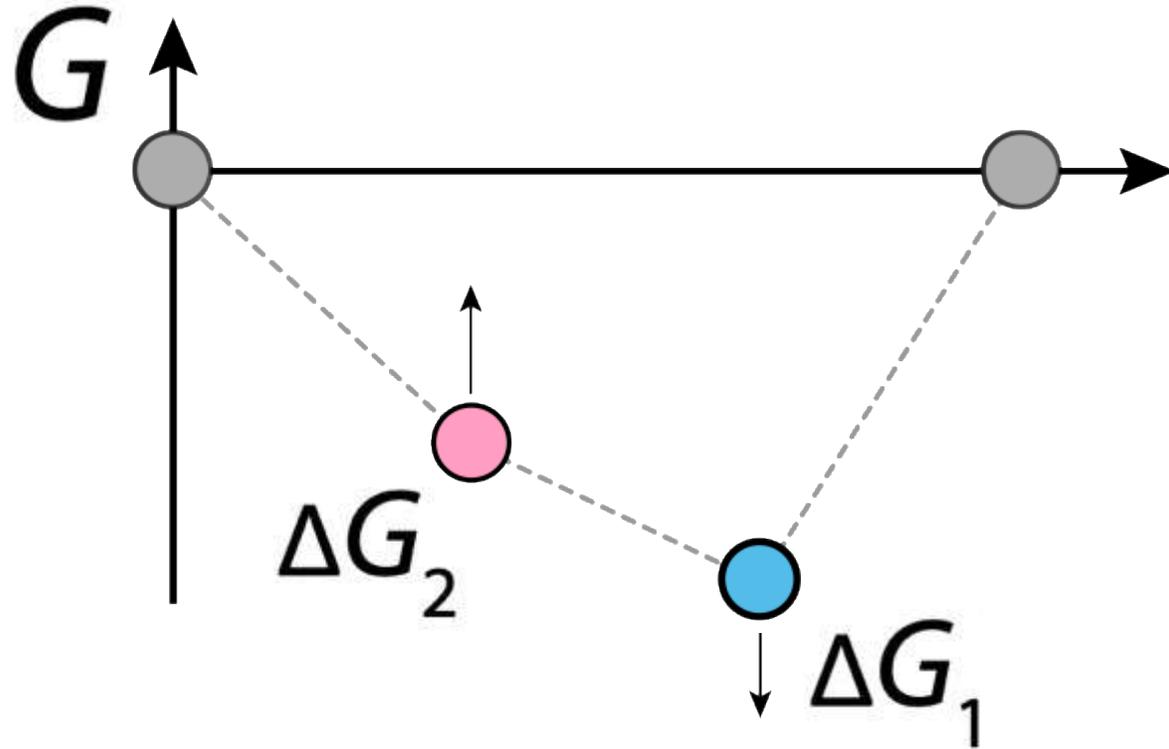


$$\ln(Q_1/Q_2) = \frac{16\pi}{3n^2 k_B T} \left(\frac{(\sigma_1)^3}{(\Delta G_1)^2} - \frac{(\sigma_2)^3}{(\Delta G_2)^2} \right)$$

Surface energy

Bulk reaction energy

Can we use ΔG to predict which phase will nucleate first?



Hypothesis:

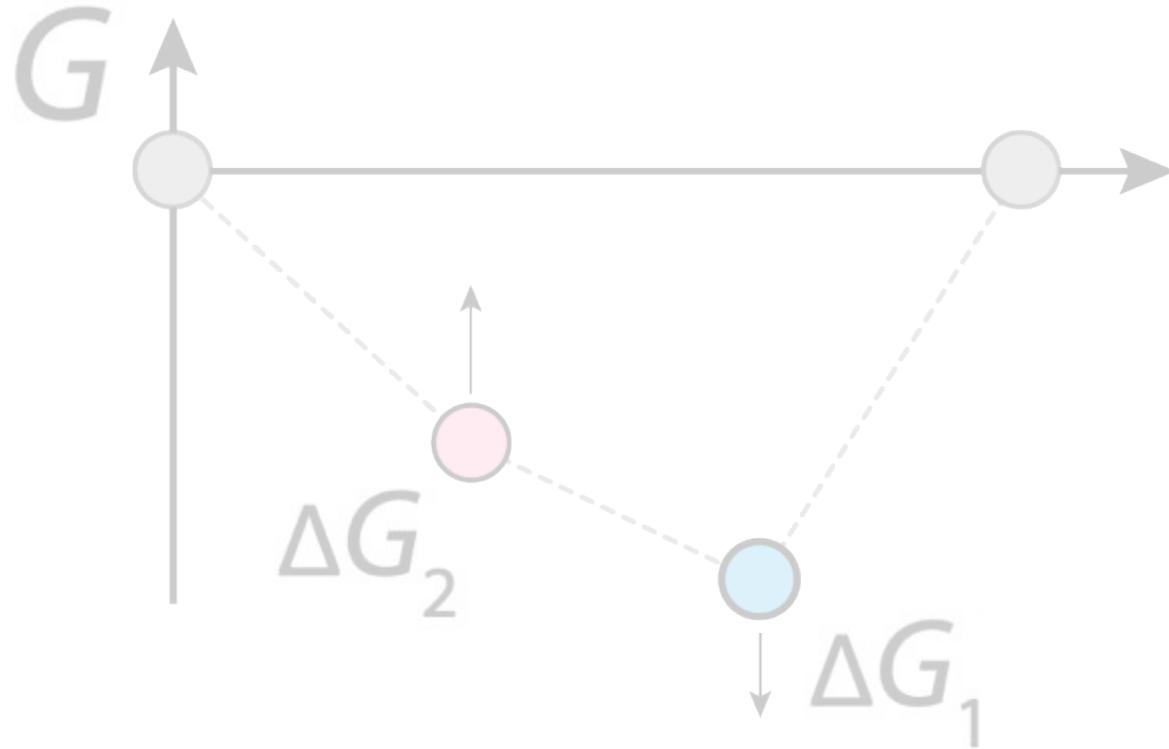
If the difference between ΔG_1 and ΔG_2 is sufficiently large, it outweighs any difference between σ_1 and σ_2

$$\ln(Q_1/Q_2) = \frac{16\pi}{3n^2 k_B T} \left(\frac{(\sigma_1)^3}{(\Delta G_1)^2} - \frac{(\sigma_2)^3}{(\Delta G_2)^2} \right)$$

Surface energy

Bulk reaction energy

Can we use ΔG to predict which phase will nucleate first?



**How large is
"sufficiently large"**

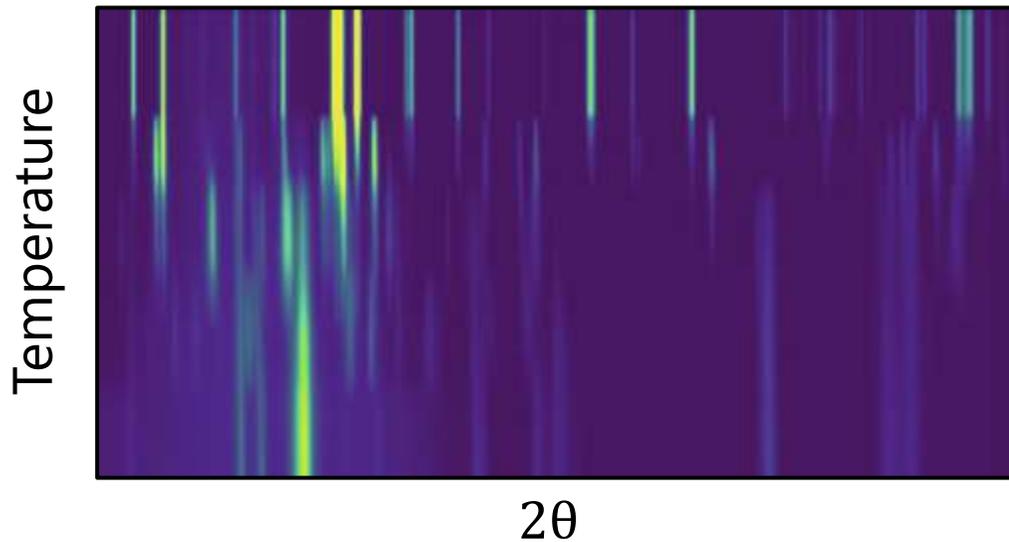
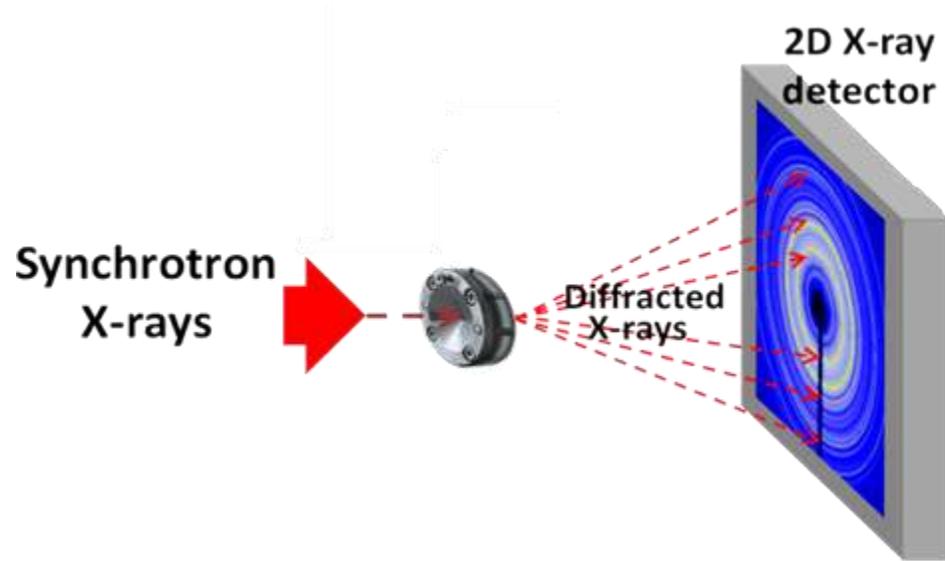
If the difference between ΔG_1 and ΔG_2 is **sufficiently large**, it outweighs any difference between σ_1 and σ_2

$$\ln(Q_1/Q_2) = \frac{16\pi}{3n^2 k_B T} \left(\frac{(\sigma_1)^3}{(\Delta G_1)^2} - \frac{(\sigma_2)^3}{(\Delta G_2)^2} \right)$$

Surface energy

Bulk reaction energy

Quantifying the limit using *in-situ* X-ray diffraction (XRD)



Given a pair of solid reactants, what is the **first product** that forms during heating?



Szymanski *et al.*, Science Advances (2024).

We used 37 ternary metal oxides (A-M-O) as a test case

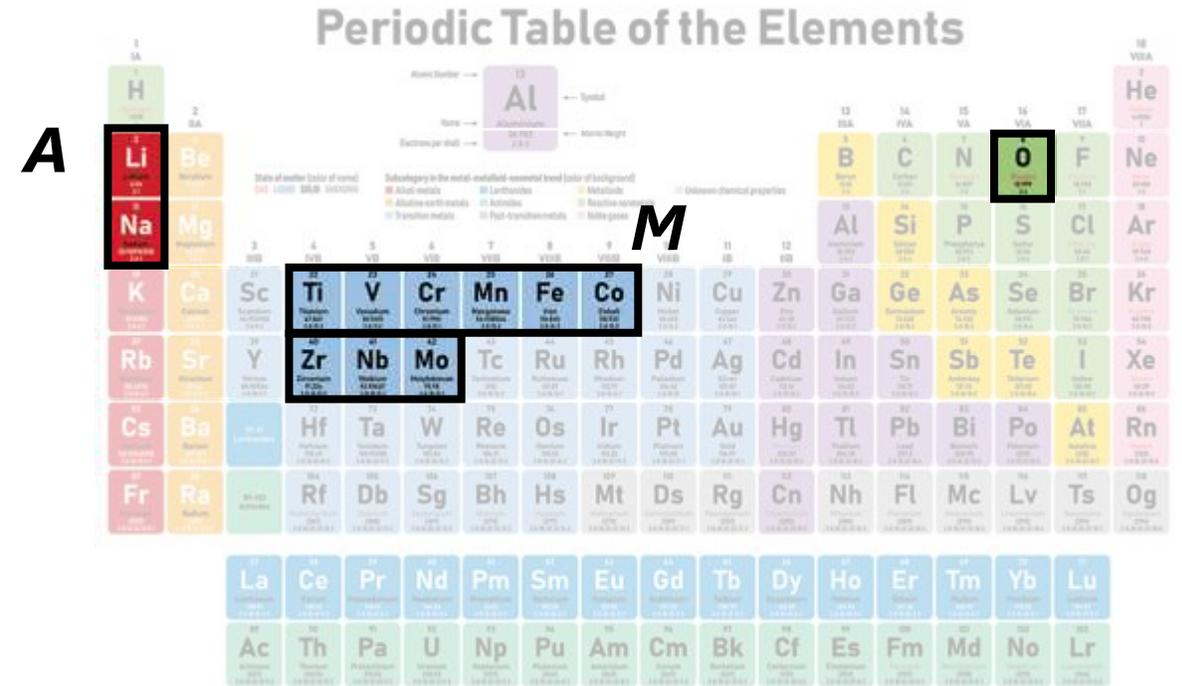
We took **alkali (A) precursors**:

Li_2CO_3 , LiOH , Li_2O , NaNO_3 , ...

Mixed them with **metal (M) precursors**:

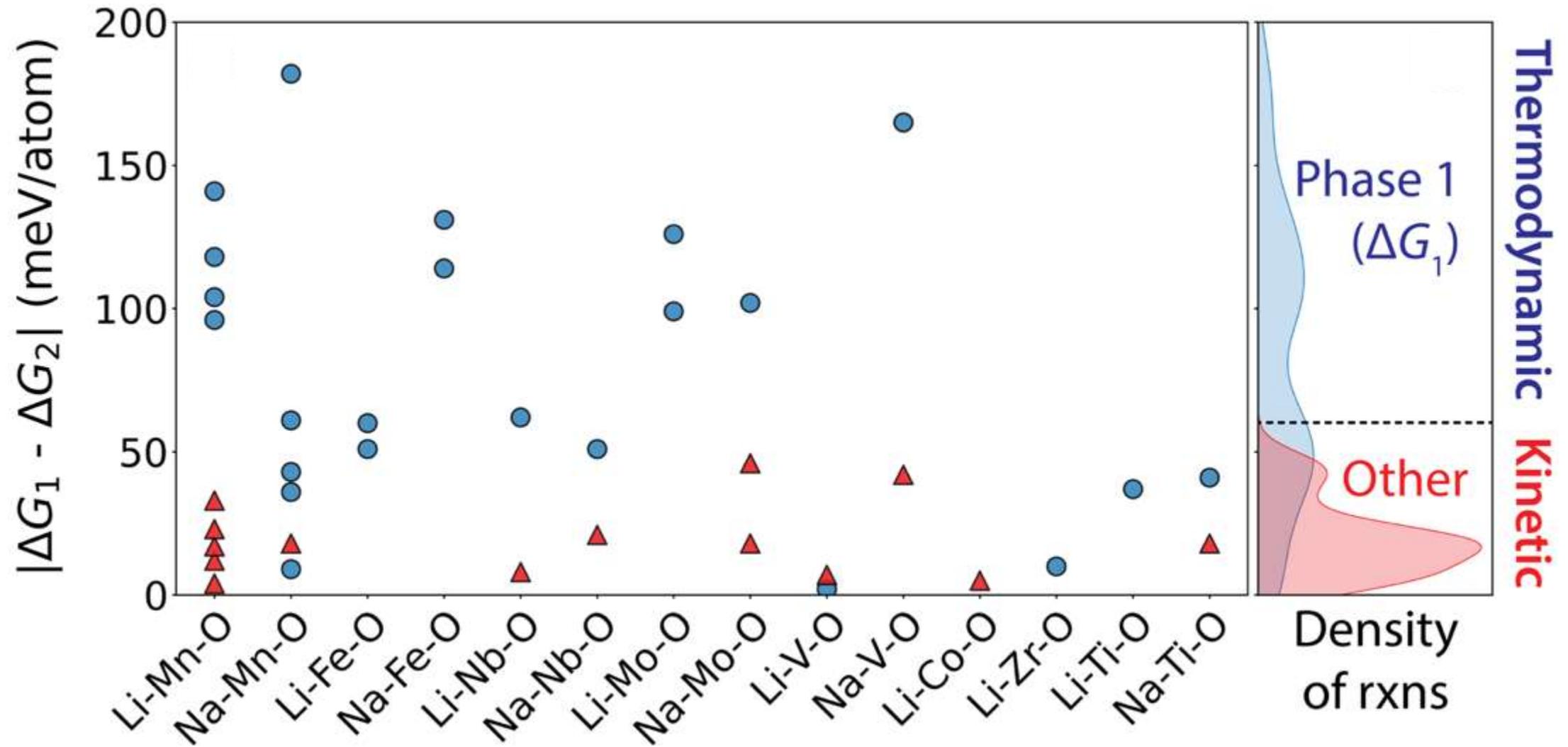
MnO , Mn_3O_4 , MnO_2 , Cr_2O_3 , ...

In a **1:1 ratio of A:M** for each sample, which was then **heated to 600 °C** while XRD scans were performed.



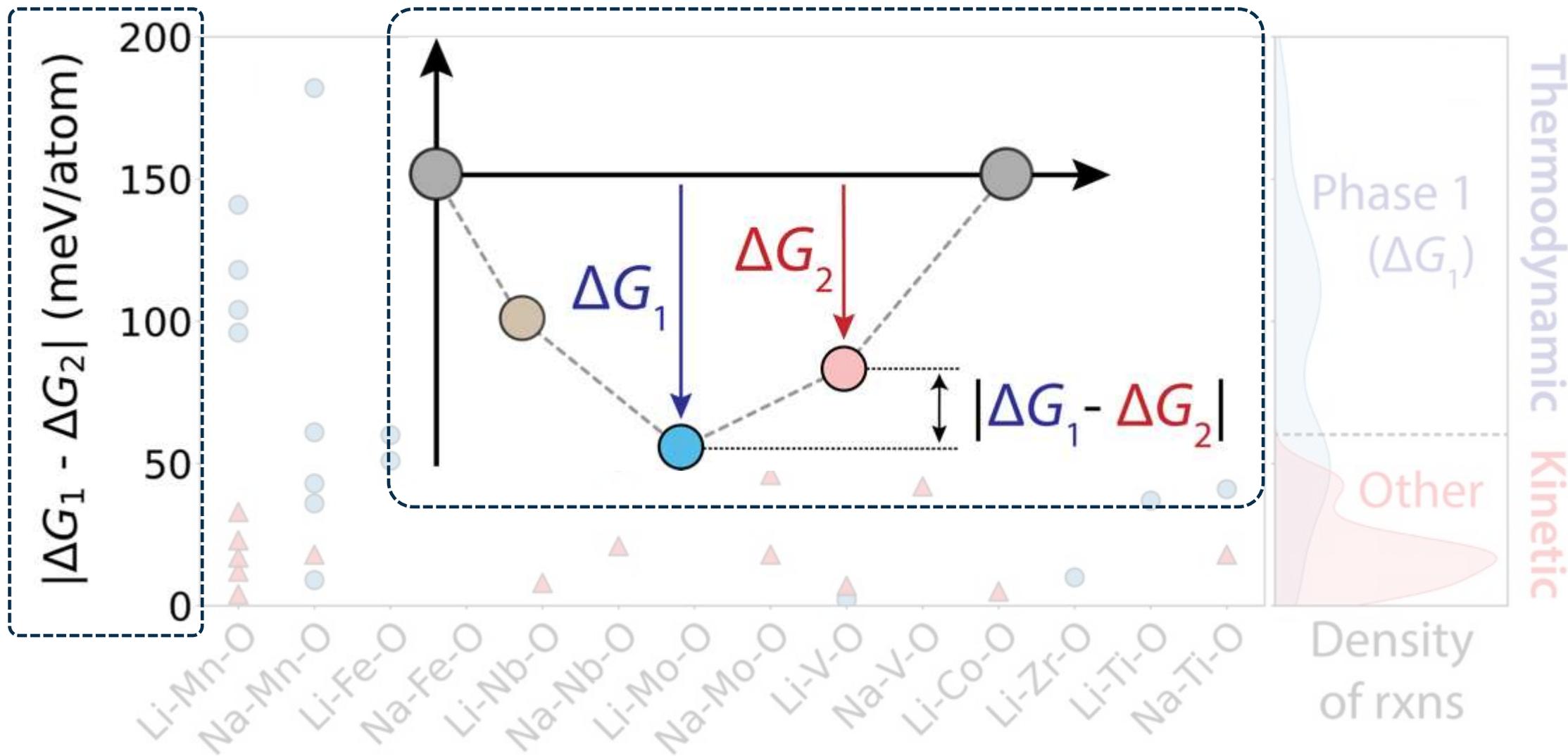
Szymanski *et al.*, Science Advances (2024).

Outcomes show a regime of thermodynamic (ΔG) control



Szymanski *et al.*, Science Advances (2024).

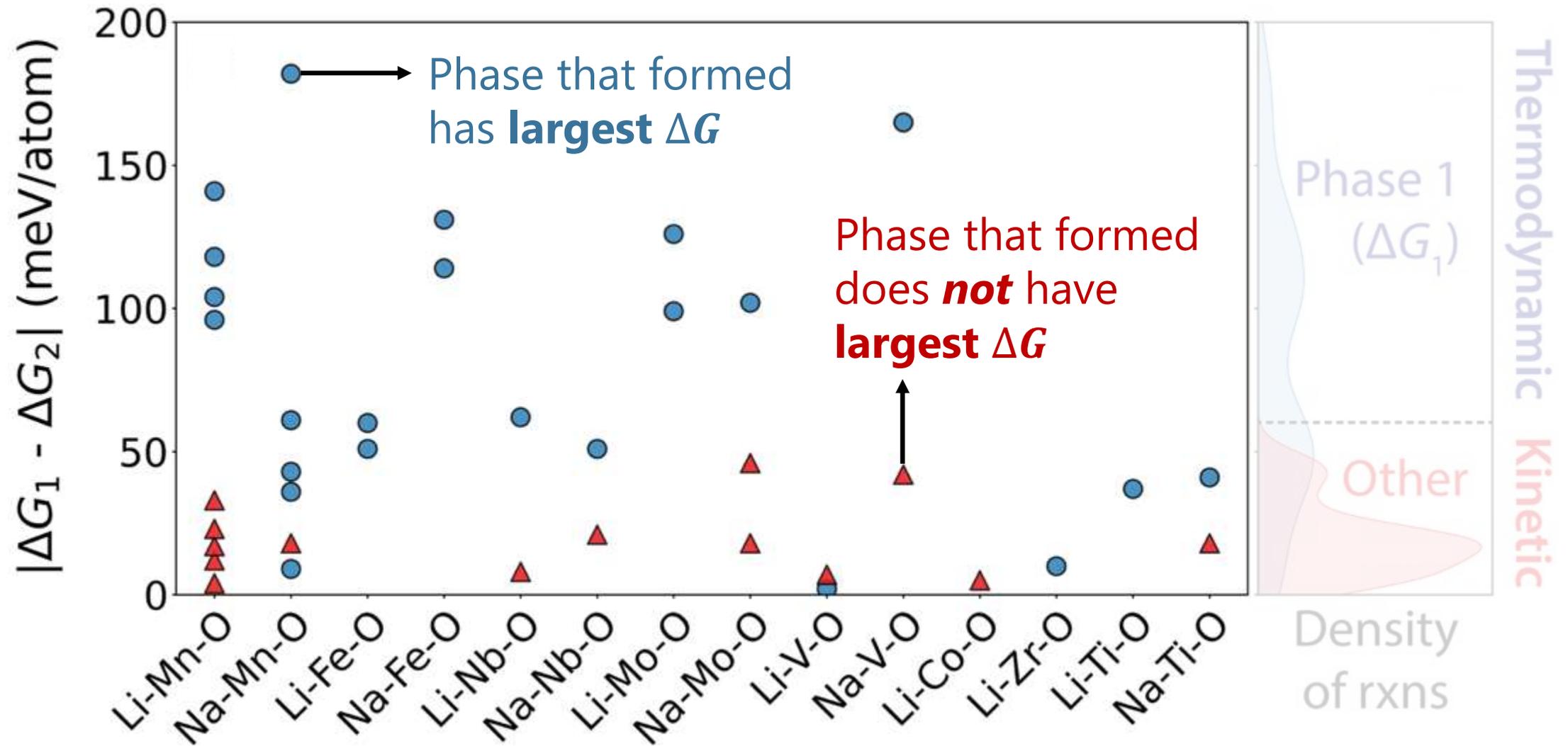
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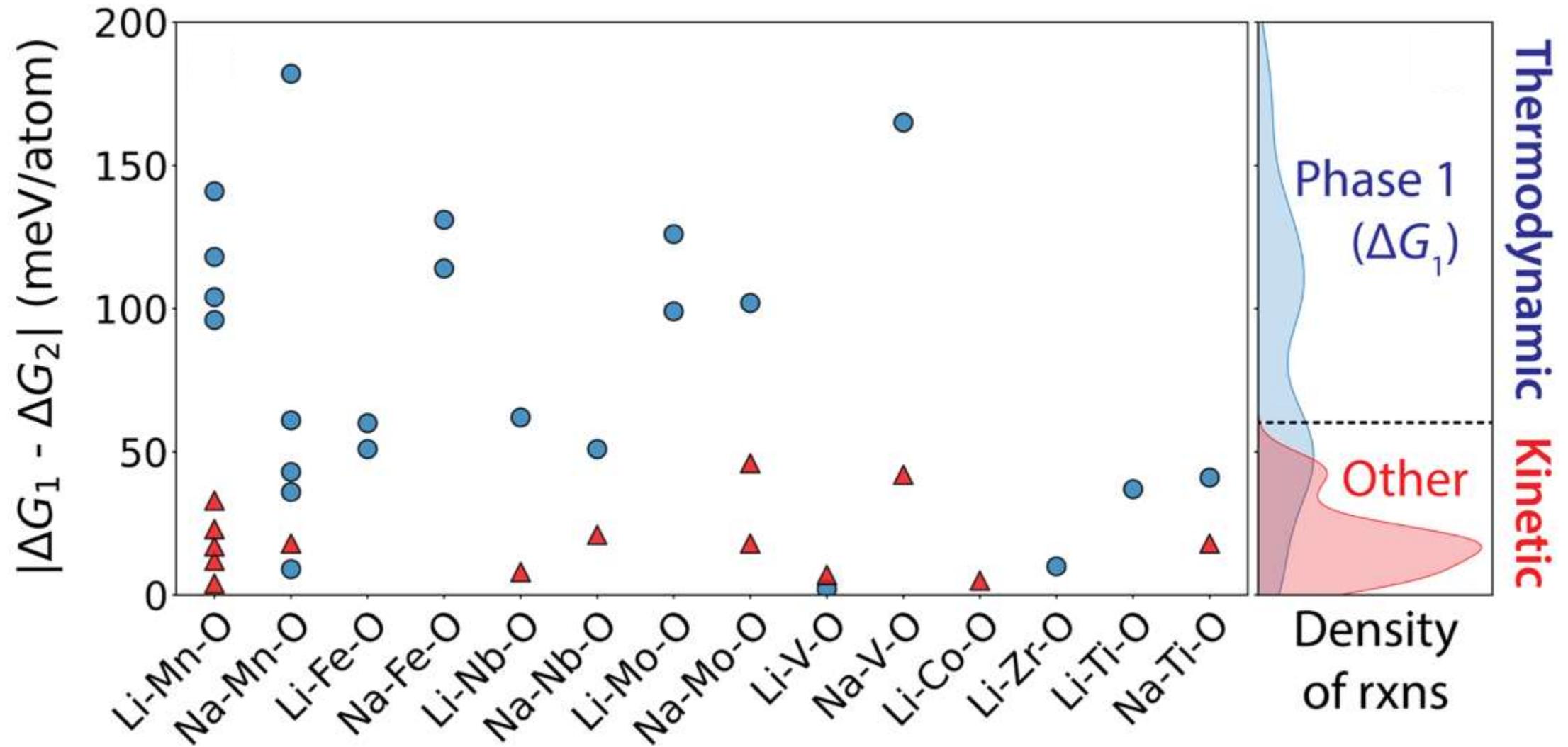
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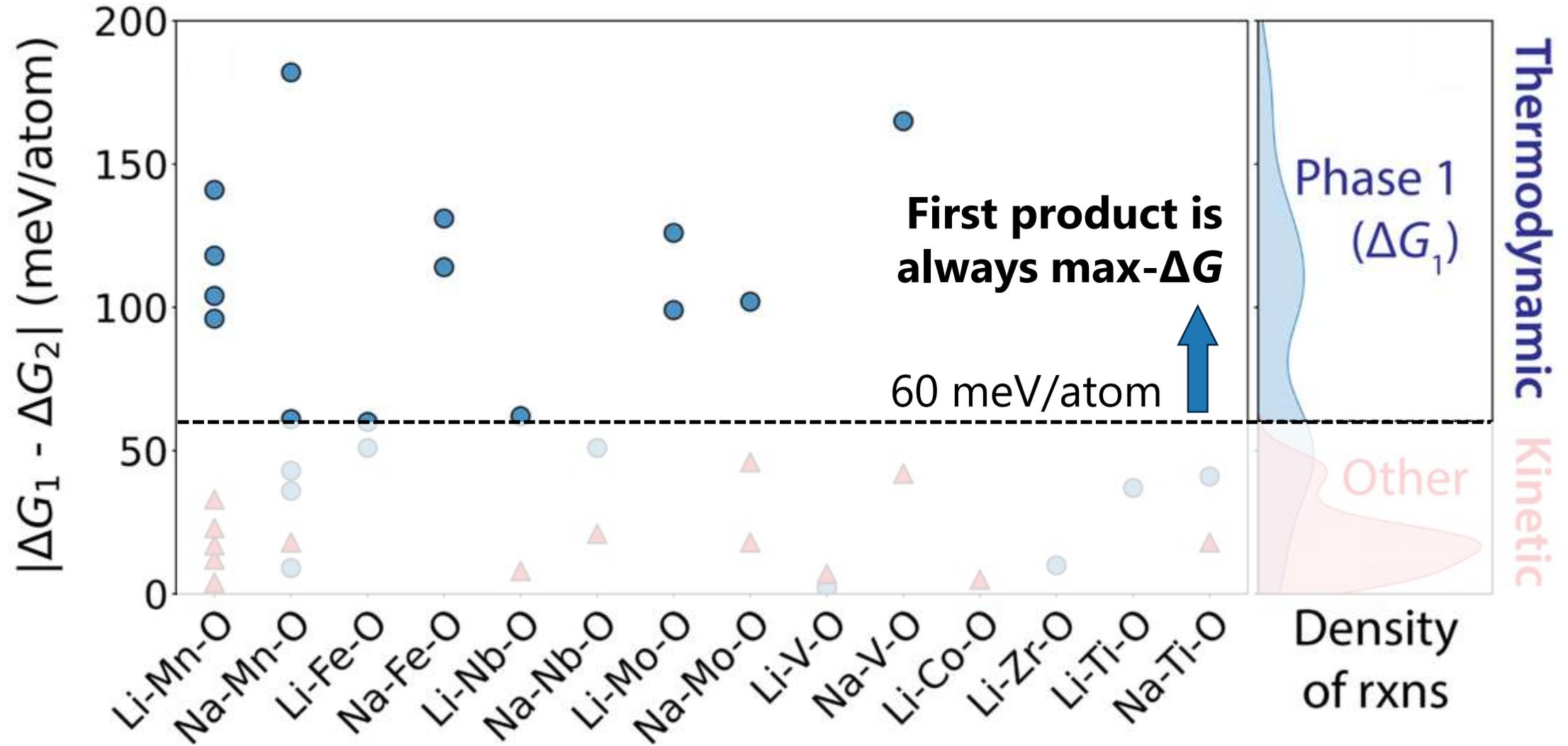


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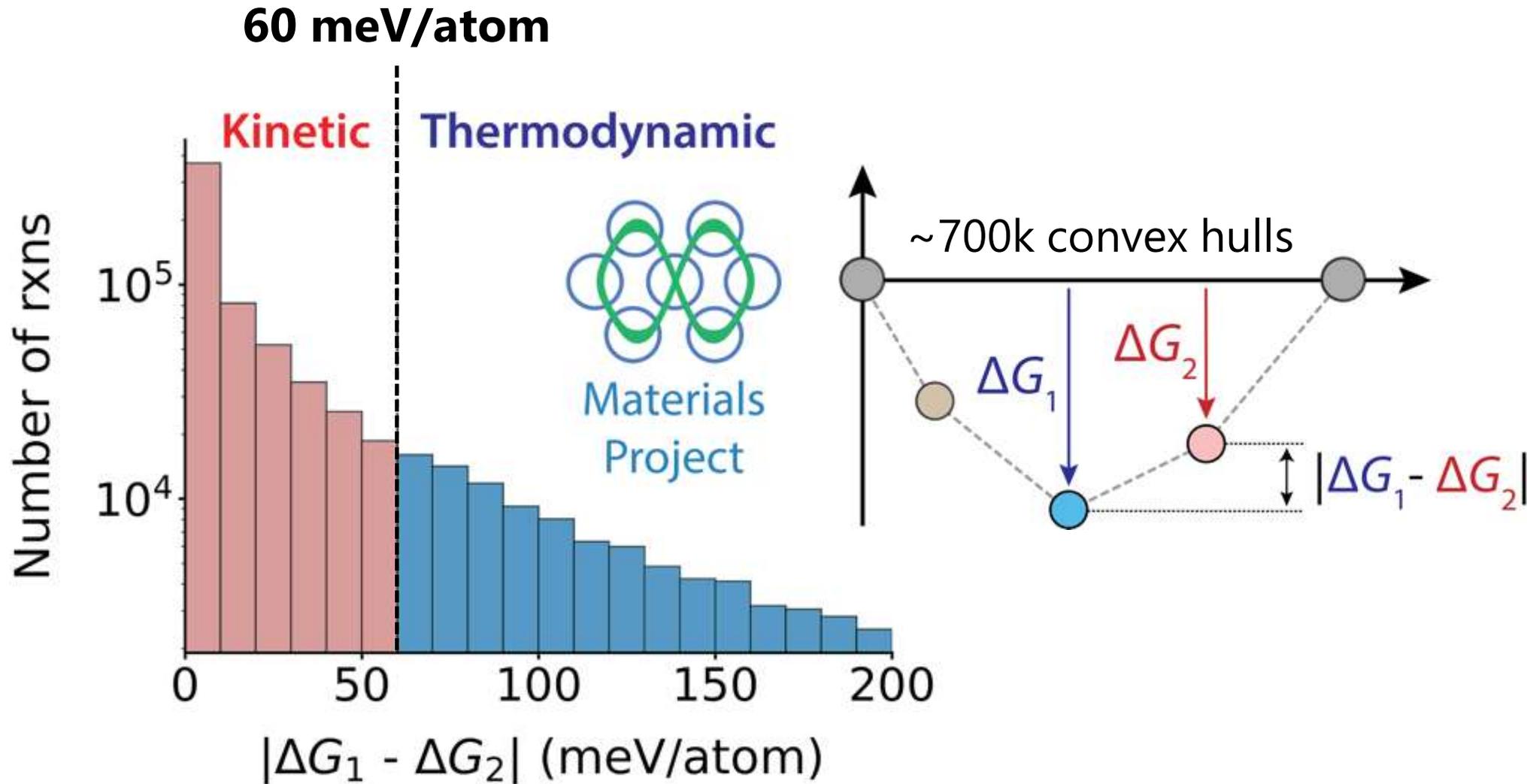
Outcomes show a regime of thermodynamic (ΔG) control



Szymanski *et al.*, Science Advances (2024).



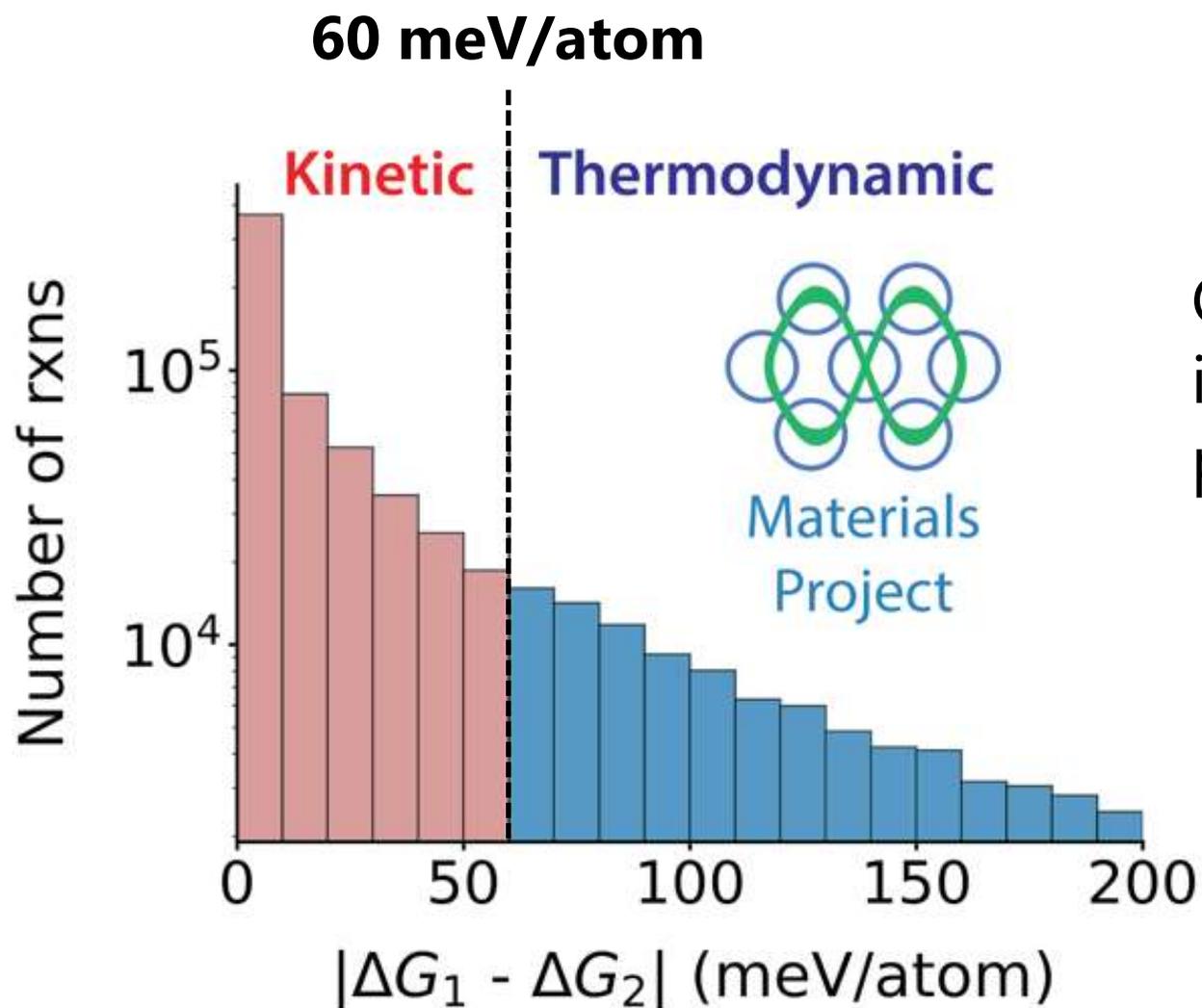
But most reactions are *not* in a thermodynamic regime



Szymanski *et al.*, Science Advances (2024).



But most reactions are *not* in a thermodynamic regime



Only **15%** of the **binary convex hulls** in the Materials Project fall above the proposed threshold of 60 meV/atom

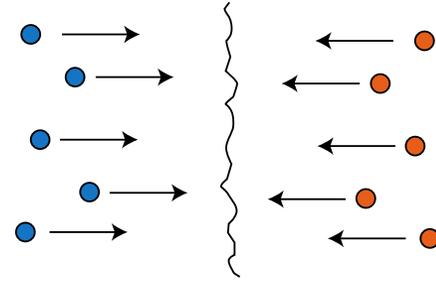
Szymanski *et al.*, Science Advances (2024).



How to deal with the remaining 85% of reactions?

Recall the two factors we neglected:

Diffusion

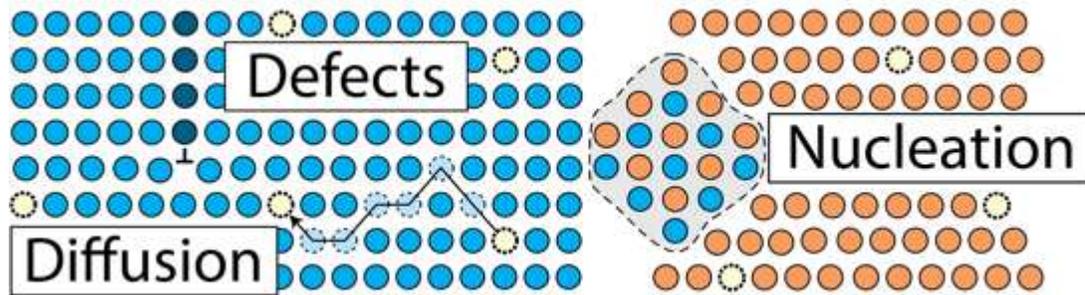


$$\Delta G^* = \frac{16\pi\sigma^3}{3(n\Delta G)^2}$$

Surface energy

Option 1:

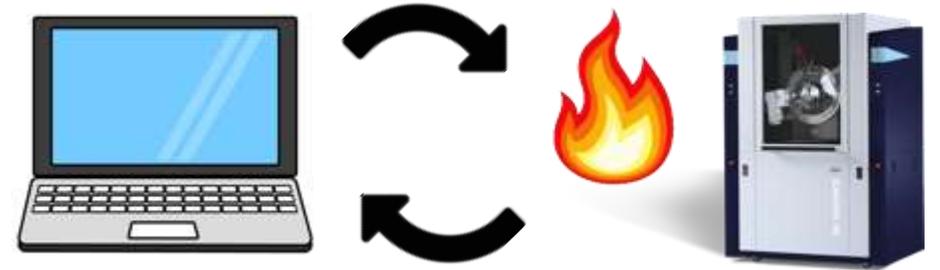
Simulate these processes directly

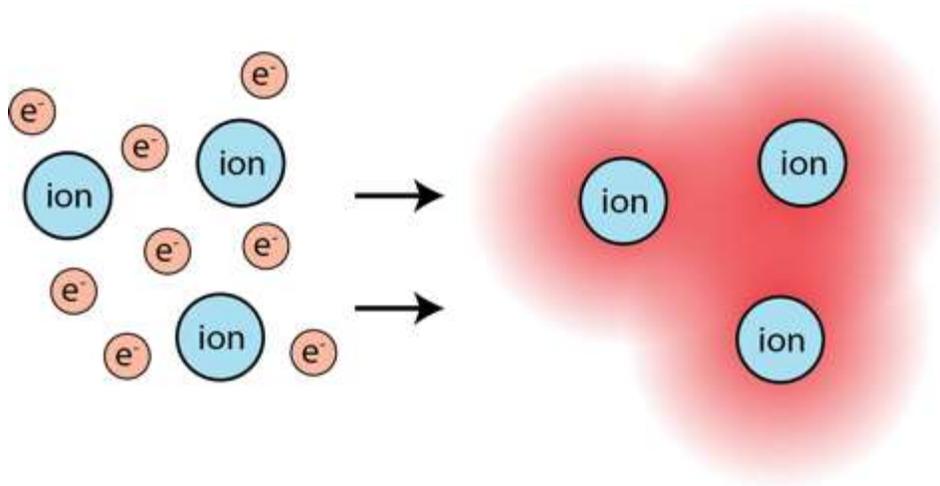


Existing computational models of kinetics are too costly

Option 2:

Integrate our starting predictions (based on ΔG) with experiment and update them accordingly



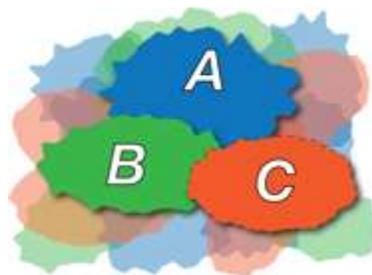


DFT for synthesis planning

- 1) What can we learn from computed thermodynamics?
- 2) Using what we've learned: how can we design synthesis procedures?**

→ **ARROWS**³ →
Autonomous Reaction Route Optimization
With Solid-State Synthesis

Given a target material, find the
best precursors and conditions



How to deal with mixtures of > 2 phases?

Figure adapted from: *A. Miura et al., Advanced Materials (2021).*

Combining predictions with experiments to optimize synthesis



ARROWS³

 Autonomous Reaction Route Optimization

 With Solid-State Synthesis

Given a target material, find the **best precursors and conditions**

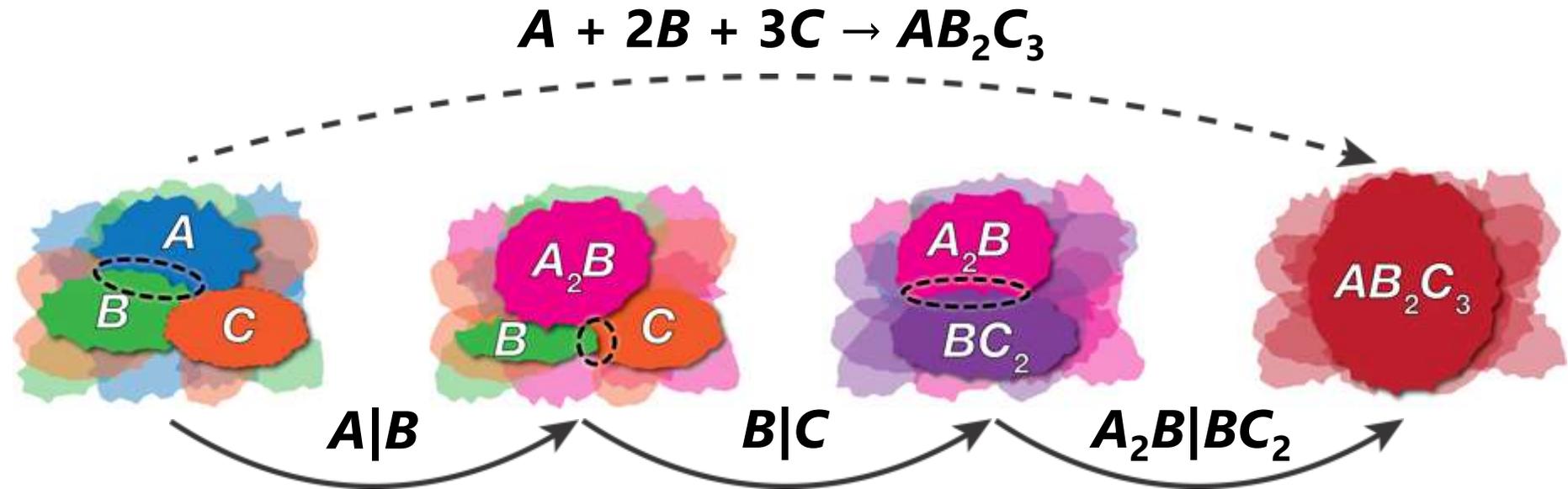


Figure adapted from: *A. Miura et al., Advanced Materials (2021).*

Combining predictions with experiments to optimize synthesis

ARROWS³
Autonomous Reaction Route Optimization
With Solid-State Synthesis

Given a target material, find the **best precursors and conditions**

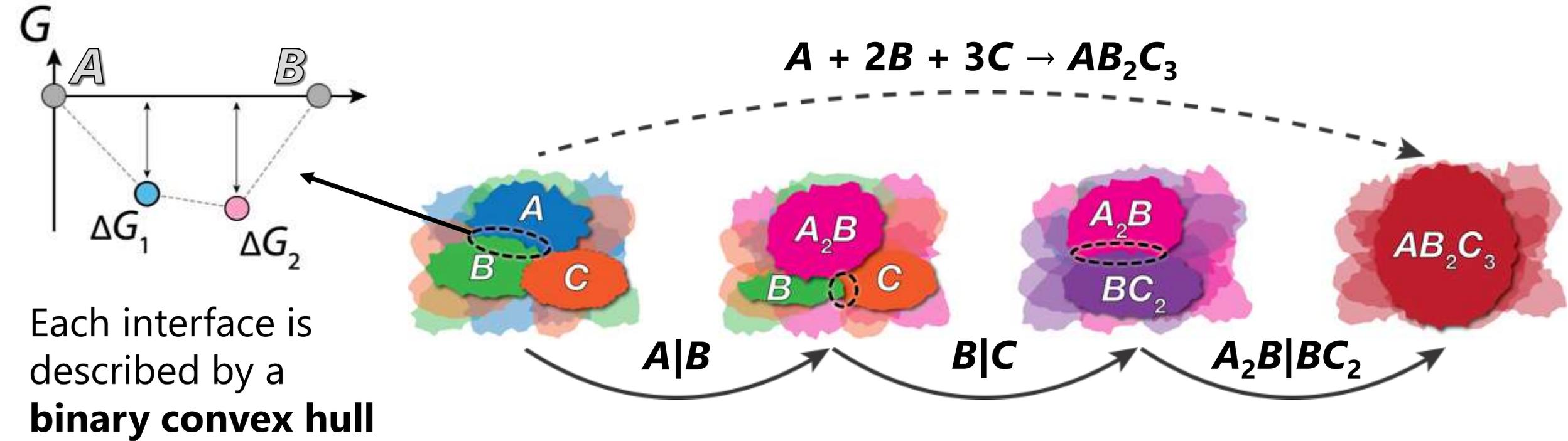
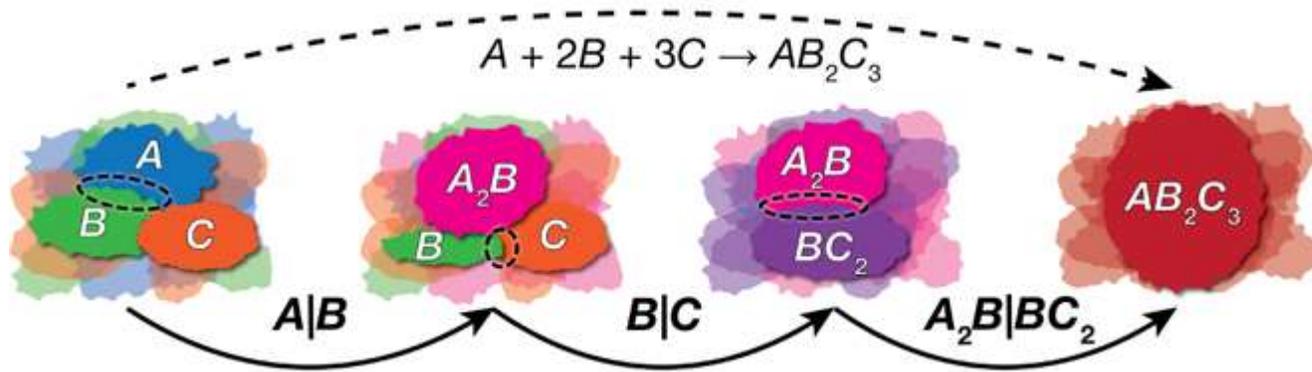
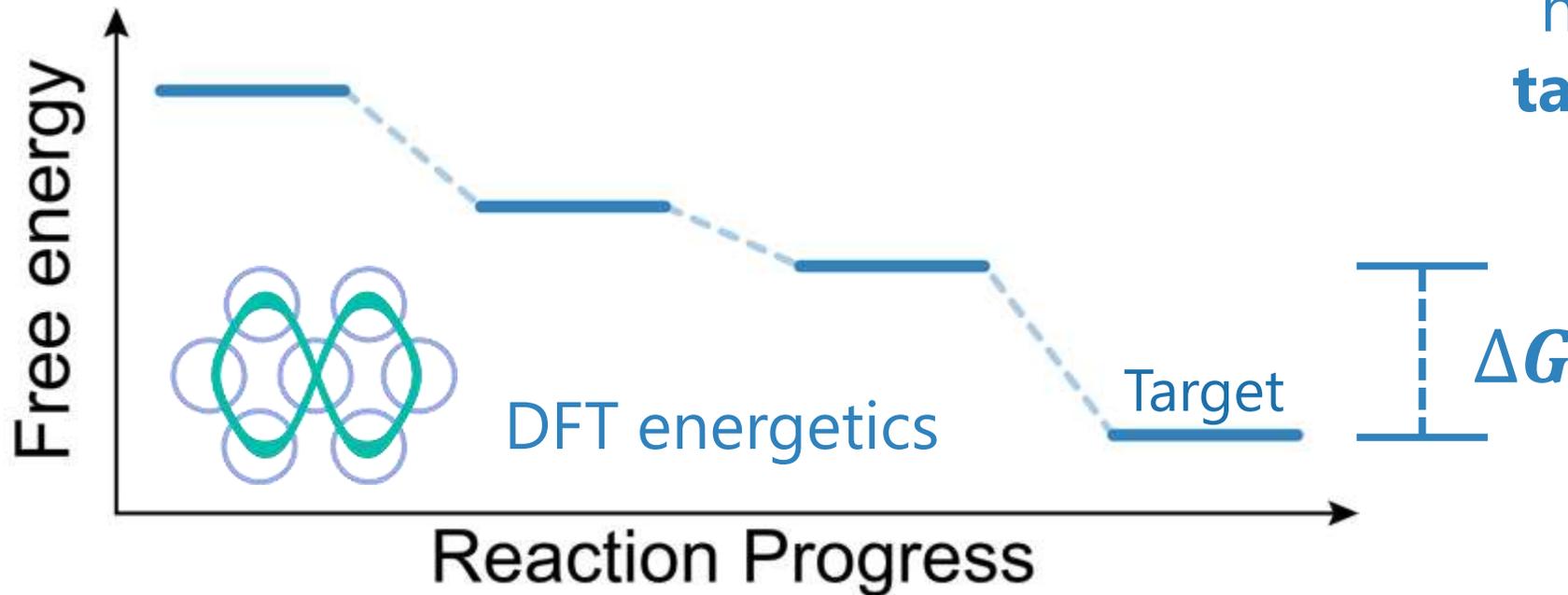


Figure adapted from: A. Miura *et al.*, *Advanced Materials* (2021).

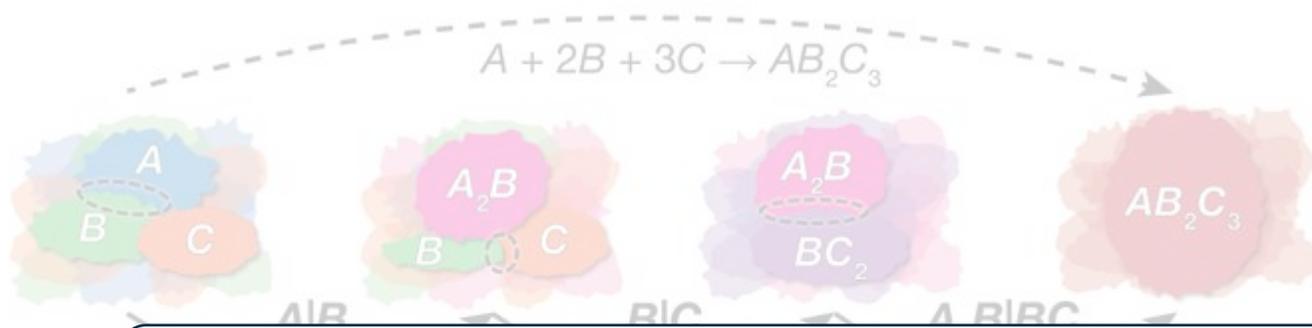
Computed thermodynamics (ΔG) guide the optimization



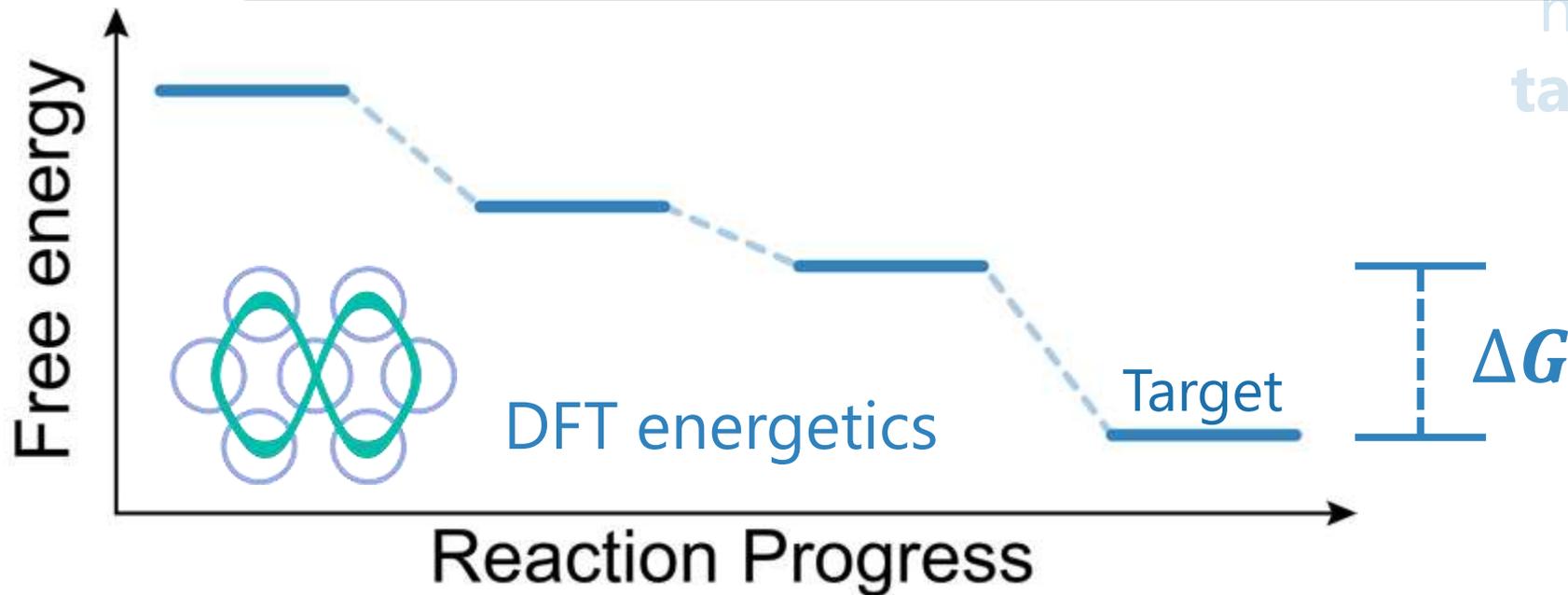
An ideal reaction pathway has **large ΔG** at the **target-forming step**



Computed thermodynamics (ΔG) guide the optimization



But how do we know what these pathways will be?



... pathway
has large ΔG at the
target-forming step

ARROWS learns the reaction pathways



DFT-calculated energetics

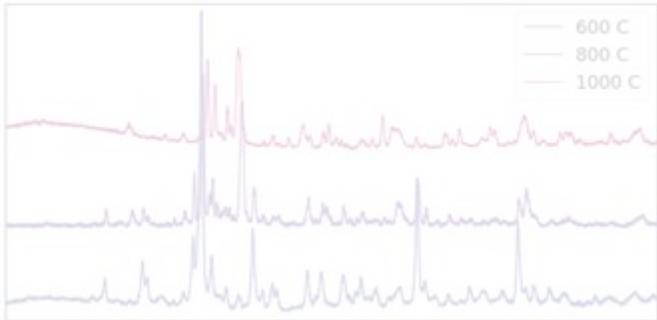


Prioritize precursor sets with **large ΔG**

Precursors
 ΔG
Target

Predict reaction outcomes of new precursor sets

Perform experiments using suggested precursors



ARROWS learns the reaction pathways



DFT-calculated energetics



Prioritize precursor sets with **large ΔG**

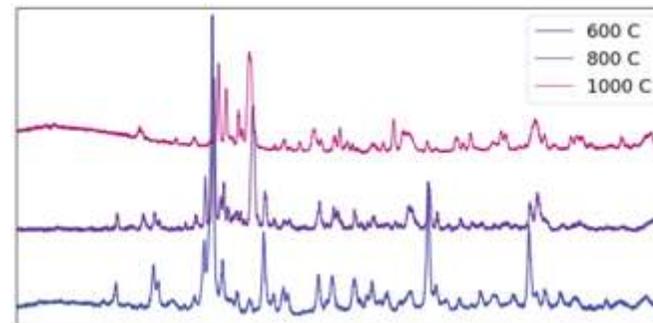
Intermediates

ΔG
Target

Perform experiments using suggested precursors

Predict reaction outcomes of new precursor sets

Learn what pairwise reactions occurred and **re-compute ΔG**



ARROWS learns the reaction pathways



DFT-calculated energetics

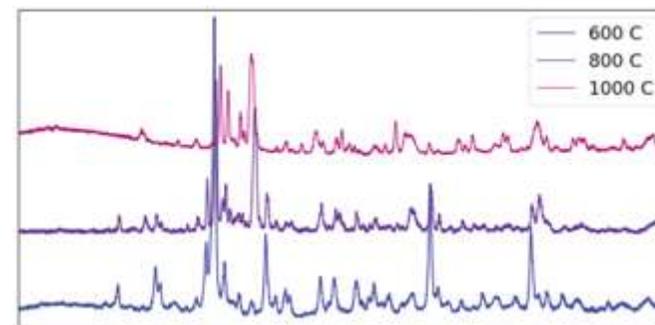
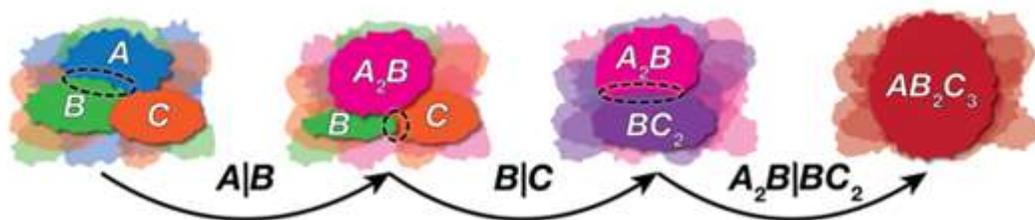
Prioritize precursor sets with **large ΔG**

Intermediates

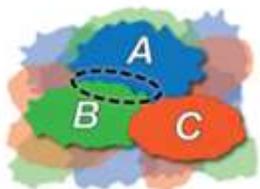
ΔG
Target

Predict reaction outcomes of new precursor sets

Perform experiments using suggested precursors



ARROWS learns the reaction pathways



Avoid pairs that form highly stable intermediates

Prioritize precursor sets that retain **large ΔG**

Intermediates

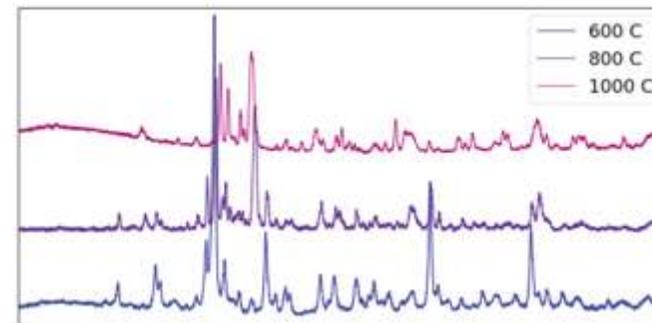
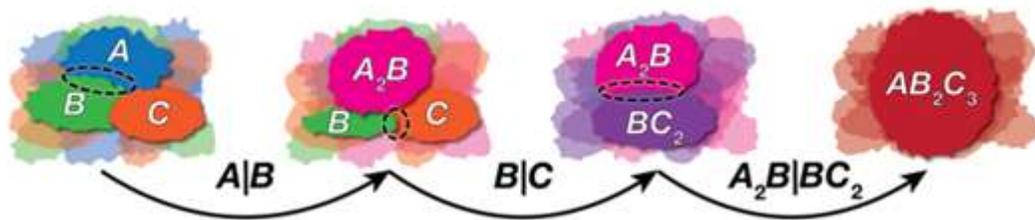
ΔG
Target

Update ranking

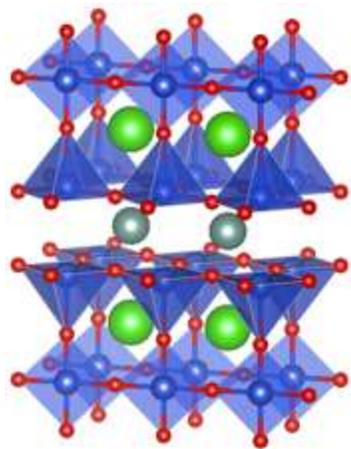
Iterate to success!

Predict reaction outcomes of new precursor sets

Perform experiments using suggested precursors



Finding improved synthesis routes for a high- T_c superconductor



Traditional synthesis of YBCO:

$4 \text{ BaCO}_3 + \text{Y}_2\text{O}_3 + 6 \text{ CuO} @ 950 \text{ }^\circ\text{C}$ for > 12 h

With intermittent regrinding and reheating

Common impurities: BaCuO_2 and Y_2BaCuO_5



ARROWS³
Autonomous Reaction Route Optimization
With Solid-State Synthesis

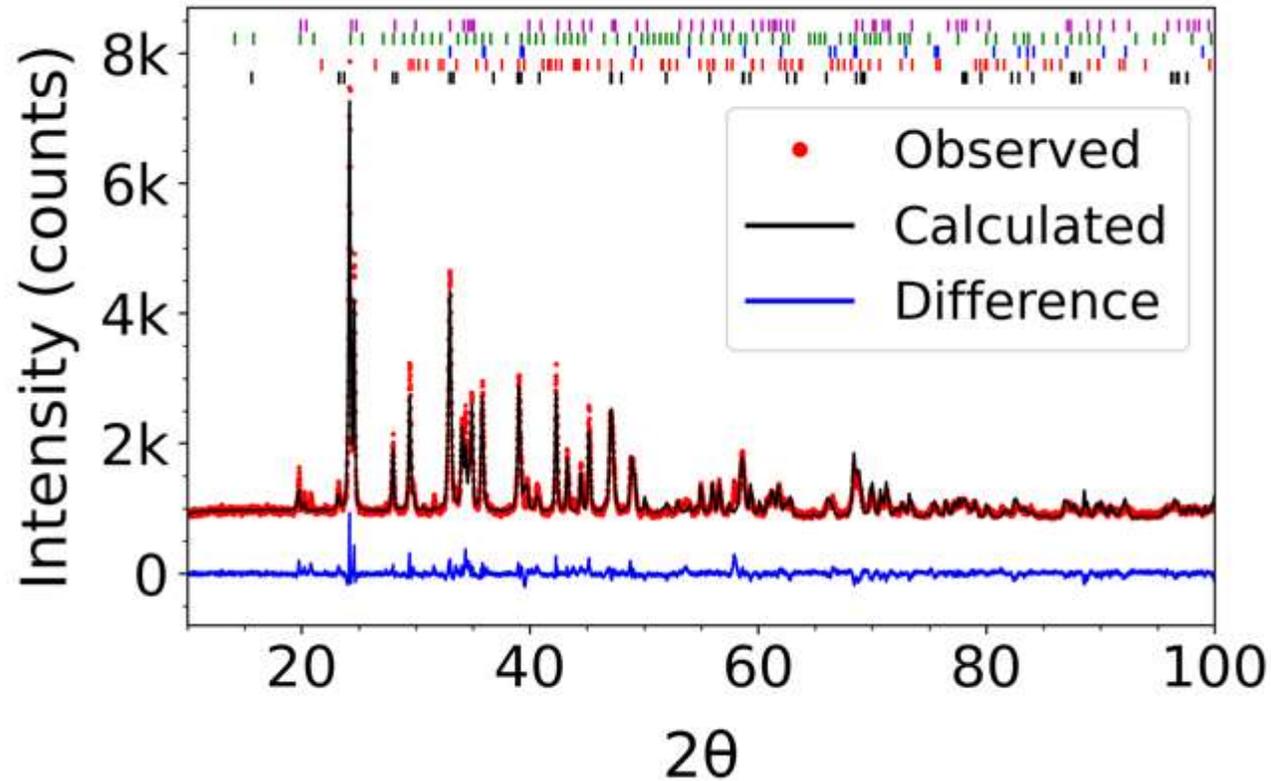
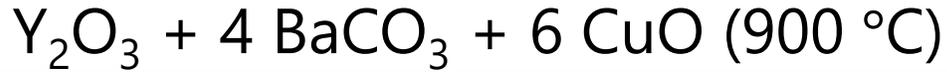
Objective:

Find synthesis routes that yield
~**pure YBCO in 4 h at $\leq 900 \text{ }^\circ\text{C}$**

N. J. Szymanski *et al.*, Nature Communications (2024).



Traditional precursors lead to many impurities after 4 h



47.8% $BaCO_3$

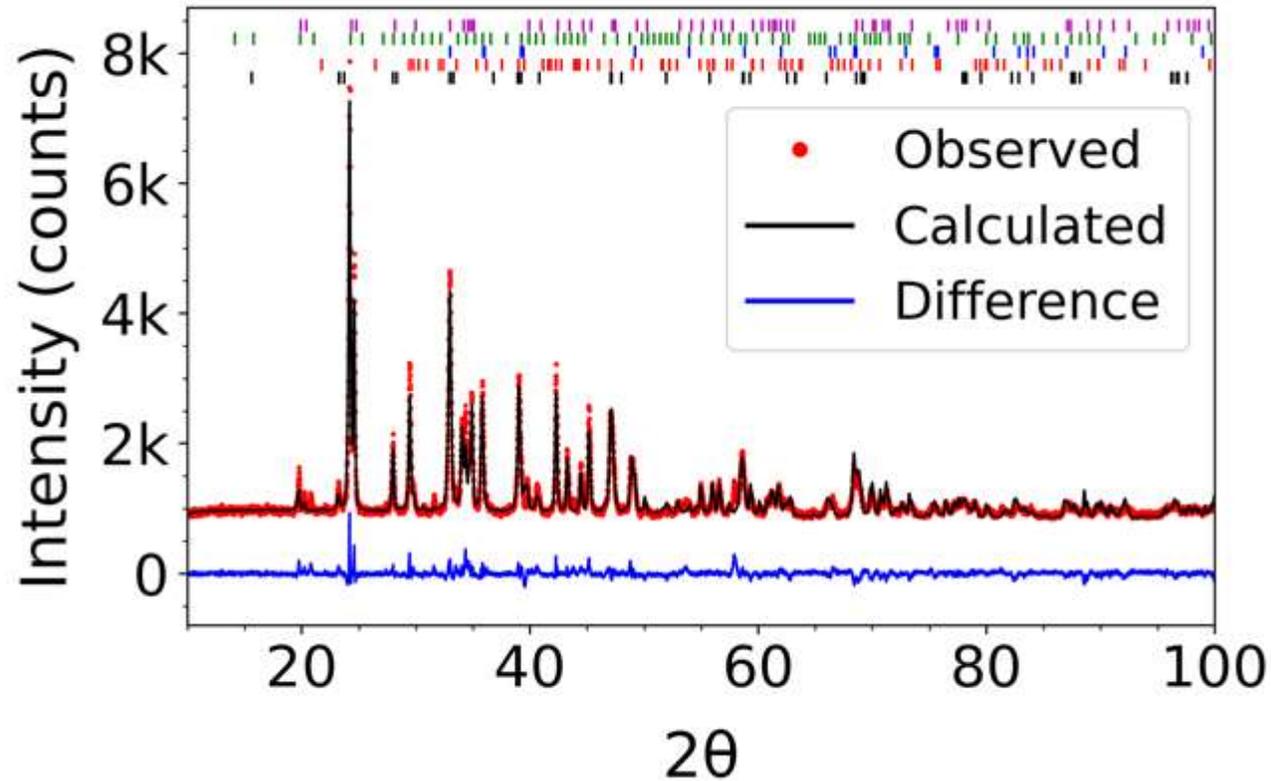
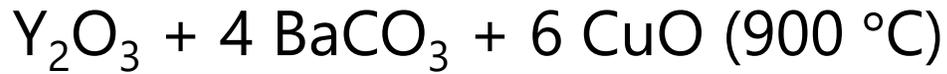
9.7% $BaCuO_2$

27.1% CuO

6.5% Y_2BaCuO_5

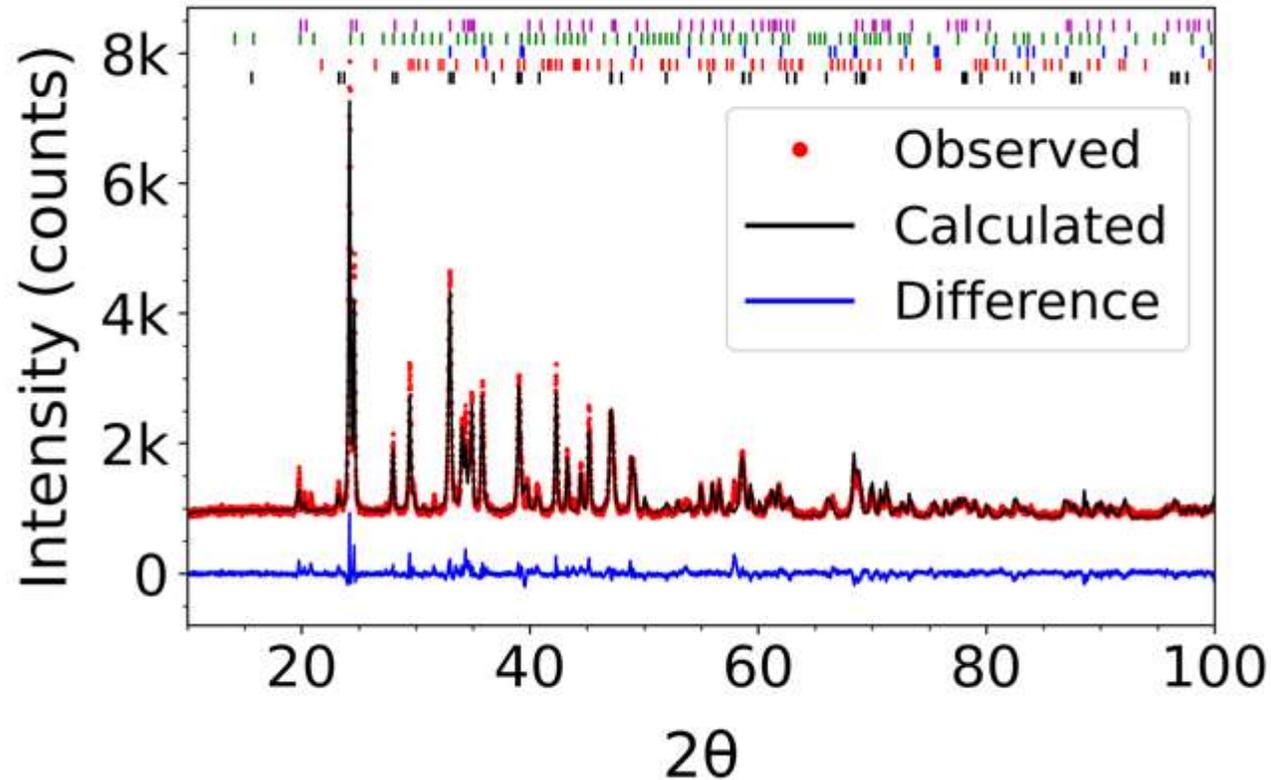
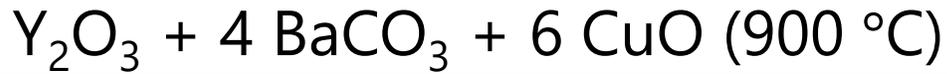
8.9% YBCO → **Low target yield**

Traditional precursors lead to many impurities after 4 h



47.8% $BaCO_3$ → $BaCO_3$ is slow to react before its decomposition (> 1000 °C)
 9.7% $BaCuO_2$
 27.1% CuO
 6.5% Y_2BaCuO_5
 8.9% YBCO

Traditional precursors lead to many impurities after 4 h



47.8% $BaCO_3$

9.7% $BaCuO_2$

27.1% CuO

6.5% Y_2BaCuO_5

8.9% YBCO



$BaCuO_2$ and subsequently

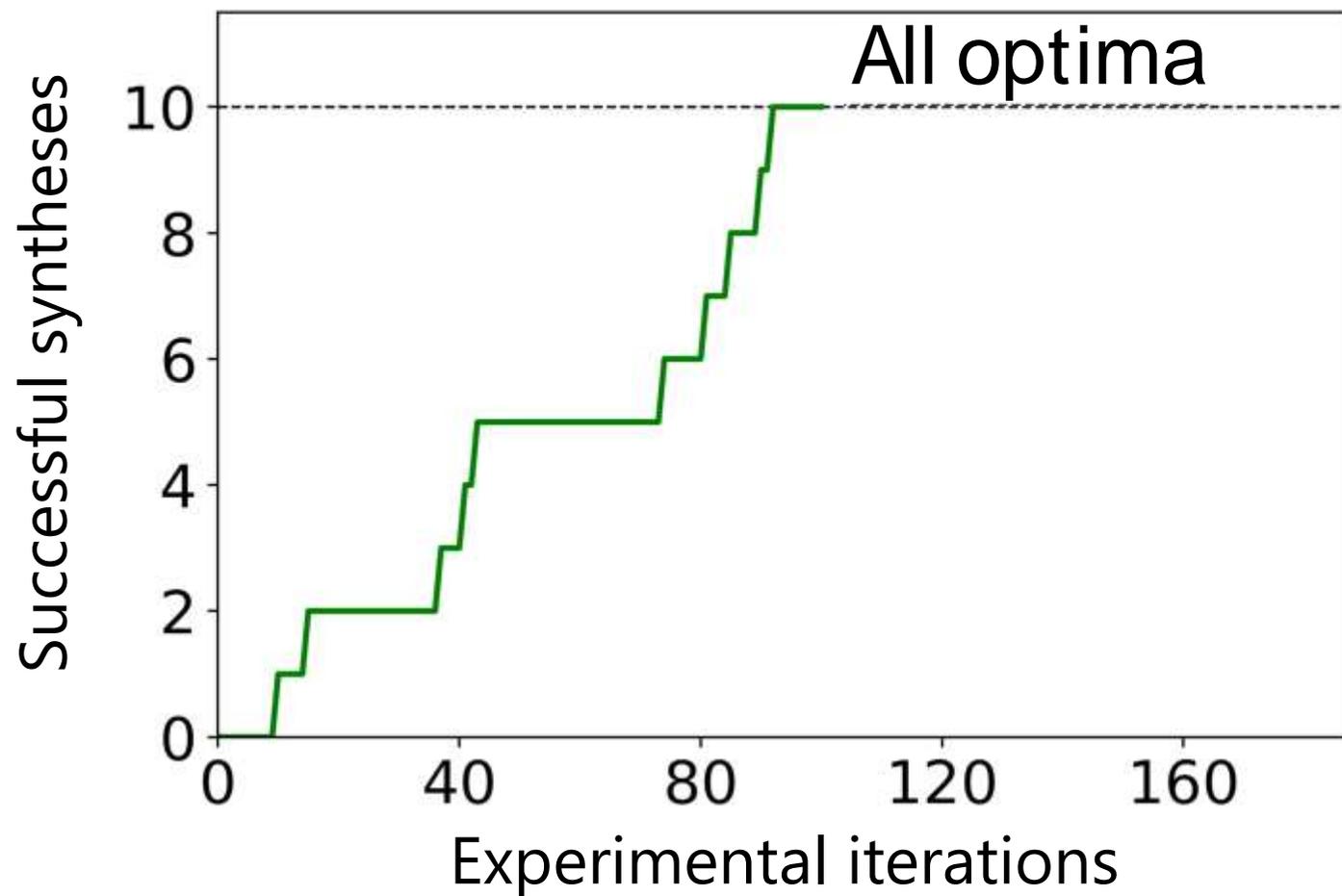


Y_2BaCuO_5

These are **impurities we'd like to avoid**

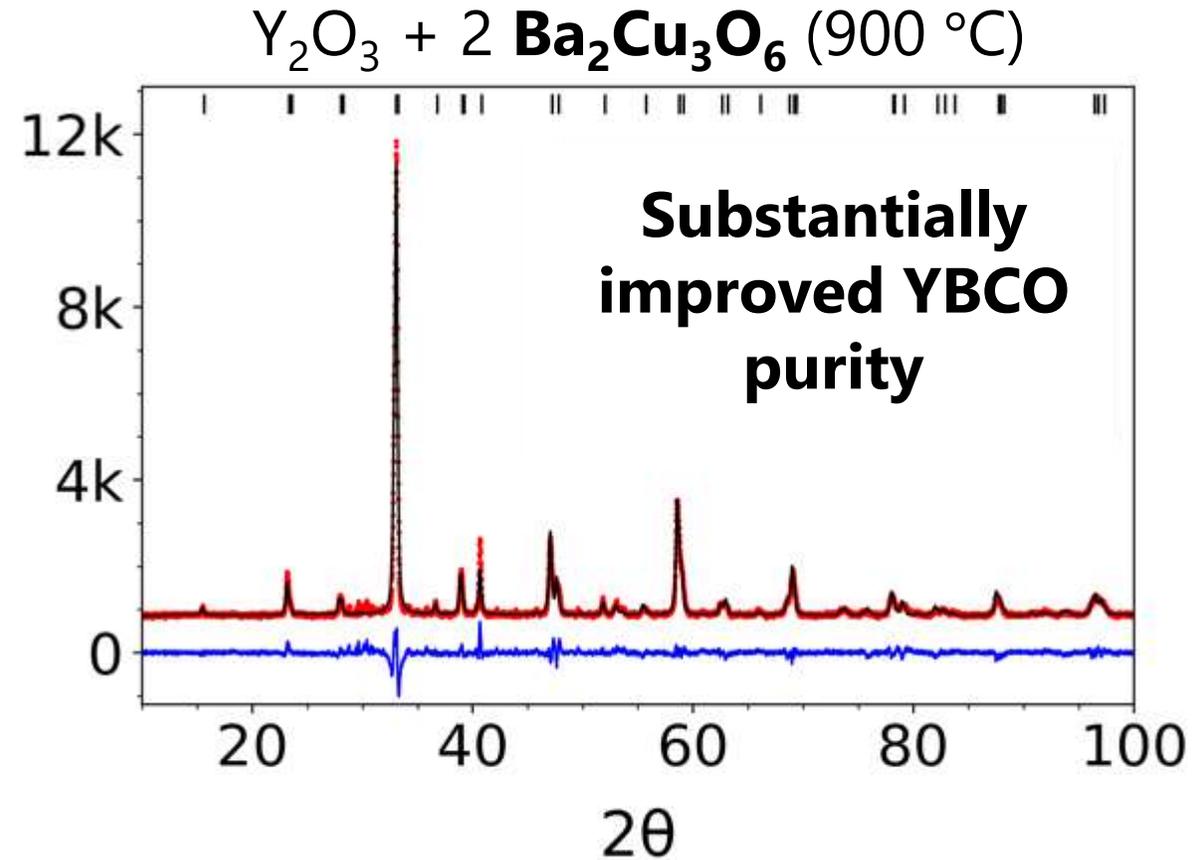
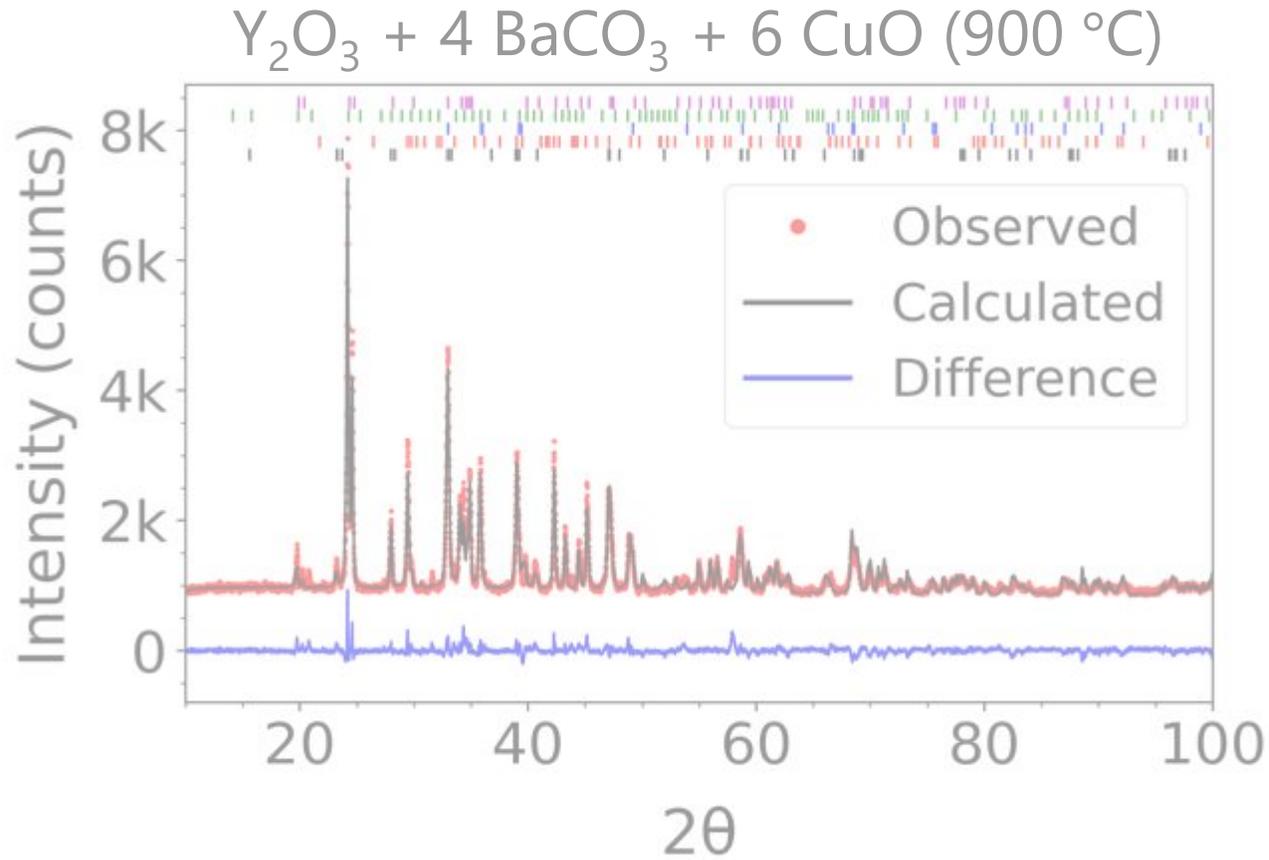


ARROWS succeeds in identifying fast synthesis routes



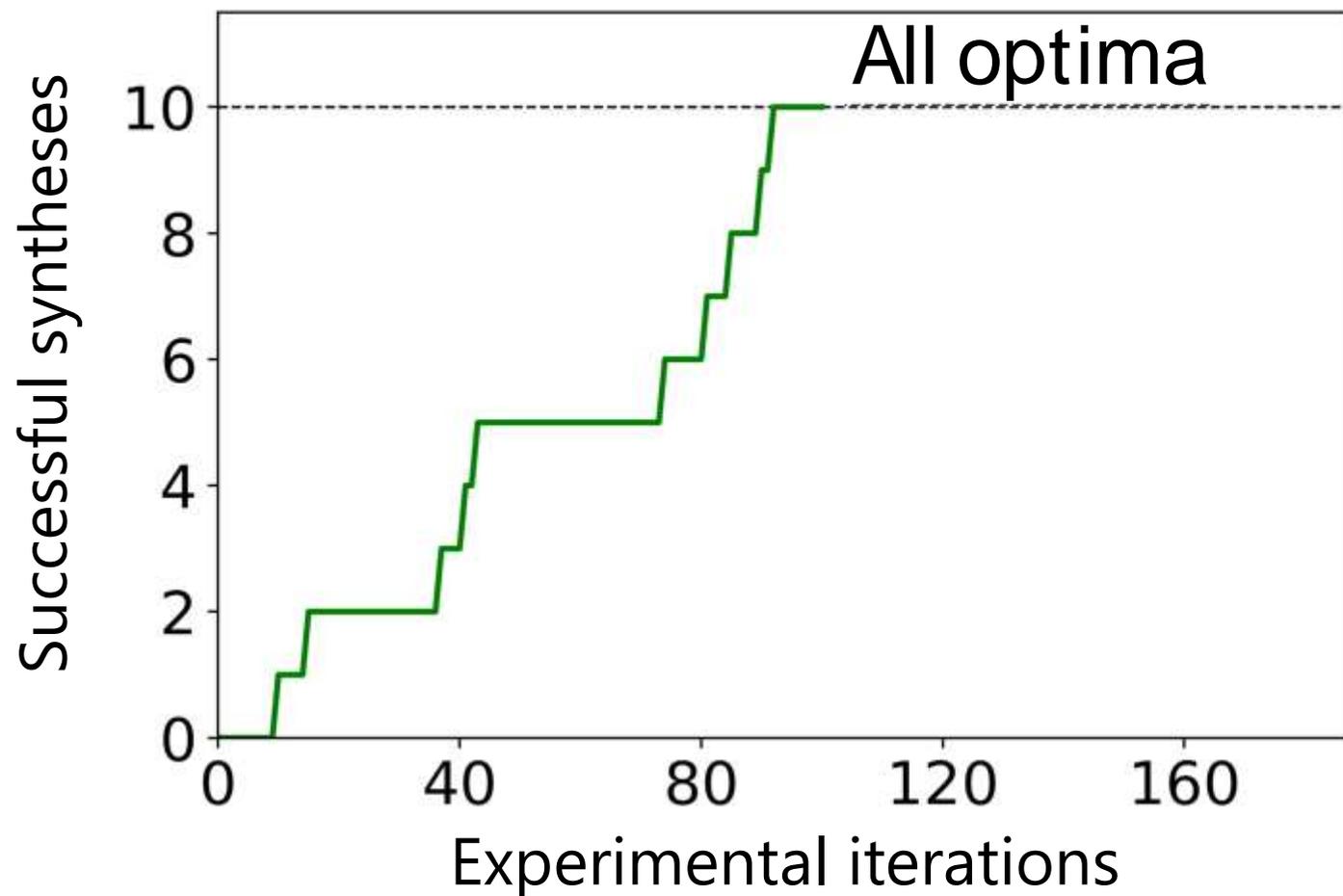
In **87 iterations**, ARROWS found **10 synthesis routes** that produce YBCO with **high yield in ≤ 4 h**

The optimized precursors lead to much higher purity



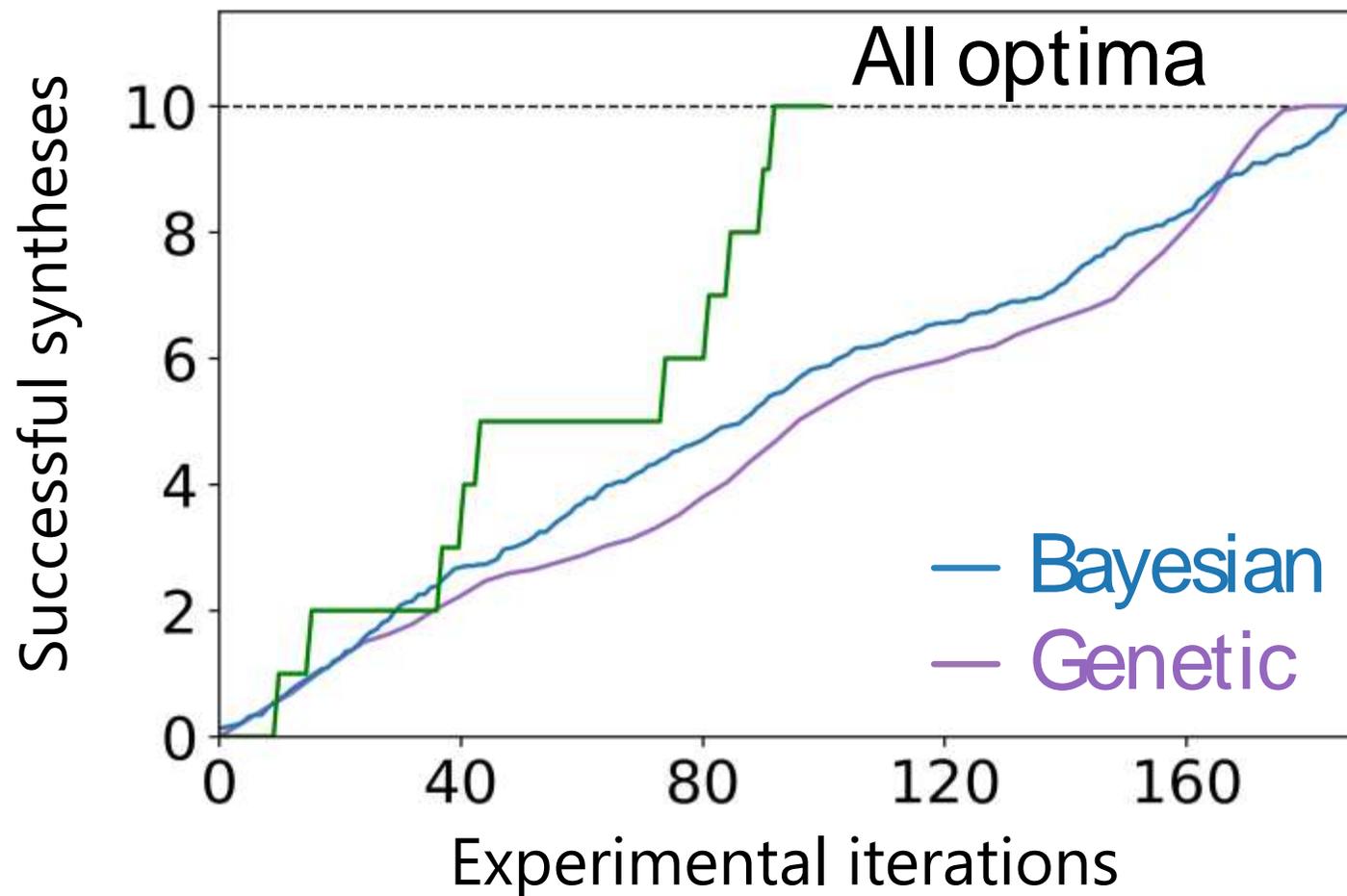
$Ba_2Cu_3O_6$ and Y_2O_3 react directly to form YBCO at $T \leq 900$ °C

ARROWS succeeds in identifying fast synthesis routes



In **87 iterations**, ARROWS found **10 synthesis routes** that produce YBCO with **> 95% yield in ≤ 4 h**

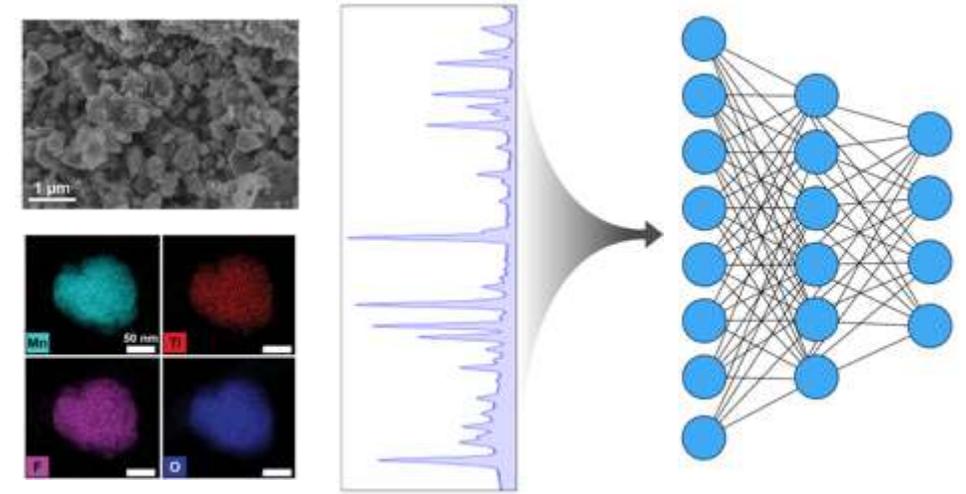
Is ARROWS efficient?



In **87 iterations**, ARROWS found **10 synthesis routes** that produce YBCO with **> 95% yield in ≤ 4 h**

For comparison:
Bayesian optimization and genetic algorithms required **> 160 iterations**

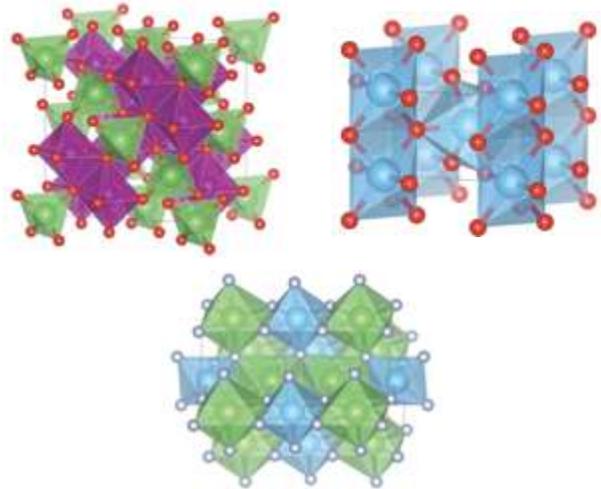
With automated decision making,
analysis of characterization data
becomes the bottleneck



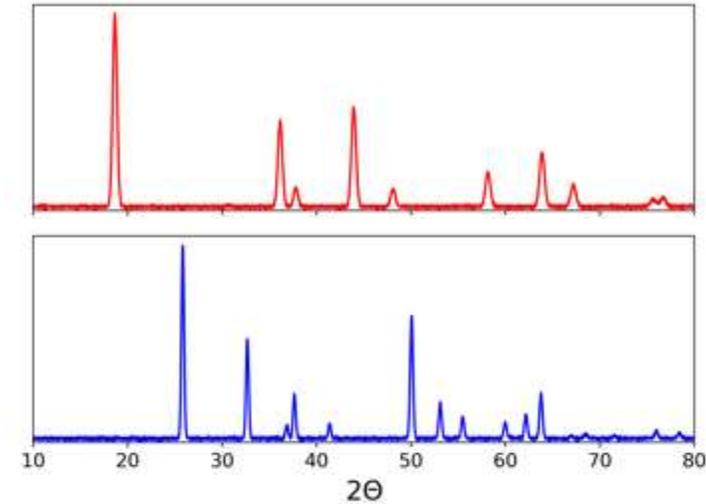
AI for characterization

Powder X-ray diffraction (XRD)
→ what phases are present

Simulating XRD is easy, but *solving* XRD is hard



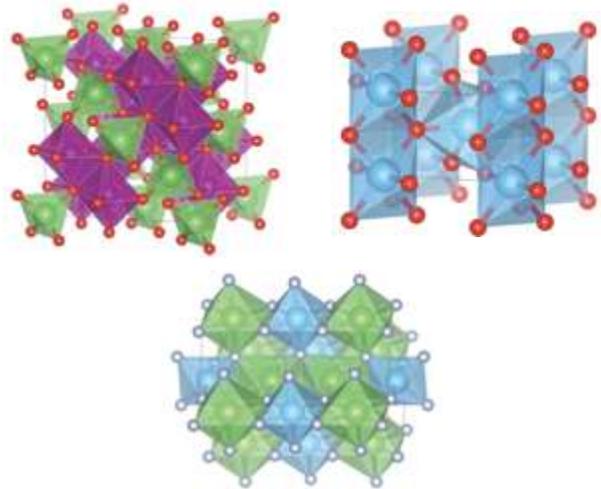
$$F_{hkl} = \sum_{j=1}^N f_j e^{-2\pi i(hx_j + ky_j + lz_j)}$$



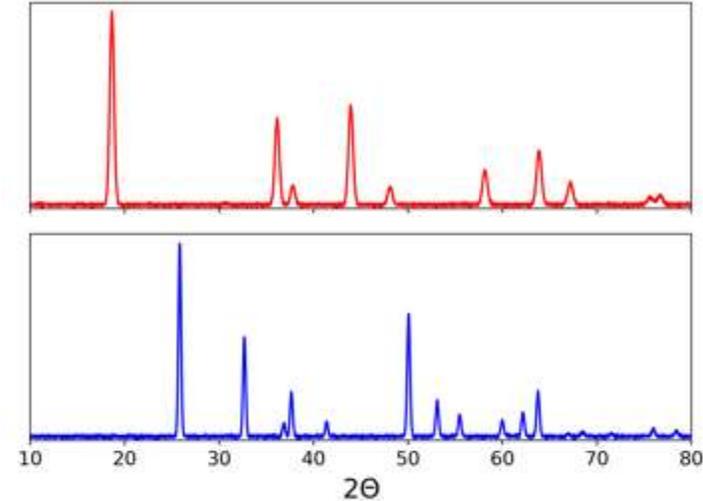
How to go from XRD to structure?

- **Experimental artifacts** modify peaks
- **Multi-phase mixtures** are common
- The pattern **may not be unique**

Simulating XRD is easy, but *solving* XRD is hard



$$F_{hkl} = \sum_{j=1}^N f_j e^{-2\pi i(hx_j + ky_j + lz_j)}$$

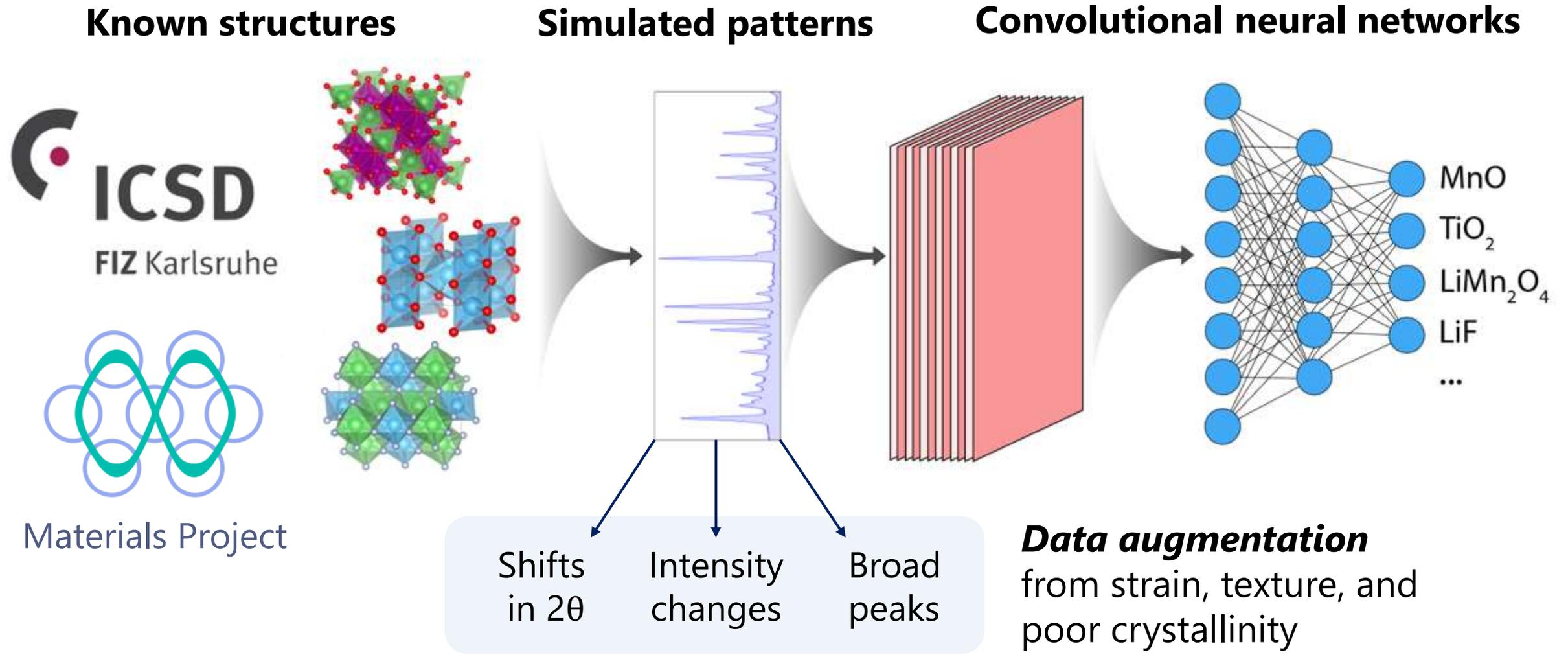


Train ML to solve reverse problem!

- **Experimental artifacts** modify peaks
 - **Multi-phase mixtures** are common
 - The pattern **may not be unique**
- } These can be ***simulated*** and used to train ML models
- ML can be ***probabilistic***



Neural networks are trained on simulated XRD patterns

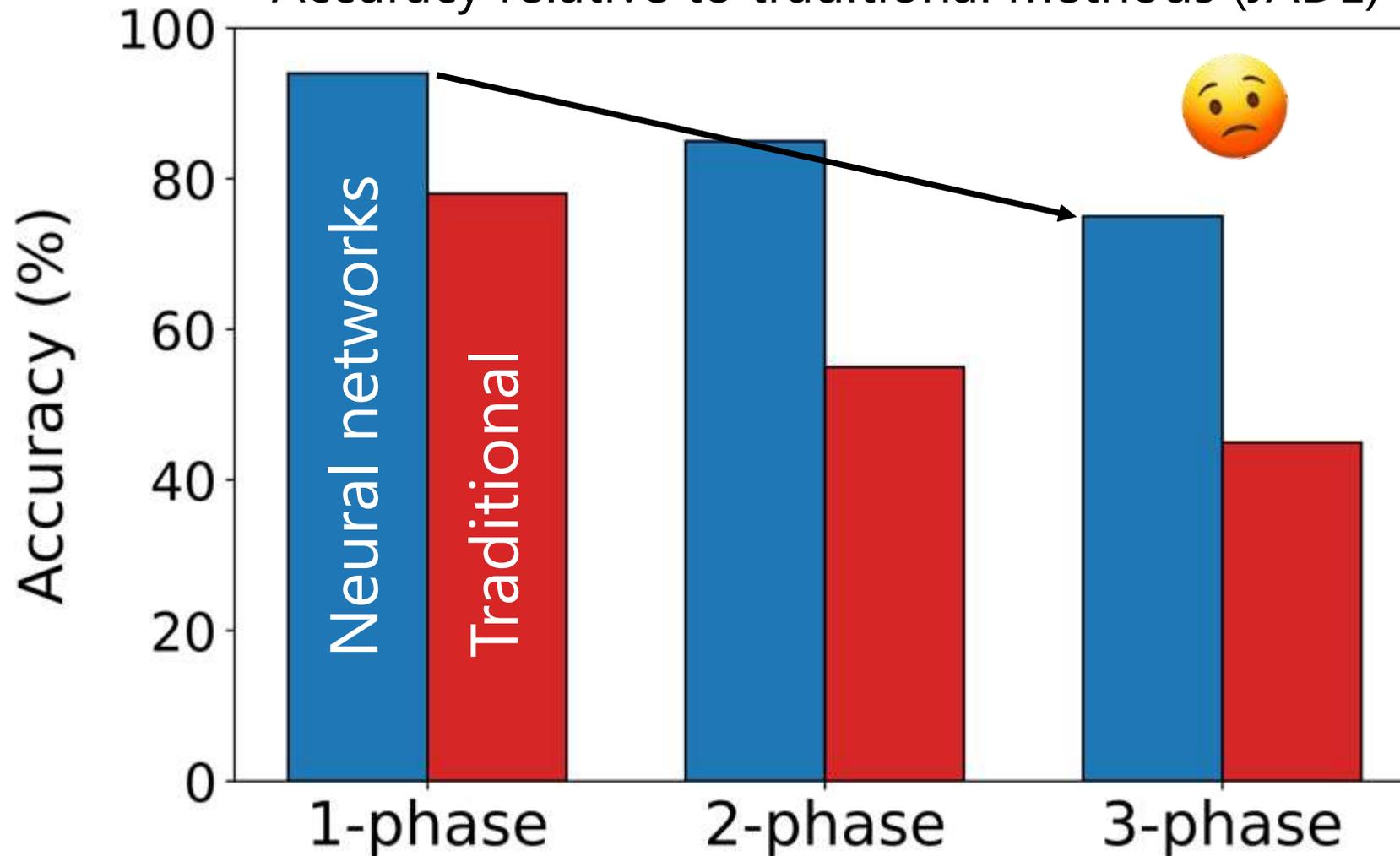


N. J. Szymanski *et al.*, Chemistry of Materials (2021).



ML outperforms traditional methods, but limitations persist

Accuracy relative to traditional methods (JADE)



Mixtures are difficult to characterize reliably

Simulated test data:

4k patterns augmented with exp artifacts

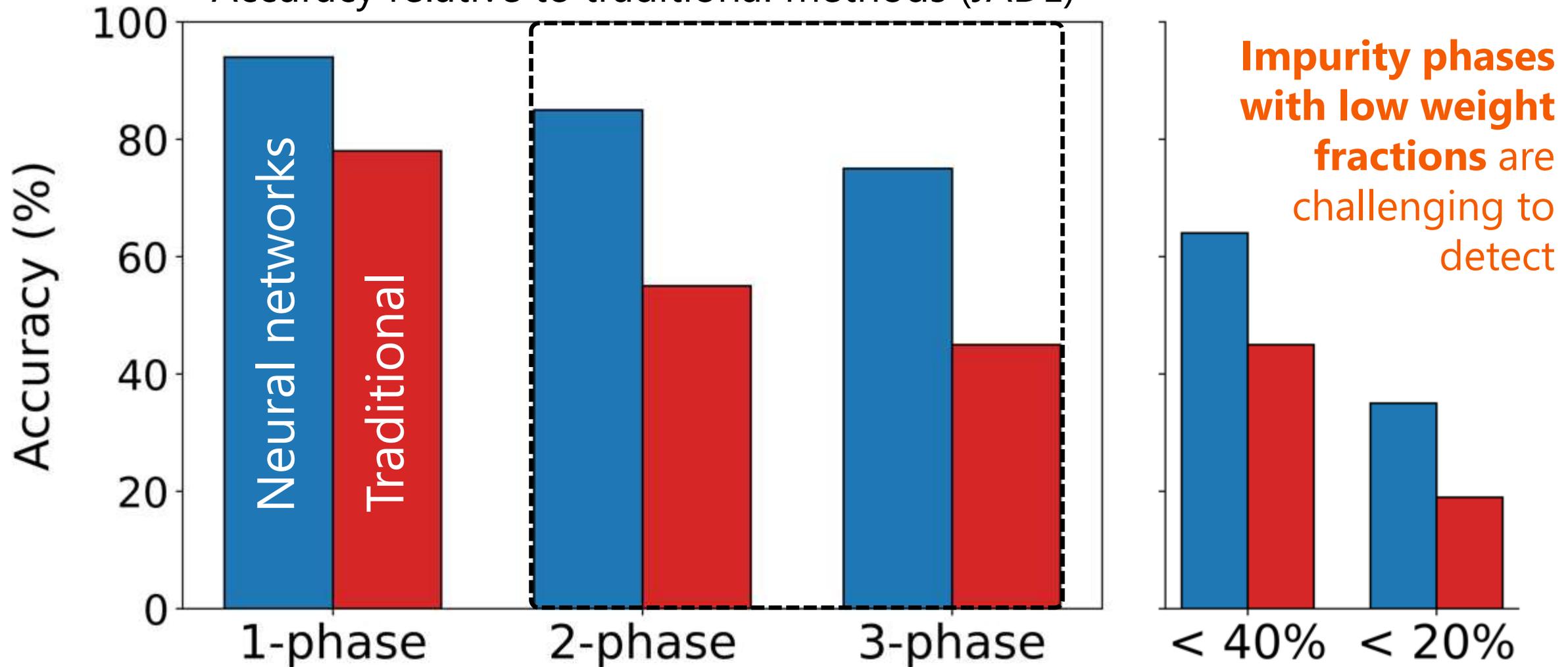
Experimental test data:

80 patterns augmented with exp artifacts

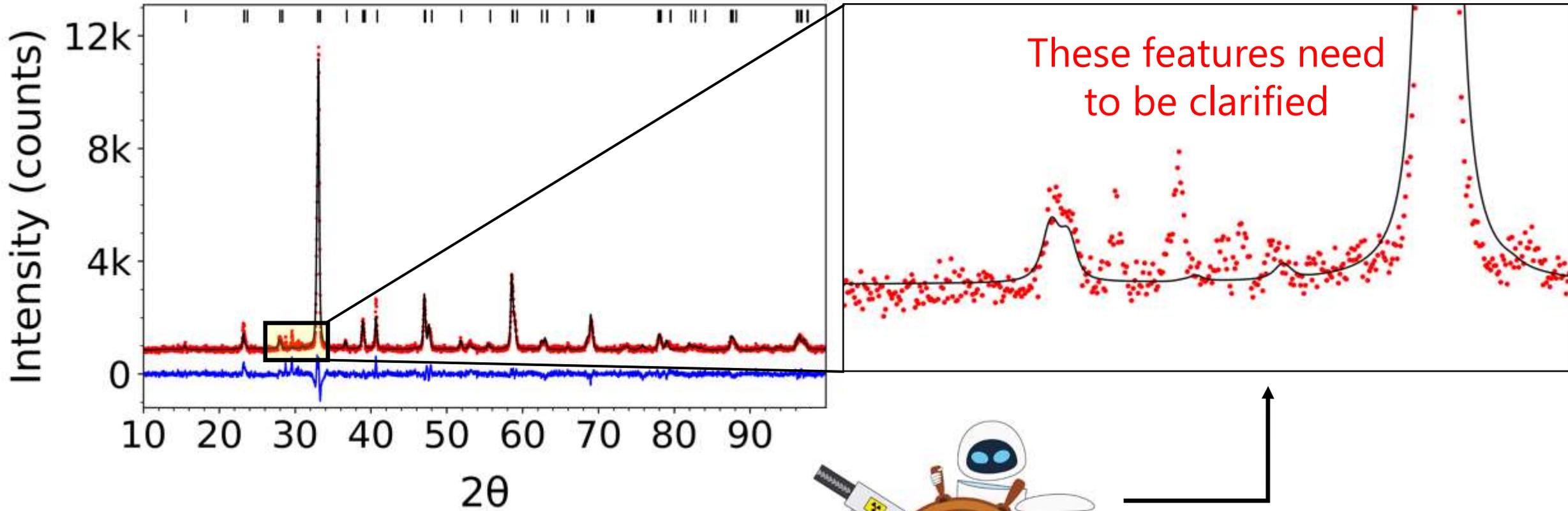
(Li-Mn-Ti-O-F)

ML outperforms traditional methods, but limitations persist

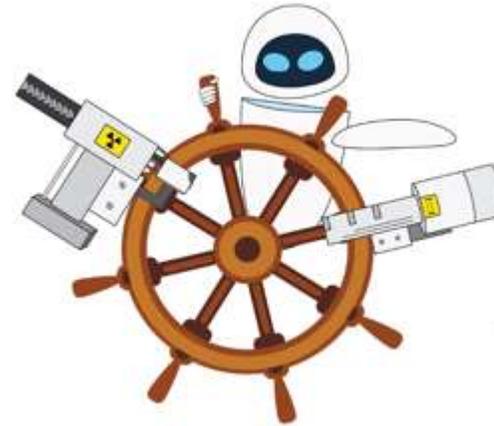
Accuracy relative to traditional methods (JADE)



Can we *adaptively* control XRD to focus on impurities?

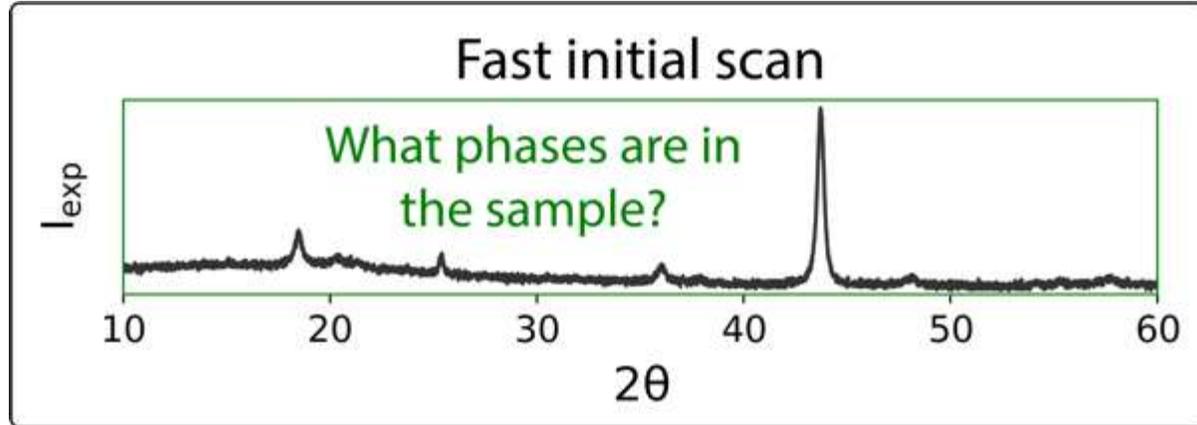


What impurity phases are present?



Steer diffractometer toward region of interest

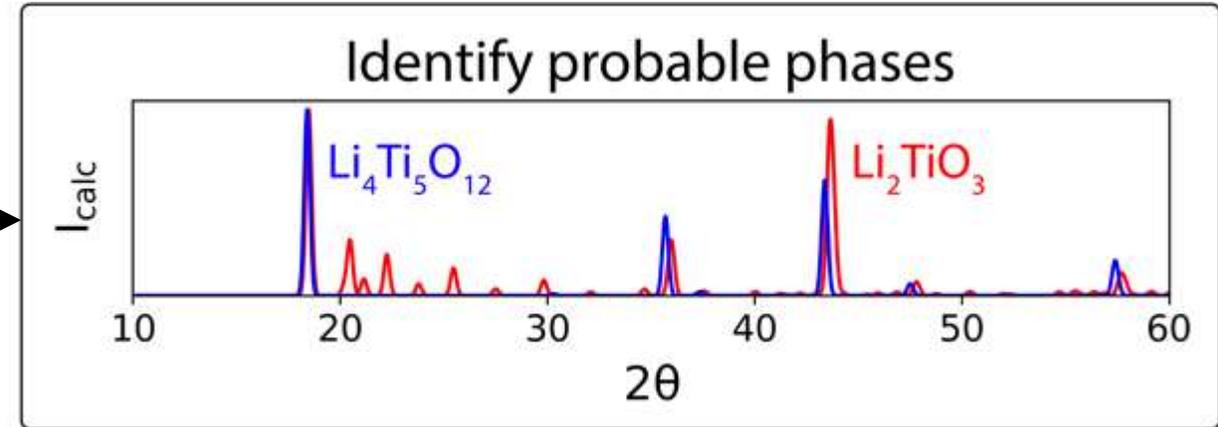
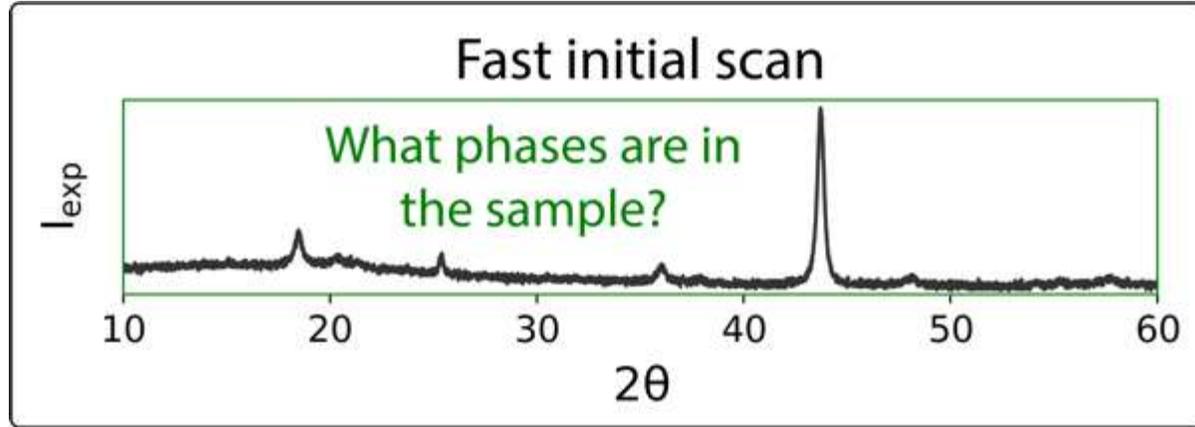
Adaptive XRD workflow: initial scan is fast and noisy



N. J. Szymanski *et al.*, npj Computational Materials (2023).

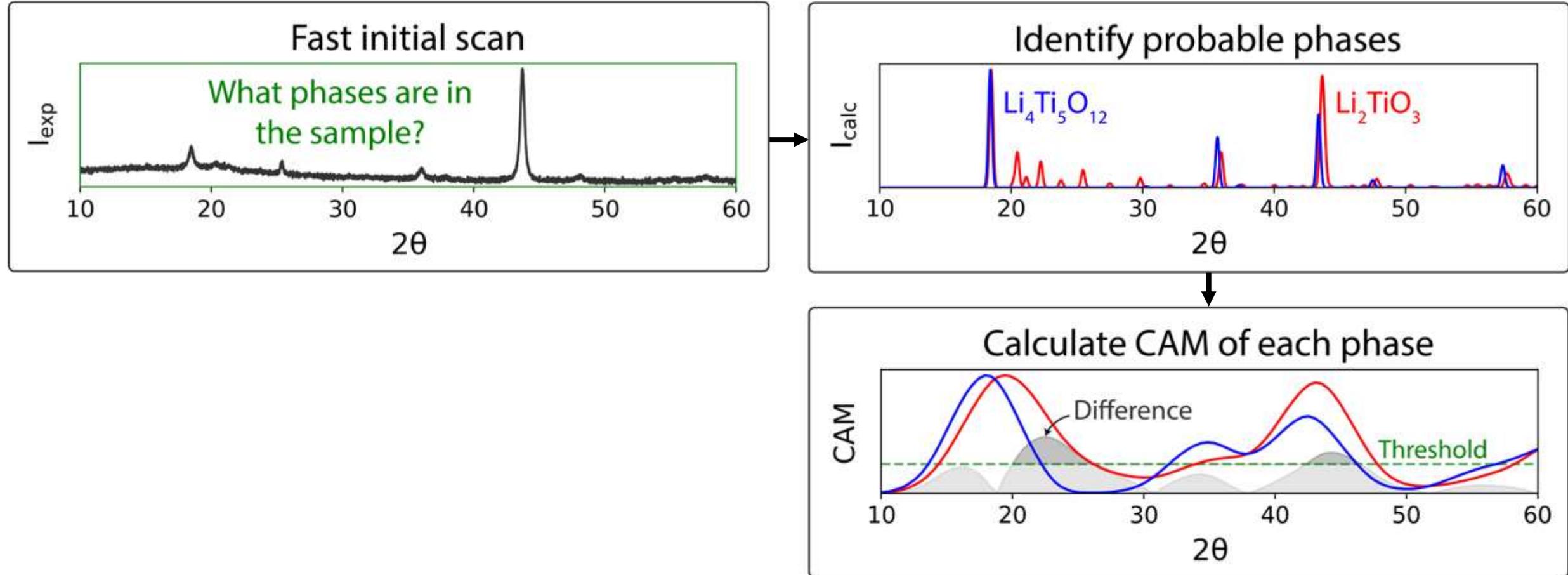


Adaptive XRD workflow: CNN predicts likely phases



N. J. Szymanski *et al.*, npj Computational Materials (2023).

Adaptive XRD workflow: CAMs highlight areas of interest



N. J. Szymanski *et al.*, npj Computational Materials (2023).



Adaptive XRD workflow: CAMs highlight areas of interest

Model predicts **dog**

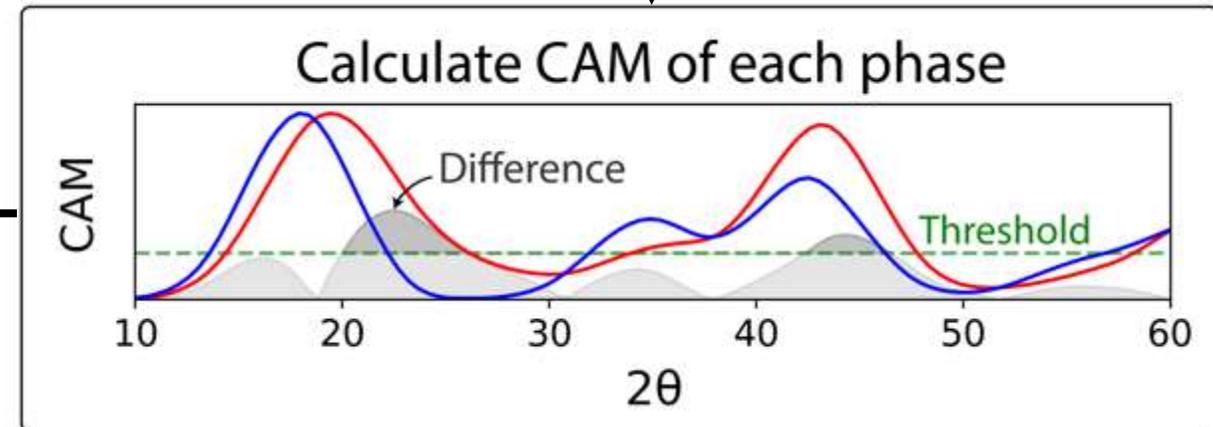
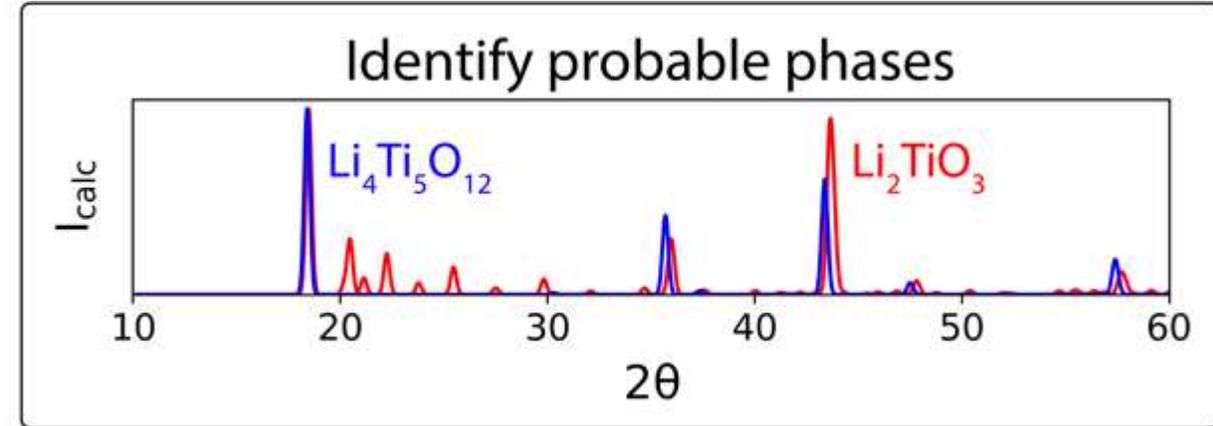


Model predicts **cat**



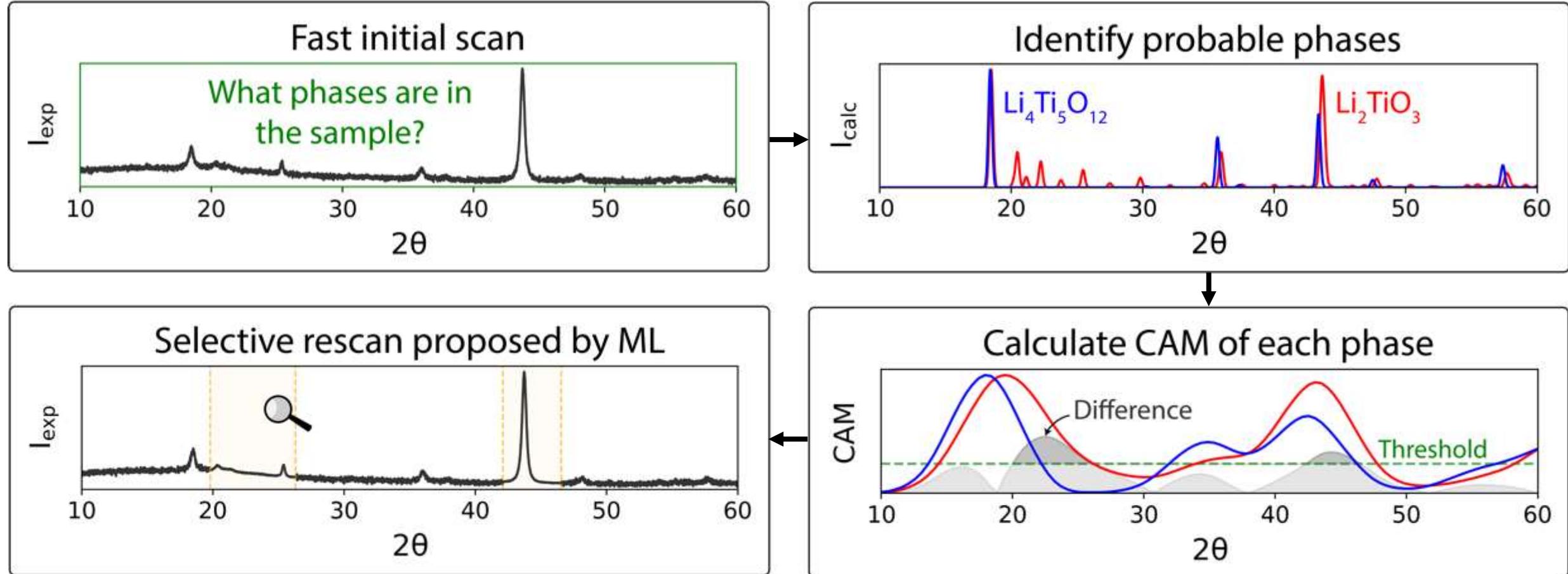
Example from [Keras tutorials](#)

**Class
activation
map (CAM)**



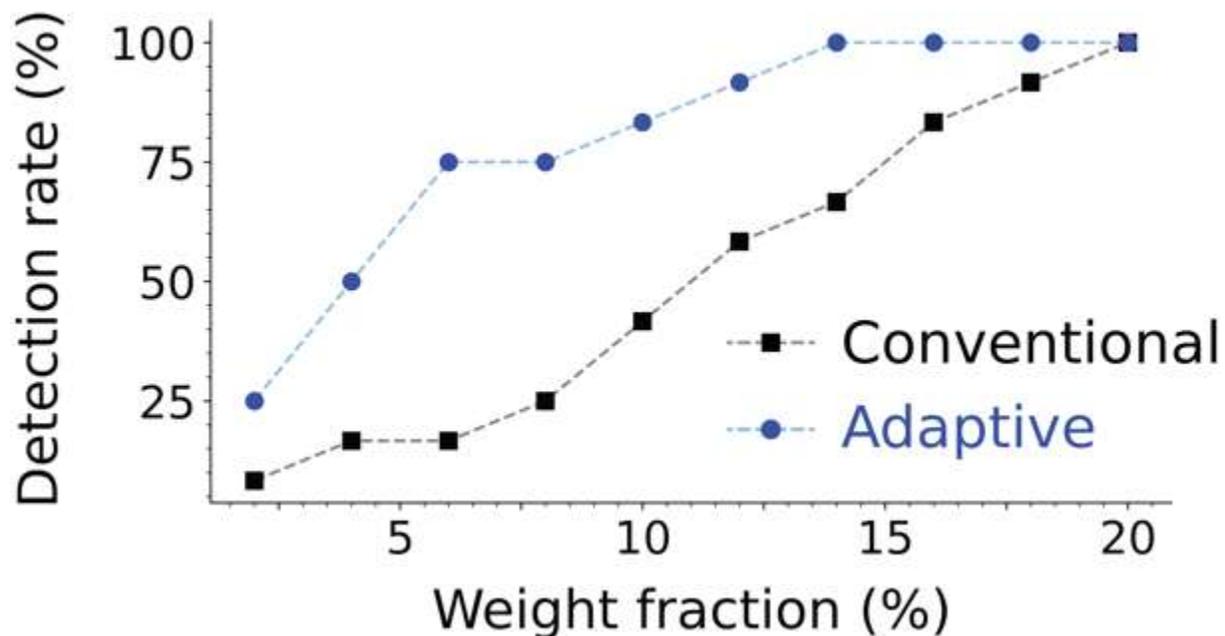
N. J. Szymanski *et al.*, *npj Computational Materials* (2023).

Adaptive XRD workflow: slower rescans clarify key features



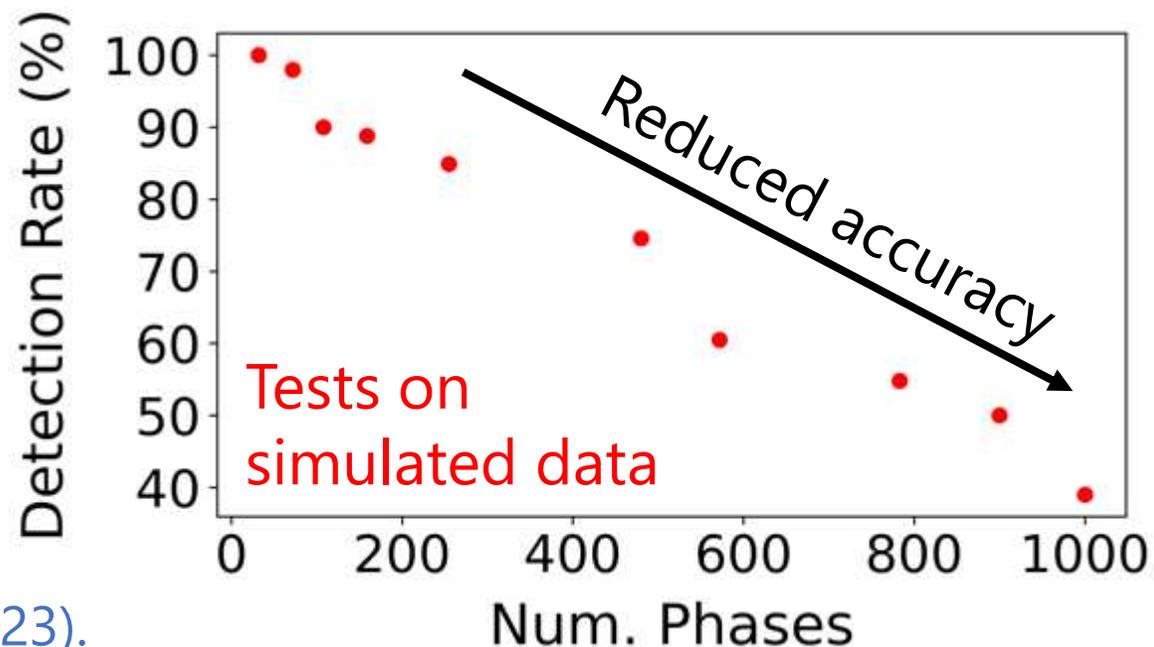
N. J. Szymanski *et al.*, npj Computational Materials (2023).

Adaptive scans more effectively detect secondary phases



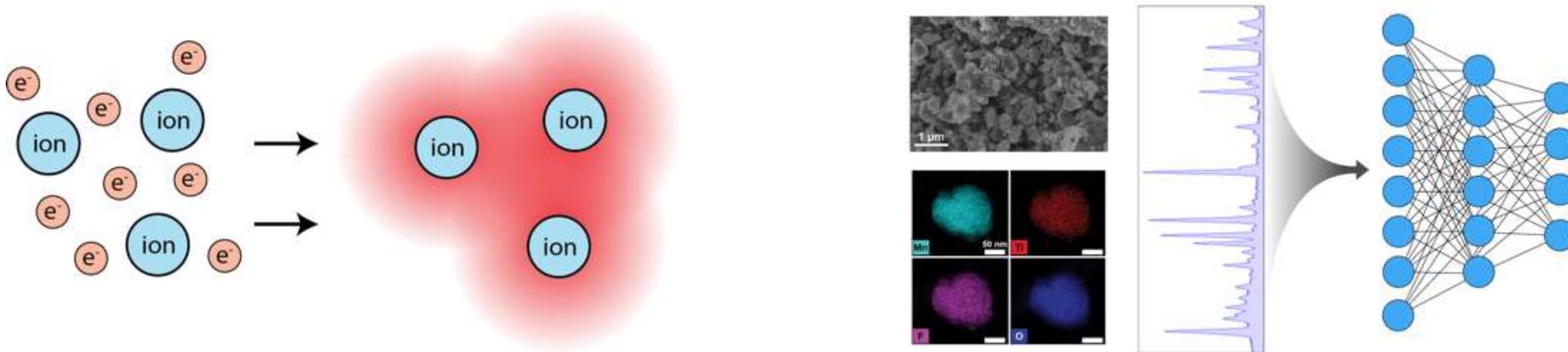
- XRD performed on **120 mixtures** in the **Li-La-Zr-O space**, prepared with varied impurity amounts
- **Adaptive scans show improved accuracy in impurity detection**

However, impurity detection remains **challenging when there are more phases to choose from**



N. J. Szymanski *et al.*, *npj Computational Materials* (2023).

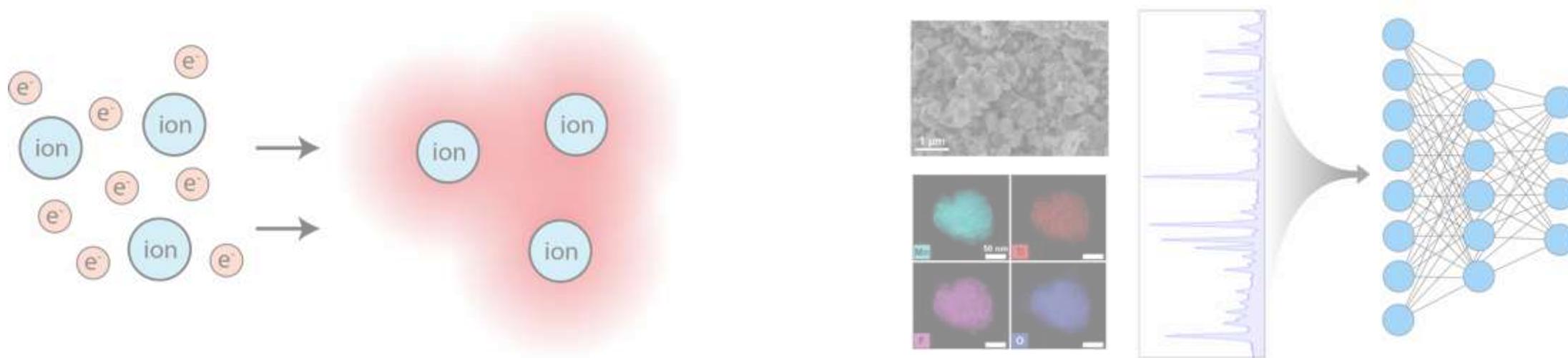




DFT for synthesis planning

AI for characterization

Computational tools for synthesis and characterization



DFT for synthesis planning

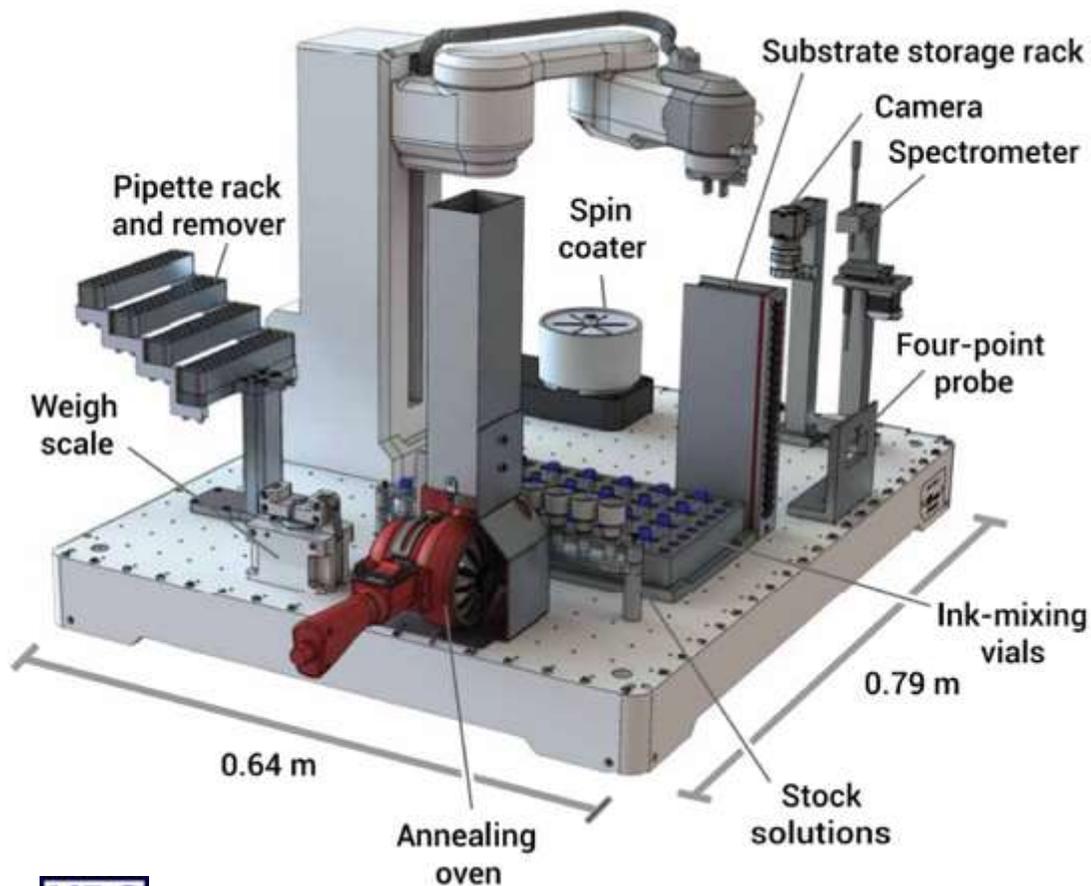
AI for characterization

Integrate these two approaches
for **closed-loop** experimental optimization

**Self-driving
labs**



Self-driving labs are being developed around the globe



Automated thin film growth



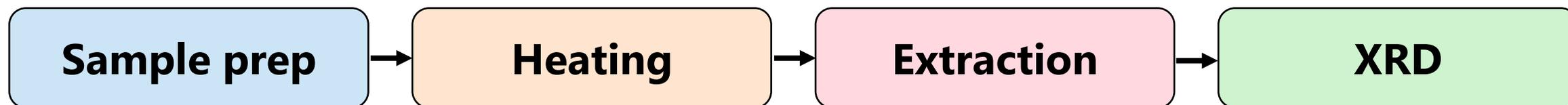
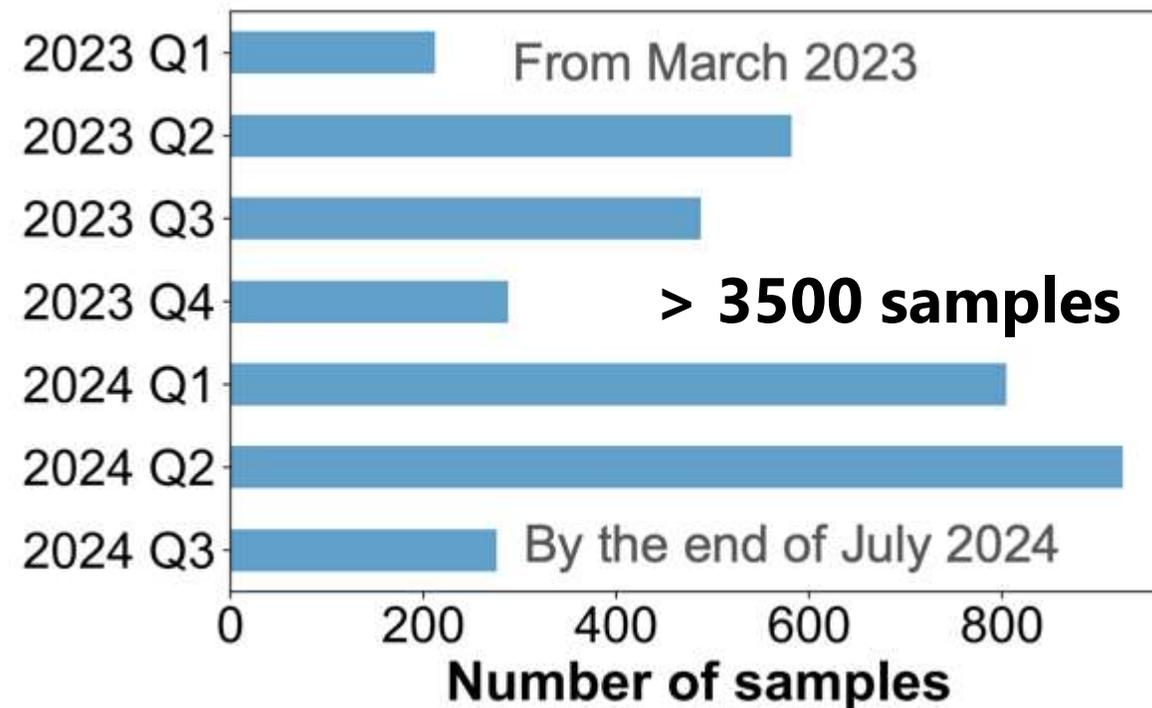
Automated solution-based synthesis

MacLeod *et al.*, *Science Advances* (2020).

Burger *et al.*, *Nature* (2020).



Automated solid-state synthesis for inorganic materials

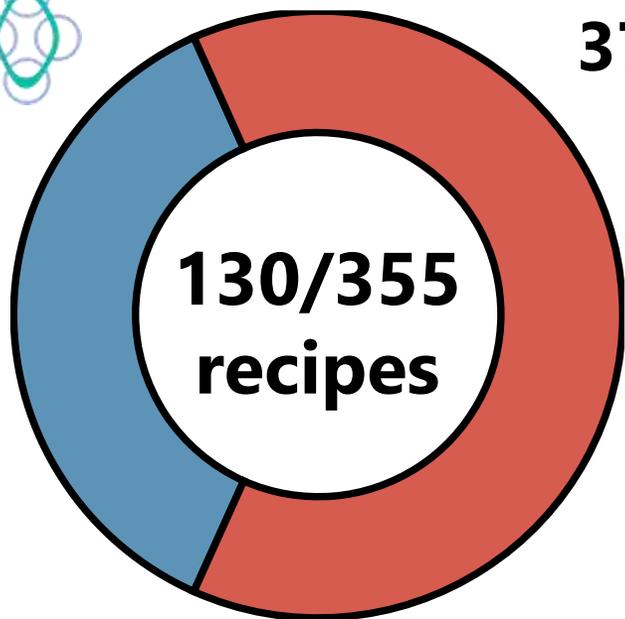


N. J. Szymanski *et al.*, Nature (2023).

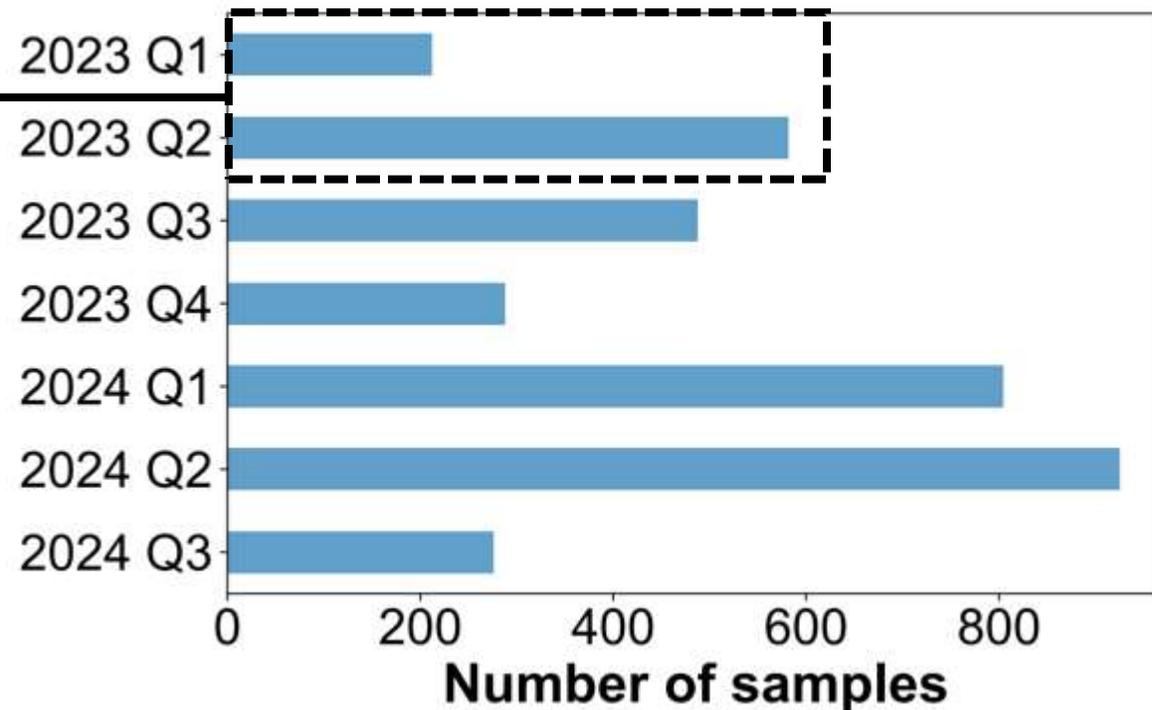
Y. Fei *et al.*, Digital Discovery (2024).



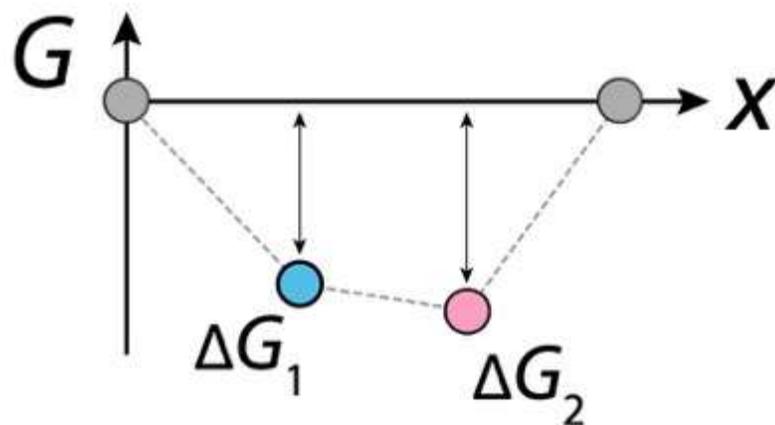
Challenge #1: most experimental iterations fail



**37% success
per recipe**



**Computed phase
diagrams only
get us so far**

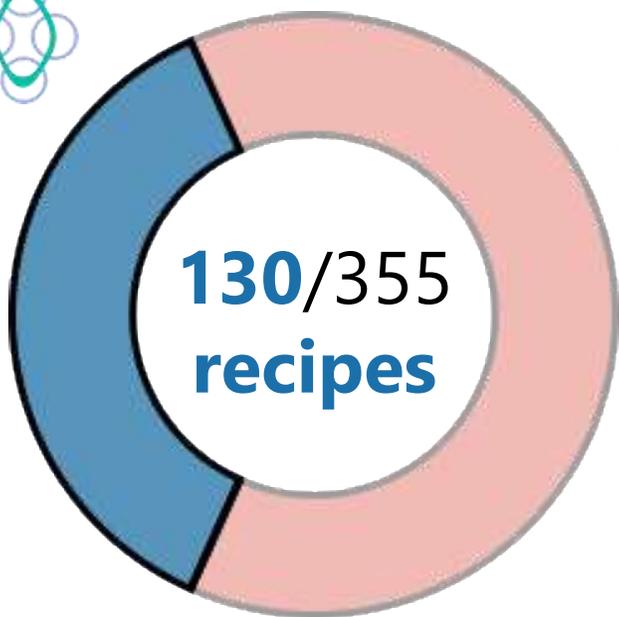


ARROWS³
Autonomous Reaction Route Optimization
With Solid-State Synthesis

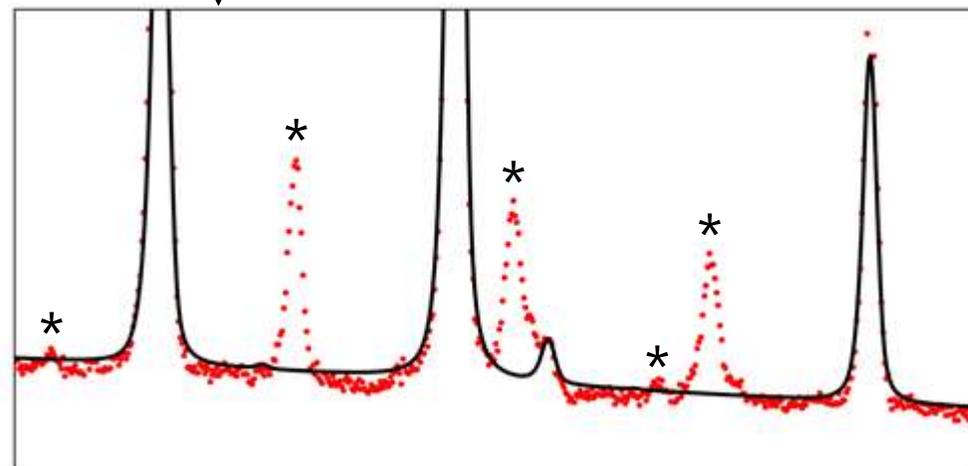
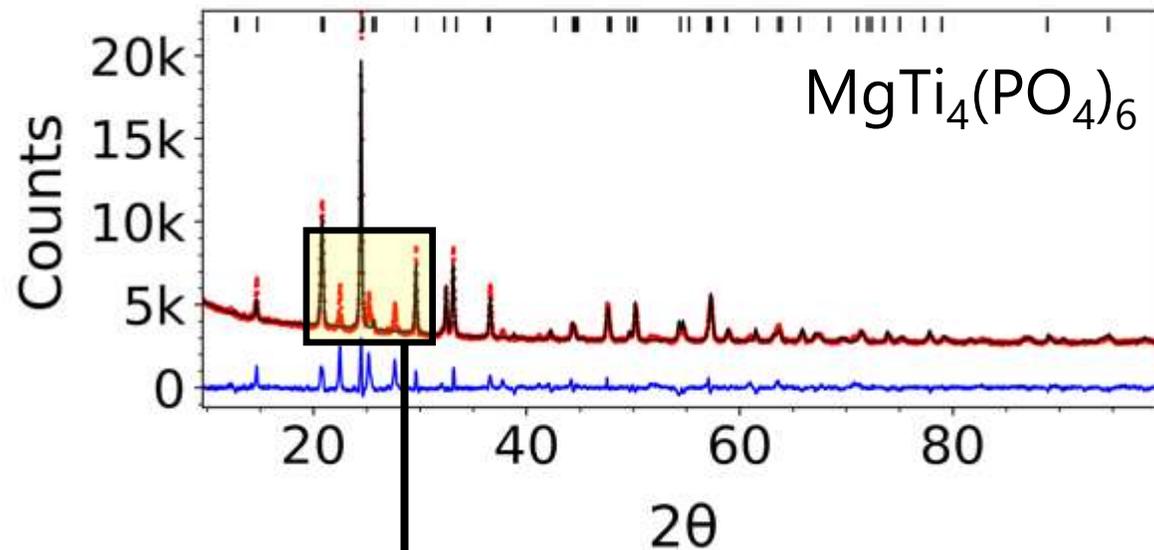
N. J. Szymanski *et al.*, Nature (2023).



Challenge #2: materials characterization remains difficult



Conventional
(*ex-situ*) XRD

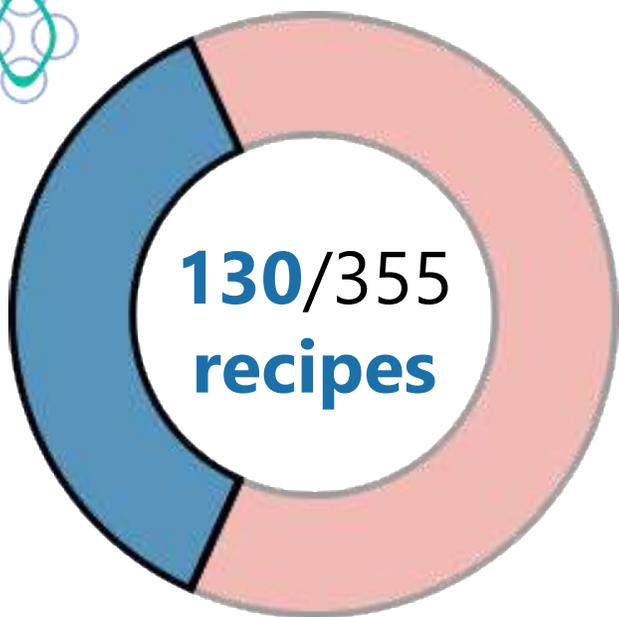


Successful syntheses often still contain **impurities**, which the **AI struggles to identify**

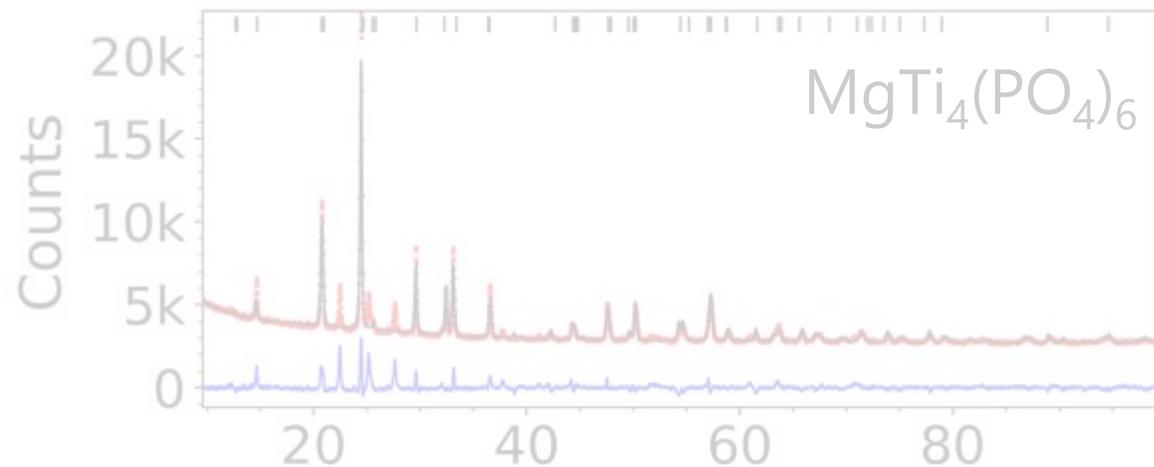
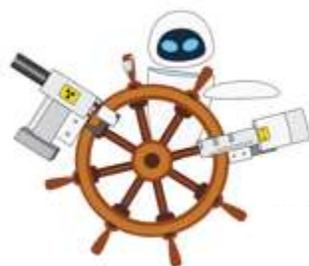
Leeman *et al.*, PRX Energy (2024).



Challenge #2: materials characterization remains difficult

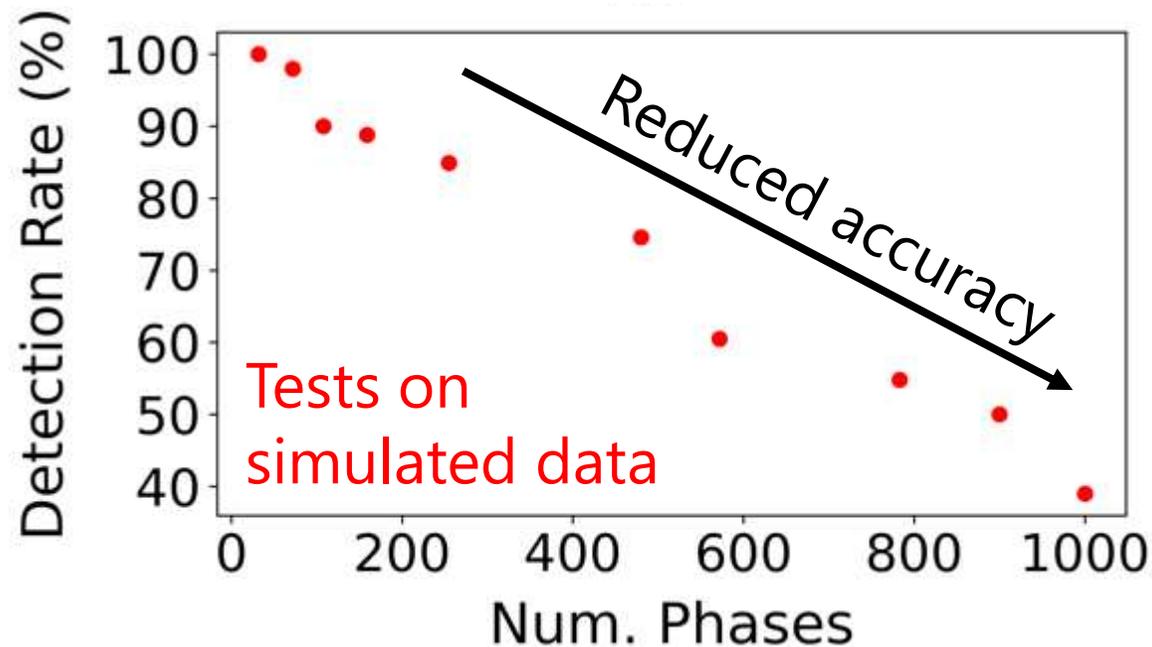


Conventional
(*ex-situ*) XRD



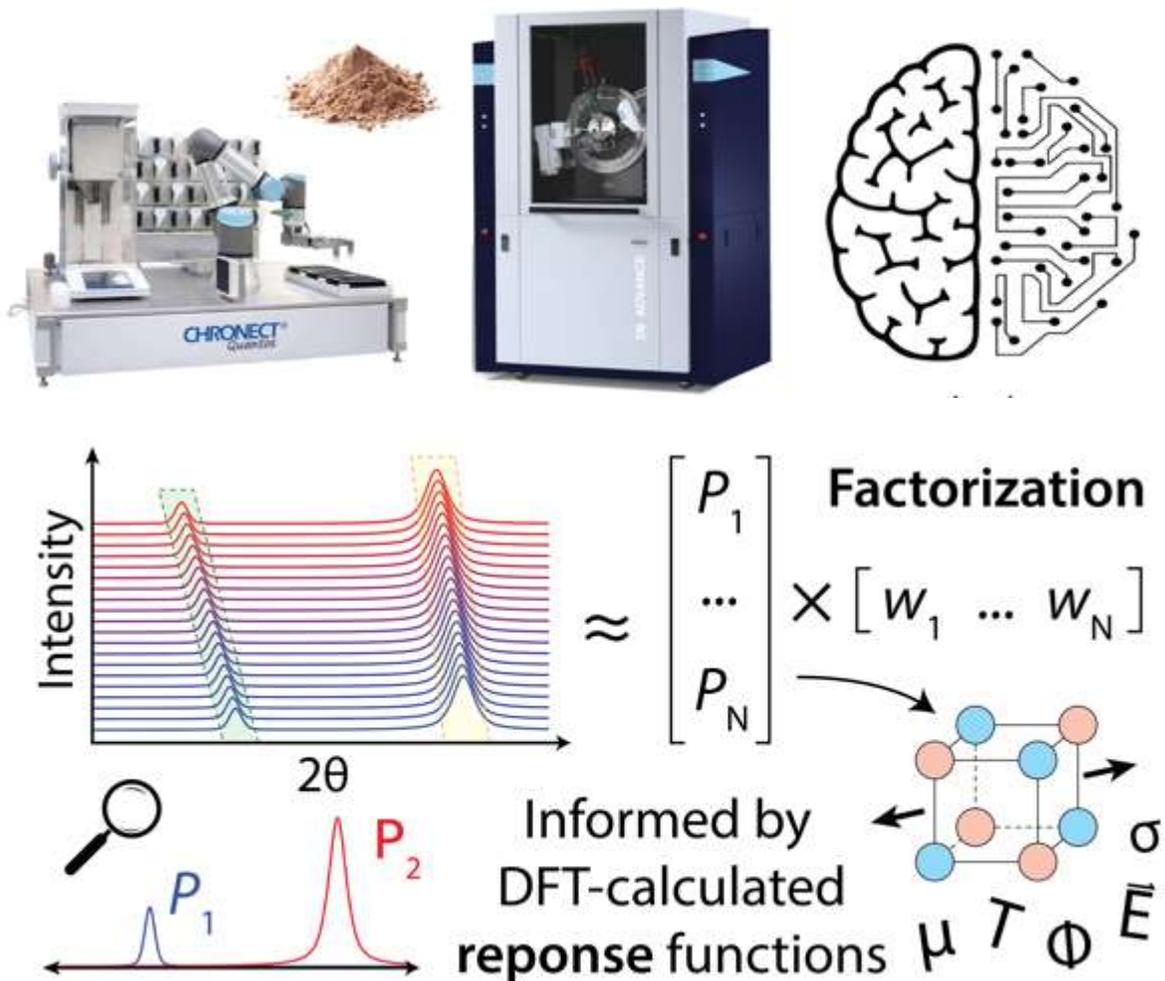
Adaptive XRD can help with impurity detection, but its accuracy still decreases in many-component chemistries

***Ex-situ* XRD only gets us so far**

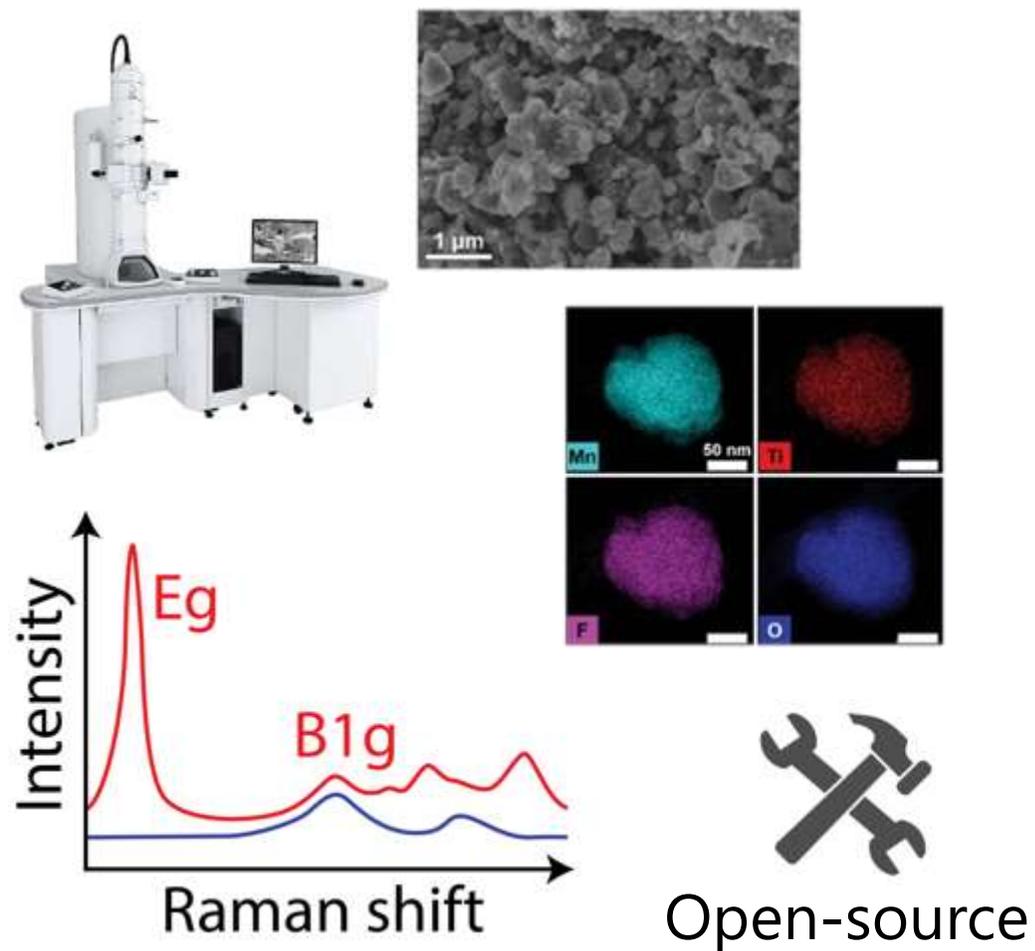


Future: additional characterization, with a focus on *in-situ*

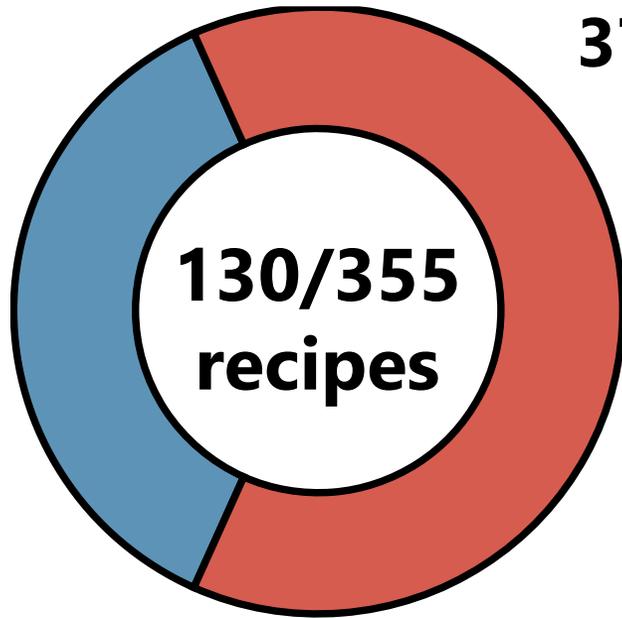
High-throughput *in-situ* XRD



ML for complementary techniques



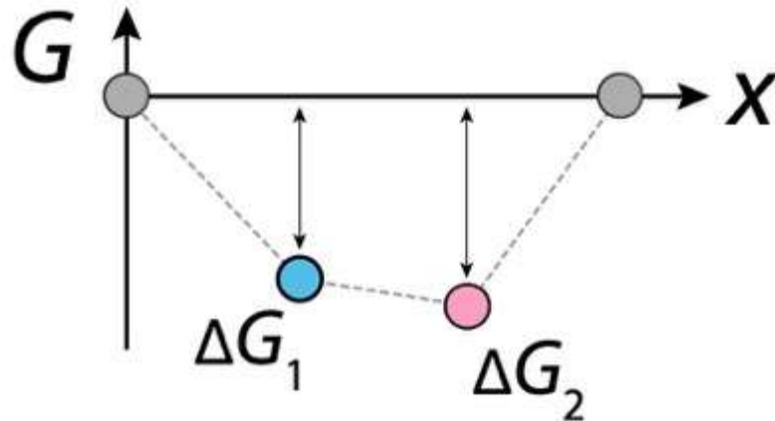
Challenge #1: most experimental iterations fail



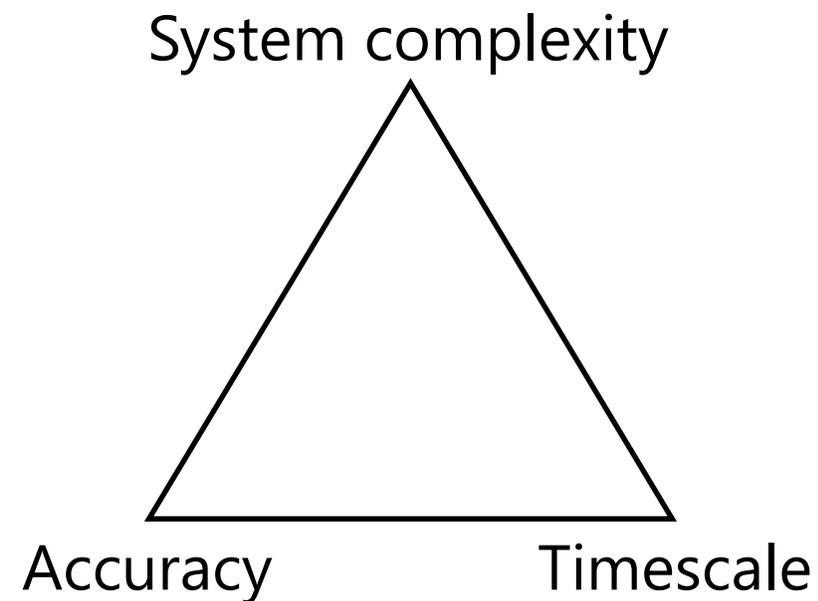
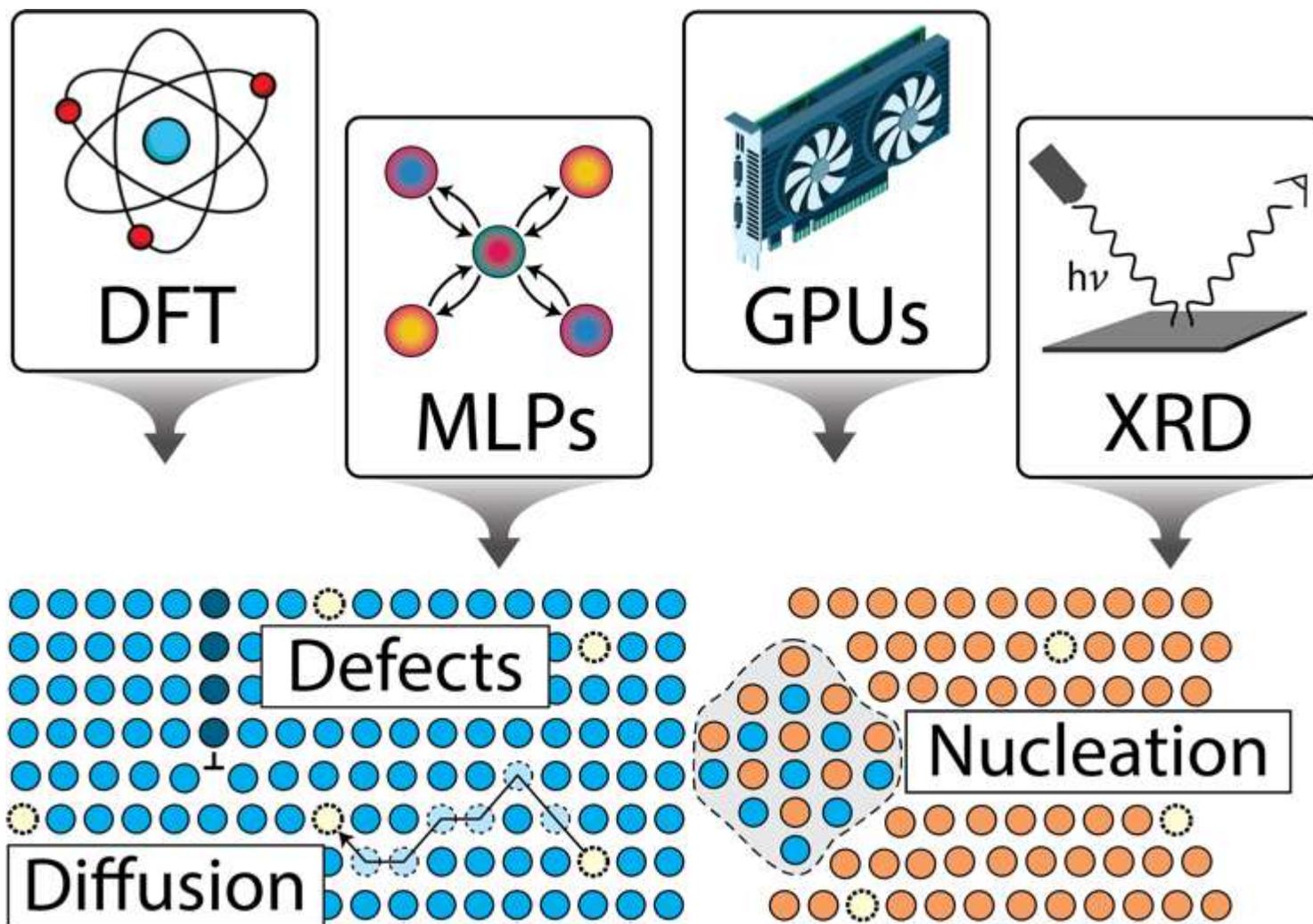
**37% success
per recipe**

How to overcome the low success rate of thermodynamic-based synthesis design?

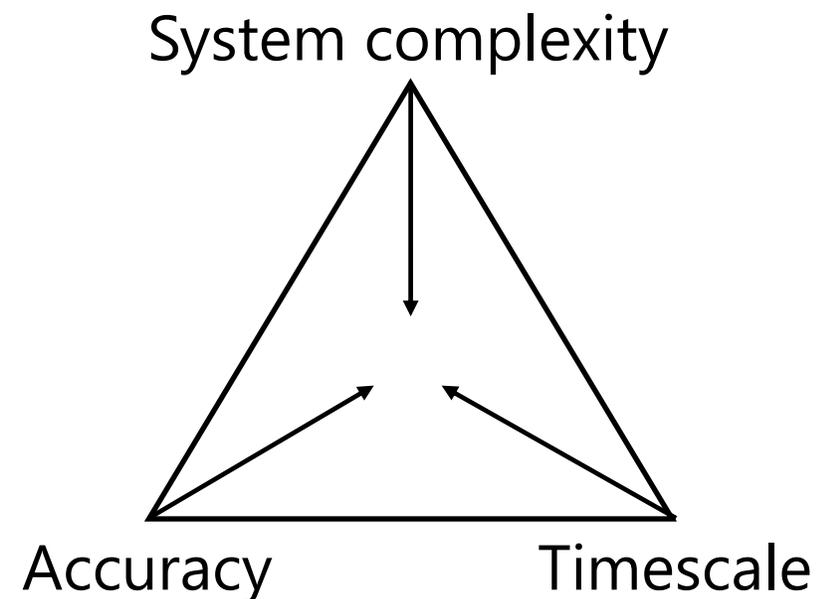
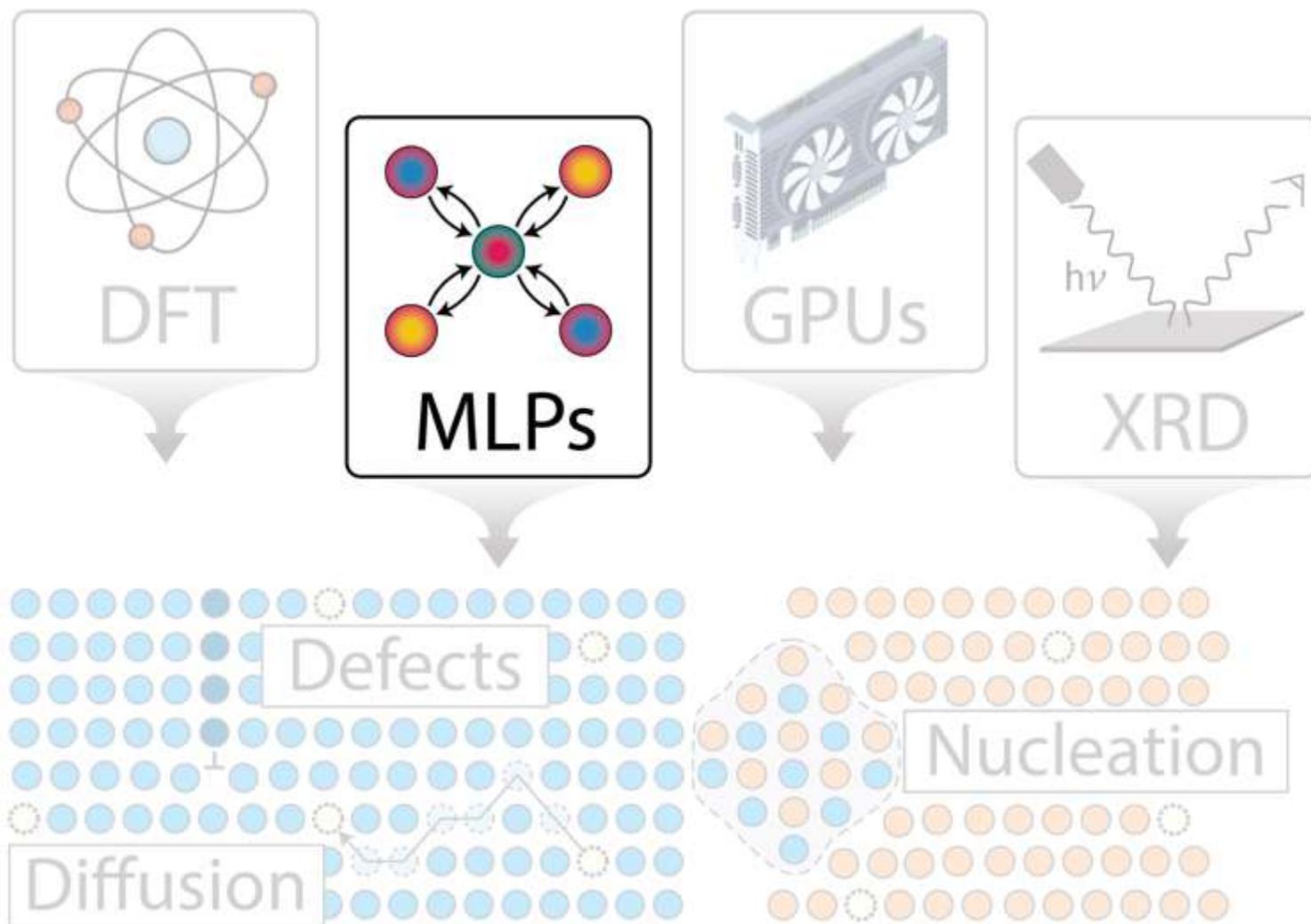
Computed phase diagrams only get us so far



Future: directly simulate the *kinetics* of solid-state reactions



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Leverage **machine learning** to bridge this gap in the simulation of kinetics

Acknowledgements

